Optimal flow sensor placement on wastewater treatment plants.

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Abstract

Obtaining high quality data collected on wastewater treatment plants is gaining increasing attention in the wastewater engineering literature. Typical studies focus on recognition of faulty data with a given set of installed sensors on a wastewater treatment plant. Little attention is however given to how one can install sensors in such a way that fault detection and identification can be improved. In this work, we develop a method to obtain Pareto optimal sensor layouts in terms of cost, observability, and redundancy. Most importantly, the resulting method allows reducing the large set of possibilities to a minimal set of sensor layouts efficiently for any wastewater treatment plant on the basis of structural criteria only, with limited sensor information, and without prior data collection. In addition, the developed optimization scheme is fast. Practically important is that the number of sensors needed for both observability of all flows and redundancy of all flow sensors is only

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one more compared to the number of sensors needed for observability of all flows in the studied WWTP configurations.

1. Introduction

Asset management of urban water infrastructures is the set of practices that utilities execute to ensure that infrastructure performance corresponds to service targets over time, that risks are adequately managed, and that the corresponding costs are as low as possible. Water asset management cannot be understood without proper data collection, either from routine off-line measurements or online data gathered from sensors and actuators. Modern small wastewater treatment plants (WWTPs) generate up to 500 signals, whereas larger ones typically register over 30,000 (Olsson et al., 2014). Despite the data-rich nature of modern WWTPs, limited useful information is typically generated, often due to improper sensor placement, installation, and/or maintenance. As a result, the resources – both in terms of time and capital – spent on installing and maintaining on-line sensors, and on collecting and storing on-line data in databases, are to a large extent lost since the collected data is not transformed into actionable knowledge for system optimization. Despite the historical recognition of the need for high quality data (Rieger et al., 2010), sub-optimal operation of a WWTP is still the norm rather than the exception. This situation is unacceptable given the need for an efficient, resilient, and sustainable use of available resources.

The focus of this paper is on sensor placement as a way to improve

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fault detection performance. This has been studied for safety-critical systems such as drinking water supply systems (Hart and Murray, 2010), but is not addressed for WWTPs. The placement of sensors on a WWTP typically responds to arbitrary choices, regulatory needs, or controller performance (Rehman et al., 2015). Furthermore, practically all studies focusing on data quality and fault detection in WWTPs consider the available sensor signals a given (e.g., Corominas et al., 2011; Maere et al., 2012; Puig et al., 2008; Rosén and Lennox, Rosen2001; Spindler and Vanrolleghem, 2012; Spindler, 2014; Villez et al., 2012; Villez and Habermacher, 2016; Yoo et al., 2004, 2006a,c,b). However, sensor placement can also be conducted wisely to increase redundancy and hence, improve the overall reliability of the plant. Indeed, the placement of sensors affects *(i)* the ability to reduce random errors, i.e. improve noise reduction and estimation accuracy (*What is the best estimate?*) and *(ii)* fault detection performance (*Is there a fault?*). Our vision is therefore that prior optimal sensor placement can be conducted to increase redundancy and hence, facilitate (posterior) fault detection for WWTP measurements.

For the placement of flow sensors, methods based on structural observability and redundancy criteria are applicable (Meyer et al., 1994). Such methods only consider whether a particular variable can be estimated (structural observability) and whether a sensor fault can be detected (structural redundancy). Structural criteria allow evaluating a sensor layout without detailed sensor information, such as failure rates or measurement uncertainty. We therefore adopt this approach and evaluate to which extent these structural criteria alone permit sensor layout optimization in typical WWTPs.

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The proposed method is inspired by earlier studies focused on drinking water supply systems (Hart and Murray, 2010) and complex plants (Meyer et al., 1994). As in earlier works we make use of graph-based methods for evaluation of observability and redundancy criteria (Kretsovalis and Mah, 1987, 1988a,b; Ponzoni et al., 1999, 2004). In contrast to earlier sensor placement studies, the sensor placement problem *(i)* is posed as a multi-objective optimization problem, *(ii)* is solved to guaranteed global optimality, and *(iii)* leads to an enumeration of all Pareto-optimal sensor layouts. In addition, cost, observability, and redundancy are optimized simultaneously and optimal sensor layouts for typical WWTP configurations are discussed for the first time.

2. Materials and Methods

2.1. Studied systems

The three studied WWTP configurations are shown in Fig. 1a/c/e and are *(i)* a simple organics removing WWTP (Tchobanoglous et al., 2003) (WWTP1), *(ii)* a WWTP for nitrogen removal (WWTP2, the so-called modified Ludzack Ettinger, MLE) which is also a popular benchmark WWTP (Gernaey et al., 2014), and *(iii)* a WWTP for biological nitrogen and phosphorus removal, namely the modified University of Cape Town (MUCT) system(Tchobanoglous et al., 2003) (WWTP3). In all cases, each flow is considered a feasible candidate for sensor placement.

2.2. Sensor placement as a multi-objective optimization problem

Problem description. The sensor placement problem consists of finding sensor layouts which are optimal in terms of cost, observability, and redundancy. A

variable is *structurally observable* when *(i)* a measurement of this variable is available or *(ii)* a unique value for the variable can be computed by means of a set of balance equations and other measurements. A sensor is considered *structurally redundant* if the measured variable remains observable when the considered sensor is removed. For optimization purposes, a sensor layout is described by means of binary *decision variables*, x_j, which represent the absence (0) or presence (1) of a sensor for flow j. Given values for all flows, $\boldsymbol{x}$, one can compute which variables are observable and which of the placed sensors are redundant. Practically, y_j indicates whether flow j is observable (1) or not (0). Similarly, z_j indicates whether flow j is equipped with a redundant sensor (1) or not (0). The set of feasible sensor layouts consists of all considered vectors $\boldsymbol{x}$ and is further referred to as the root set. All symbols used in what follows are given in Table 1.

For the purpose of optimization, the cost, observability, and redundancy objectives are:

$$f_C(\boldsymbol{x}) \;=\; \sum_j w_{x,j} \cdot x_j = \boldsymbol{w}_x^T \cdot \boldsymbol{x} \tag{1}$$

$$f_O(\boldsymbol{x}) \;=\; \sum_j w_{y,j} - \sum_j w_{y,j} \cdot y_j = \boldsymbol{w}_y^T \cdot (\boldsymbol{1} - \boldsymbol{y}) \tag{2}$$

$$f_R(\boldsymbol{x}) \;=\; \sum_j w_{z,j} - \sum_j w_{z,j} \cdot z_j = \boldsymbol{w}_z^T \cdot (\boldsymbol{1} - \boldsymbol{z}) \tag{3}$$

with $w_{x,j}$, $w_{y,j}$, and $w_{z,j}$ non-negative weights. The optimization problem consists of finding vectors $\boldsymbol{x}$ which minimize $f_C(\boldsymbol{x})$, $f_O(\boldsymbol{x})$, and $f_R(\boldsymbol{x})$. Without loss of generality, all results are obtained with the weights set equal to one:

$$\forall j \in \{1, 2, \ldots, n_j\} \;\; : \;\; \{w_x(j) = 1 \wedge w_y(j) = 1 \wedge w_z(j) = 1\} \tag{4}$$

Nature of the problem. The optimization problem described above is an integer program. Despite this complexity, the following rules are easily verified:

$$\forall a, b : \boldsymbol{x}_a \leq \boldsymbol{x}_b \quad \Rightarrow \quad f_C(\boldsymbol{x}_a) \leq f_C(\boldsymbol{x}_b) \tag{5}$$

$$\forall a, b : \boldsymbol{x}_a \leq \boldsymbol{x}_b \quad \Rightarrow \quad f_O(\boldsymbol{x}_a) \geq f_O(\boldsymbol{x}_b) \tag{6}$$

$$\forall a, b : \boldsymbol{x}_a \leq \boldsymbol{x}_b \quad \Rightarrow \quad f_R(\boldsymbol{x}_a) \geq f_R(\boldsymbol{x}_b) \tag{7}$$

Equations (5)-(7) are used below to prove the lower bounds.

2.3. Labeling observable variables and redundant sensors

To evaluate $\boldsymbol{y}$ and $\boldsymbol{z}$, graph-based labeling procedures are used. The graphs (Deo, 2004) for the studied WWTPs are given in Fig. 1b/d/f. Edges correspond to flows in the WWTP. *Cycles* and *components* are critical concepts for our method. A cycle is defined here as a non-empty combination of edges in a graph which enables to connect a given node to itself by traversing one or more edges of the graph in any direction and without repetition. A component or connected component is a subgraph (Deo, 2004) within which each pair of nodes can be connected by traversing the edges of the graph.

Labeling is executed as follows. First, label all edges with measurements as observable and remove them from the graph. In the reduced graph, label the edges which are not on a cycle as observable. Label all other edges as unobservable. For redundancy labeling, identify all components of the reduced graph. For each of the removed edges, evaluate whether the start and end node are in different components and label the measurement as redundant when so. All remaining measurements are non-redundant. For proofs we refer to the existing literature (Stanley and Mah, 1981; Kretsovalis and Mah, 1988a,b).

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2.4. Optimization

Optimization is executed by multi-objective branch-and-bound optimization in a breadth-first manner (Nemhauser and Wolsey, 1988; Ehrgott and Gandibleux, 2002). This is a deterministic algorithm for nonlinear global optimization as explained in the Supplementary Information (S.I.). The necessary bounds are given in the next section. The specific Matlab-based software needed to reproduce our results is published under the GPL v3 license and is added in the S.I. All computations were executed with Matlab R2014b (64-bit, win64) on a Lenovo ThinkPad X240 (Applied CPU: 1.40 GHz, Available RAM: 4.00 GB).

2.5. Bounds

At every branch-and-bound iteration, one evaluates the bounds to the objectives for a set of sensor layouts, $\mathcal{X}$. Each set consists of layouts for which some, none, or all values x_j are the same. For a remaining set of flows, the value for x_j can be 0 or 1. Consider two extremal sensor layouts within the set. The first of these layouts, $\underline{\boldsymbol{x}_{\mathcal{X}}}$, is the solution corresponding to placing sensors only in the locations for which every sensor layout within the set includes a sensor:

$$\underline{\boldsymbol{x}_{\mathcal{X}}}(j) = \begin{cases} 1 & \text{if } \forall \boldsymbol{x} \in \mathcal{X} : \boldsymbol{x}(j) = 1 \\ 0 & \text{otherwise} \end{cases} \tag{8}$$

The second extremal sensor layout, $\overline{\boldsymbol{x}_{\mathcal{X}}}$, is obtained by placing a sensor in every location for which at least one sensor layout in the set includes a sensor:

$$\overline{\boldsymbol{x}_{\mathcal{X}}}(j) = \begin{cases} 1 & \text{if } \exists \boldsymbol{x} \in \mathcal{X} : \boldsymbol{x}(j) = 1 \\ 0 & \text{otherwise} \end{cases} \tag{9}$$

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2.5.1. Upper bounds

In this study, upper bounds are obtained for the $\overline{\boldsymbol{x}_{\mathcal{X}}}$ solution:

$$\overline{f}_C = f_C(\overline{\boldsymbol{x}_{\mathcal{X}}}) \;=\; \boldsymbol{w}_x^T \cdot \overline{\boldsymbol{x}_{\mathcal{X}}} \tag{10}$$

$$\overline{f}_O = f_O(\overline{\boldsymbol{x}_{\mathcal{X}}}) \;=\; \boldsymbol{w}_y^T \cdot (\mathbf{1} - \overline{\boldsymbol{y}_{\mathcal{X}}}) \tag{11}$$

$$\overline{f}_R = f_R(\overline{\boldsymbol{x}_{\mathcal{X}}}) \;=\; \boldsymbol{w}_z^T \cdot (\mathbf{1} - \overline{\boldsymbol{z}_{\mathcal{X}}}) \tag{12}$$

The values for $\overline{\boldsymbol{y}_{\mathcal{X}}}$ and $\overline{\boldsymbol{z}_{\mathcal{X}}}$ are determined with the provided labeling procedures. These are valid upper bounds since the computed objective values are simultaneously attained with a single solution $(\overline{\boldsymbol{x}_{\mathcal{X}}})$ in the considered set.

2.5.2. Lower bounds

The lower bounds are obtained as follows. The lowest value of the cost within a set is obtained for the $\underline{\boldsymbol{x}_{\mathcal{X}}}$ solution. Based on Eq. 5 one obtains:

$$\forall \boldsymbol{x} \in \mathcal{X} : \underline{\boldsymbol{x}_{\mathcal{X}}} \leq \boldsymbol{x} \Rightarrow \underline{f_C} = f_C(\underline{\boldsymbol{x}_{\mathcal{X}}}) \leq f_C(\boldsymbol{x}) \tag{13}$$

The lowest value of the observability function within a set is obtained for the $\overline{\boldsymbol{x}_{\mathcal{X}}}$ solution. This follows from Eq. 6:

$$\forall \boldsymbol{x} \in \mathcal{X} : \left\{ \overline{\boldsymbol{x}_{\mathcal{X}}} \geq \boldsymbol{x} \Rightarrow \overline{\boldsymbol{y}_{\mathcal{X}}} \geq \boldsymbol{y} \Rightarrow \underline{f_O} = f_O(\overline{\boldsymbol{x}_{\mathcal{X}}}) \leq f_O(\boldsymbol{x}) \right\} \tag{14}$$

The lowest value of the redundancy objective within a set is obtained for the $\overline{\boldsymbol{x}_{\mathcal{X}}}$ solution. This follows from Eq. 7:

$$\forall \boldsymbol{x} \in \mathcal{X} : \left\{ \overline{\boldsymbol{x}_{\mathcal{X}}} \geq \boldsymbol{x} \Rightarrow \overline{\boldsymbol{z}_{\mathcal{X}}} \geq \boldsymbol{z} \Rightarrow \underline{f_R} = f_R(\overline{\boldsymbol{x}_{\mathcal{X}}}) \leq f_R(\boldsymbol{x}) \right\} \tag{15}$$

3. Results

The basic methodological concepts are demonstrated first by means of WWTP1. Afterwards, the results for WWTP2 and WWTP3 are discussed.

3.1. WWTP1

3.1.1. Sensor layout examples

Each of the seven flows in Fig. 1(a) is given as an edge in Fig. 1(b). The nodes a, b, c, and d correspond to physical locations. A fifth node, e, is the *environmental node* which represents the system boundary. This makes it a mathematically consistent graph, i.e. there are no loose ends.

To demonstrate the labelling procedures, consider that F1 and F6 are measured (layout A). Flows F1 and F6 are then removed for observability labeling (Fig. 2, top-left). Edges not lying on any cycle correspond to observable flows (F2, F3). All other flows are on cycles and thus unobservable (F4, F5, F7). The resulting graph consists of a single component so that all sensors are non-redundant. The situation changes when a flow sensor is added for the excess sludge flow (F7, layout B). Now there are no cycles (Fig. 2, top-right). Therefore, all flows are observable. Once more, a single-component graph results and the sensors remain non-redundant. Another sensor is now placed at the exit of the reactor (F3, layout C). All flows remain observable (Fig. 2, bottom-left). Two graph components result after removal of measured flows. The start and end nodes of edges 1, 3, and 6 correspond to different components, so F1, F3, and F6 are redundant. This is because these flow measurements are tied through a balance equation. In contrast, edge 7 has start and end nodes on the same component of the graph. Equivalently, no balance equation without unmeasured flows and including the F7 measurement exists. Therefore, F7 is non-redundant. Adding another sensor for the WWTP effluent (F4, layout D) makes all sensors redundant (Fig. 2, bottom-right). These results are summarized in Table 2.

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3.1.2. Pareto-optimal sensor layouts

Deterministic optimization is now used to evaluate the Pareto optimal sensor layouts. The complete set of feasible solutions consists of $2^7 = 128$ solutions. Ten distinct Pareto-optimal combinations for the objectives are shown in Fig. 3 with bubble sizes reflecting the number of layouts for each combination. These combinations and all individual solutions are listed in S.I. (Table S.1, Table S.2). Layouts A, B, and D discussed above are part of the Pareto front. Layout C is not part of this Pareto front. A total of 70 layouts lie on the Pareto front. Of these layouts, 37 layouts exhibit no redundant sensors (layouts 1-37), 38 layouts render all variables observable and all sensors redundant (layouts 43-70), and five layouts exhibit some redundant sensors while not all variables are observable (layouts 38-42). Note that these 5 layouts cannot be obtained through conventional optimization methods since these methods (e.g., Ali and Narasimhan, 1998) add sensors first until all variables are observable and proceed to increase the number of redundant sensors only after this is achieved. The Pareto front contains the layout without any sensors as a trivial solution (layout 1) and 23 layouts with three non-redundant sensors making all variables observable (layout 14-37). Four sensors are sufficient to make all variables observable and all sensors redundant. Five such layouts exist (layout 43-47).

3.2. WWTP2 (MLE)

3.2.1. Sensor layout examples

Fig. 1(d) shows the graph representation of WWTP2. In Table 3, the results for a few layouts on the Pareto front are displayed in detail. Layout A is a layout with measurements for F3, F8, F10, and F11. In this case, eight

flows are observable and none of the sensors is redundant. F6, F7, and F9 remain unobservable. Adding a sensor for F9 makes all flow rates observable (layout B). None of the sensors is redundant. Adding another sensor in F6 makes all placed sensors redundant (layout C). Layout D is a layout where all sensors are redundant but not all variables observable. Sensors are placed in F1, F4, F8, F10, and F11. F6, F7, and F9 remain unobservable as is the case for layout A.

A typical plant may already have sensors for the influent flow (F1) and flows equipped with pumps (F8-11). This makes all flows observable based on the labeling procedures discussed above. This is typical and means that all flows are observable in most WWTPs. In this case, at least two more sensors (seven sensors in total) are necessary to make all sensors redundant if the already installed sensors are kept in their positions. However, layout C has only six sensors while all flows are observable and all sensors are redundant. There are no minimal sensor layouts with all sensors redundant which include sensors for F1 and F8-11 simultaneously. The Pareto optimal set of sensor layouts thus depends on previously installed sensors. This can be taken into account easily by setting the corresponding cost weights ($w_{x,j}$) to zero. This is however not studied in detail.

3.2.2. Pareto-optimal sensor layouts

In the WWTP2 (MLE) case, there are eleven distinct flows for which a sensor can be placed. This leads to a total of $2^{11} = 2048$ feasible sensor layouts. The resulting Pareto front consists of 609 layouts in 15 unique objective combinations (Fig. 4). All combinations and solutions are given in the S.I. (Table S.3, Table S.4). Six combinations represent the 383 solutions

without any redundant sensors (layout 1-383). Five sensors are sufficient to make all flow rates observable. There exist 209 such layouts (layout 175-383). With one to four sensors, one obtains at most one, three, six, and eight observable flow rates (layouts 2-174). Placing six sensors is sufficient to make all flow rates observable while also making all sensors redundant. Interestingly, there exist only seven such layouts (layout 402-408). Beyond six installed sensors, each additional sensor placement will increase the cost and the number of redundant sensors with one unit (201 layouts, layout 409-609). There are 18 sensor layouts for which not all flow rates are observable while all installed sensors are redundant (layout 384-401). The number of observable variables is three, six, and eight for three, four, and five installed sensors.

3.3. WWTP3 (MUCT)

3.3.1. Sensor layout examples

Fig. 1(f) shows the graph representation of WWTP3. Table 4 lists four layouts on the Pareto front. The first (layout A) consists of four sensors placed in the excess sludge flow and the recycle flows (F9-12). Five flows are observable and there is no redundancy. Adding a sensor for F4 (anoxic reactor outlet) makes all variables observable (layout B). Adding another sensor for F7 (effluent) makes all sensors redundant (layout C). Layout D involves a flow sensor in the influent (F1), the anoxic reactor outlet (F4), and the recycle flows (F10-12). Nine flow rates are observable and all sensors are redundant. Note that adding a sensor for F4 might be unrealistic for many plants as F4 typically exists between two tank zones separated with a baffle. To account for this, one can set the corresponding value for x to zero

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in the root solution set or one can set the corresponding cost weight $(w_{x,j})$ to infinity. The effect of such changes is however not studied in detail.

3.3.2. Pareto-optimal sensor layouts

WWTP3 exhibits twelve distinct flows leading to $2^{12} = 4048$ feasible layouts. The Pareto front in Fig. 5 contains 1154 of these. Sixteen unique points exist on this front and are described in detail in S.I. (Table S.5, Table S.6). Six of the points represent 577 solutions without redundancy (layout 1-577). These include the trivial solution without any sensors (layout 1) and 336 layouts with five sensors which make all flows observable (layout 242-577). Adding sensors delivers layouts with additional redundant sensors (layouts 609-1154). Interestingly, only ten layouts exist with six sensors for which all variables are observable and all sensors are redundant. The Pareto front also contains 31 layouts for which all sensors are redundant while not all flow rates are observable (layout 578-608).

4. Discussion

In what follows, the main benefits of the applied optimization method as demonstrated above are given, followed by more general observations regarding the solved sensor placement problem and a few considerations regarding future work.

4.1. Benefits of the optimization method

In this study, Pareto optimal flow sensor layouts are found by means of a deterministic optimization scheme combined with graph-based evaluation

of structural observability and redundancy. These are the most important benefits of this method:

- Using structural objectives for optimization means that sensor layout optimization *(i)* can be executed for any plant as well as at the design stage of a new plant, *(ii)* does not require information regarding the performance of candidate sensors, and *(iii)* does not require collecting measurements prior to optimization. This is the most important benefit of the method.

- The provided Pareto front solutions are guaranteed to be globally optimal thanks to bounds on the objectives developed specifically for this work. At the same time, the time needed to compute the Pareto front was less than 20 minutes for all studied cases. This indicates that automated screening of candidate sensor layouts on the basis of structural criteria is possible with conventionally available computational resources.

- All Pareto-optimal sensor layouts can be found by the proposed method, including sensor layouts with redundant sensors that do not make all flows observable. This is not guaranteed by conventional sequential optimization of observability and redundancy criteria. This of particular interest when only a few flows should be estimated with high accuracy and reliability while other flows are not of interest at all.

4.2. General observations

Based on the three case studies, the following observations can be made:

- Although the number of Pareto-optimal layouts tends to be large (e.g., 1154 for MUCT), the fraction of optimal layouts among all feasible layouts is reduced considerably (28.2% and 29.7% for the realistic MLE and MUCT plants). Most likely, the resulting Pareto front is most valuable to assist the end-user with further elucidation of sensor layout preferences.

- Increasing the complexity of a WWTP configuration, particularly by increasing the number of flows, leads to a smaller fraction of feasible sensor layouts lying on the Pareto front. This is thought to be due to an increased presence of recycle flows.

- For the MLE and MUCT plants, installing five sensors is sufficient to achieve observability for all flows without any redundant sensors while installing six sensors is sufficient to achieve the same observability with this time with all sensors redundant. This shows that the additional investments to move from complete observability to complete observability and redundancy are small in many WWTPs.

- All flows were considered feasible sensor locations. However, some of the computed solutions require that a sensor is placed at the inlet of a reactor tank or at the inlet of the settler, which is not always feasible. Our method however allows accounting for this by setting the corresponding weights $(w_{x,j})$ to infinity or by redefining the root set so it does not contain infeasible sensor layouts prior to optimization. Similarly, already installed sensors or legally required instruments can be included automatically by redefining the root set so it contains only

sensor layouts which include these sensors. Importantly, the physical configuration of a WWTP and existing sensor placements can restrict the possibilities for sensor layout optimization. Plant design and sensor layout optimization is thus best considered simultaneously.

4.3. Outlook

The following enhancements are considered for future work:

- The inclusion of isolability criteria is considered valuable if one aims not only to facilitate data reconciliation (*What is the best estimate?*) and fault detection (*Is there a fault?*) but also to automatically execute fault isolation (*Which sensor signal(s) cause the detection?*), and *(iv)* improve diagnosis performance (*What is the root cause?*). Unfortunately, there is no algorithm yet for isolability labelling based on topological graphs as used in this work. Note however that an alternative approach based on a bipartite graph is available (Raghuraj et al., 1999).

- The addition of practical criteria for observability (Waldraff et al., 1998; Chmielewski et al., 2002) or redundancy (Ali and Narasimhan, 1998) will enable further refinement of the Pareto front. This however requires that detailed information about the candidate sensors is available.

5. Conclusions

In this study, a systematic search for optimal sensor layouts is solved as a deterministic multi-objective optimization problem involving cost, observability and redundancy objectives. The general applicability of the developed

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method is demonstrated by means of three popular wastewater treatment plant configurations. Our results indicate that the additional investments to move from complete observability to complete observability and redundancy requires only one additional flow sensor in the studied configurations. Finally and most importantly, the applied optimization method is fast and is applicable for any plant configuration without prior data collection or specification of sensor characteristics .

6. Acknowledgements

7. Supplementary Information

The Supplementary Information includes all code necessary to generate the results, detailed information regarding the optimization algorithm, and additional results.

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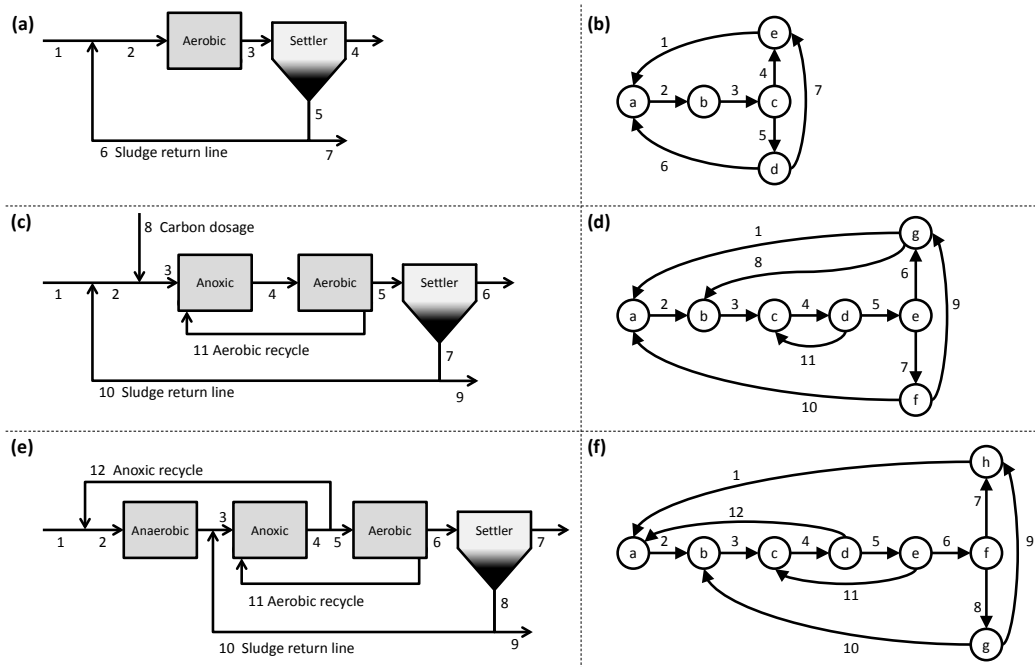
Figure 1: Schemes and graph representations of the studied plant layouts. WWTP1: *(a)* scheme, *(b)* graph. WWTP2 (MLE): *(c)* scheme, *(d)* graph. WWTP3 (MUCT): *(e)* scheme, *(f)* graph.
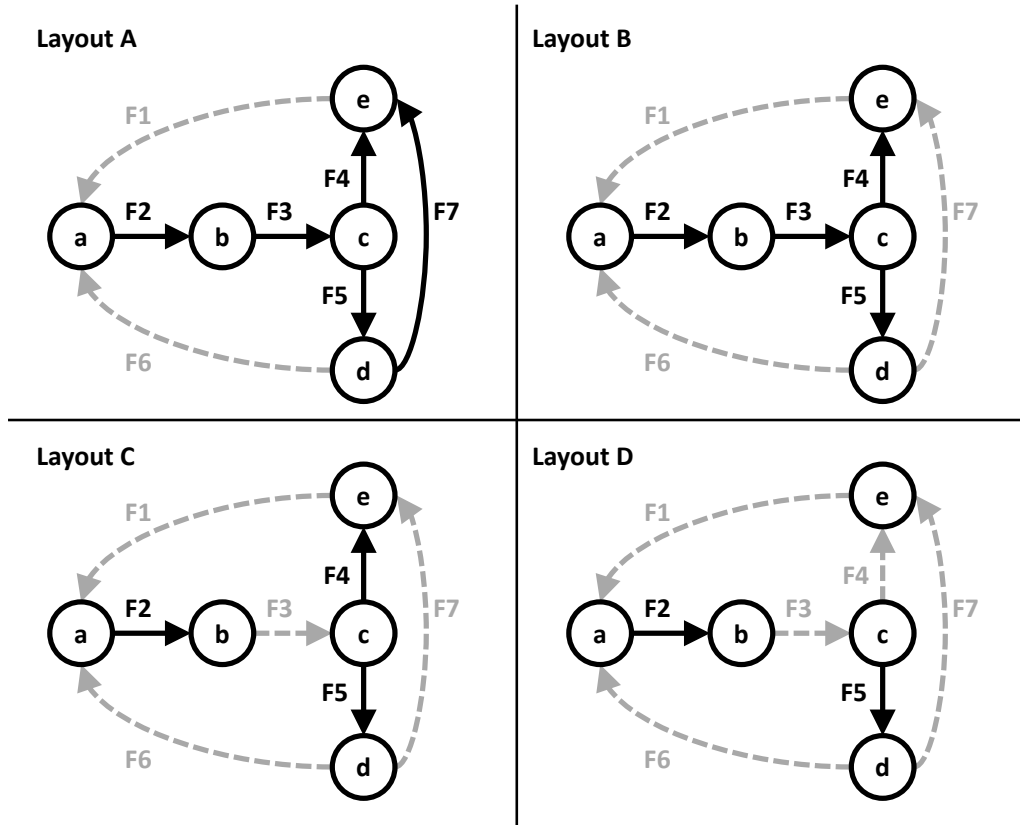
Figure 2: WWTP1. Modified graphs for four sensor layouts. Removed edges are dashed and grey. Layout A: observable: F2, F3, redundant: none. Layout B: observable: all, redundant: none. Layout C: observable: all, redundant: F1, F3, F6. Layout D: observable: all, redundant: all installed sensors.
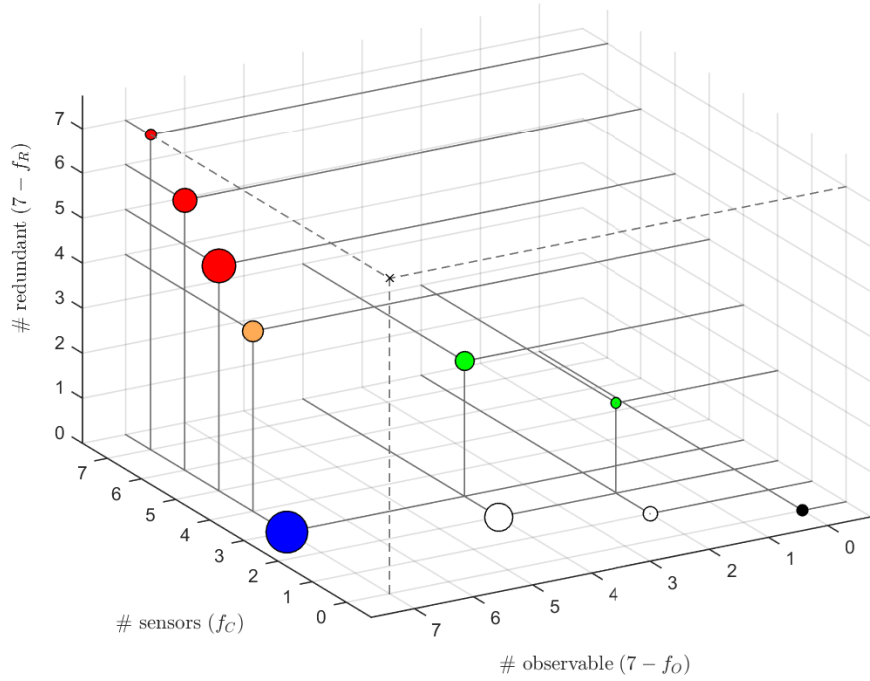
Figure 3: WWTP1. Visualization of the Pareto front. The size of the bubbles reflects the number of layouts in each point on the Pareto front. The ideal solution is indicated with dashed lines. Black: trivial sensor layout without any sensor. Blue: 23 layouts, observable: all, redundant: none. Green: five layouts, observable: some, redundant: some. Orange: five sensor layouts, cost: minimal, observable: all, redundant: all. Red: 33 layouts, observable: all, redundant: all. White: 13 layouts, observable: some, redundant: none.
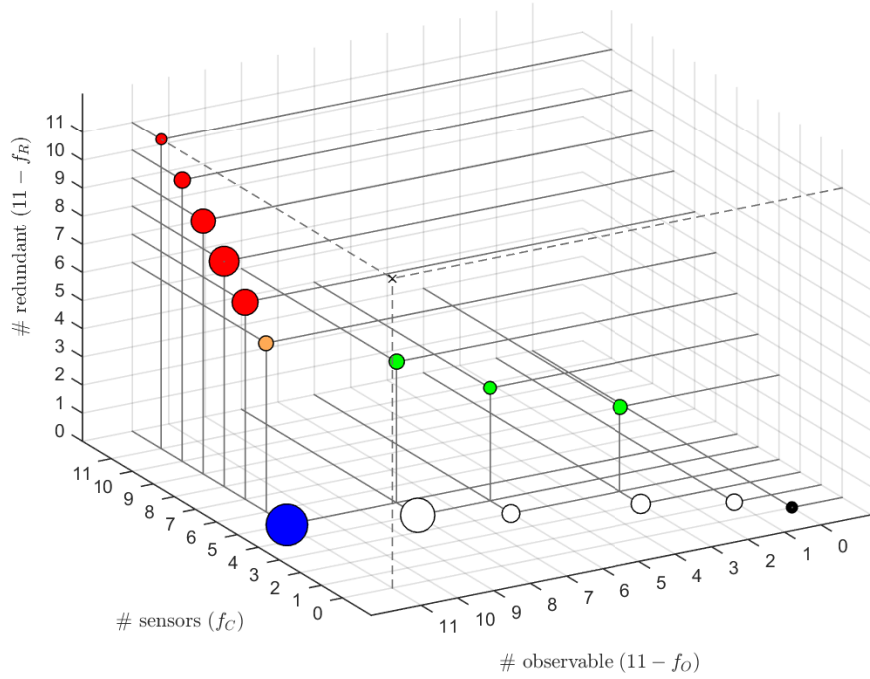
Figure 4: WWTP2 (MLE). Visualization of the Pareto front. The size of the bubbles reflects the number of layouts in each point on the Pareto front. The ideal solution is indicated with dashed lines. Black: trivial sensor layout without any sensor. Blue: 209 layouts, observable: all, redundant: none. Green: 18 layouts, observable: some, redundant: some. Orange: seven sensor layouts, cost: minimal, observable: all, redundant: all. Red: 201 layouts, observable: all, redundant: all. White: 173 layouts, observable: some, redundant: none.
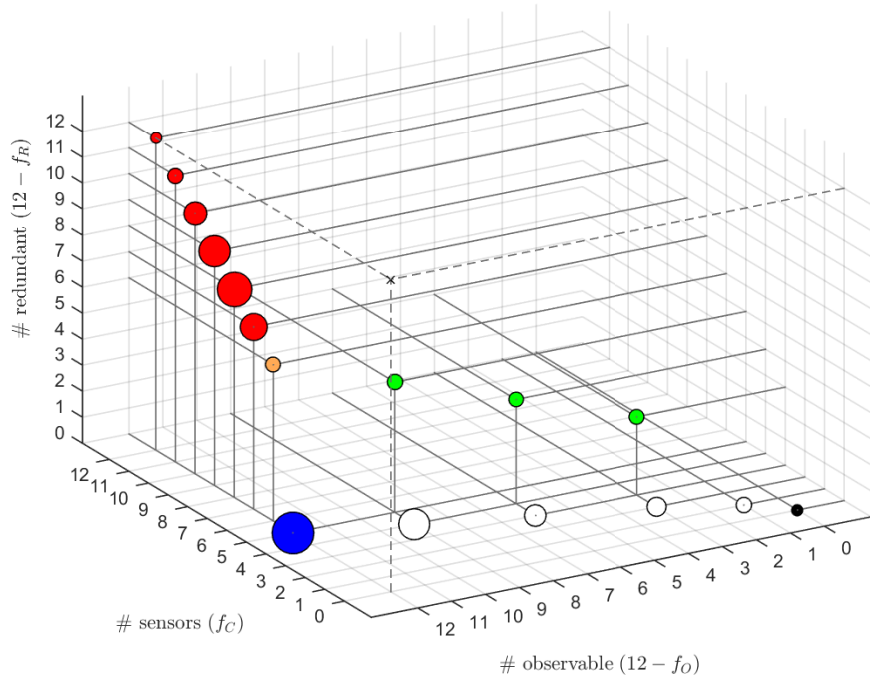
Figure 5: WWTP3 (MUCT). Visualization of the Pareto front. The size of the bubbles reflects the number of layouts in each point on the Pareto front. The ideal solution is indicated with dashed lines. Black: trivial sensor layout without any sensor. Blue: 336 layouts, observable: all, redundant: none. Green: 31 layouts, observable: some, redundant: all. Orange: ten sensor layouts, cost: minimal, observable: all, redundant: all. Red: 536 layouts, observable: all, redundant: all, White: 240 layouts, observable: some, redundant: none.

Symbol	Description
j	Flow index
$f_C(\boldsymbol{x})$	Cost objective
$f_O(\boldsymbol{x})$	Observability objective
$f_R(\boldsymbol{x})$	Redundancy objective
n_j	Number of flows
$\boldsymbol{w}_o(j),\, w_{o,j}$	Weight for flow j
$\boldsymbol{x}(j),\, x_j$	Presence of a sensor for flow j
$\boldsymbol{y}(j),\, y_j$	Observability of flow j
$\boldsymbol{z}(j),\, z_j$	Presence of a redundant sensor in flow j
$\underline{o_\mathcal{X}},\, \overline{o_\mathcal{X}}$	Lower/upper bound over the set $\mathcal{X}$
$\mathcal{X}$	Set of vectors x

Table 1: List of mathematical symbols.

Table 2: WWTP1. Observability and redundancy labelling for example layouts. Note that absence of a sensor ($x_j = 0$) logically implies the absence of a redundant sensor ($z_j = 0$).

Flow	Layout A			Layout B			Layout C			Layout D		
j	x	y	z	x	y	z	x	y	z	x	y	z
1	1	1	0	1	1	0	1	1	1	1	1	1
2	0	1	0	0	1	0	0	1	0	0	1	0
3	0	1	0	0	1	0	1	1	1	1	1	1
4	0	0	0	0	1	0	0	1	0	1	1	1
5	0	0	0	0	1	0	0	1	0	0	1	0
6	1	1	0	1	1	0	1	1	1	1	1	1
7	0	0	0	1	1	0	1	1	0	1	1	1

Table 3: WWTP2 (LME). Observability and redundancy labelling for example layouts. Note that absence of a sensor ($x_j = 0$) logically implies the absence of a redundant sensor ($z_j = 0$).

Flow j	Layout A			Layout B			Layout C			Layout D		
	x	y	z	x	y	z	x	y	z	x	y	z
1	0	1	0	0	1	0	0	1	0	1	1	1
2	0	1	0	0	1	0	0	1	0	0	1	0
3	1	1	0	1	1	0	1	1	1	0	1	0
4	0	1	0	0	1	0	0	1	0	1	1	1
5	0	1	0	0	1	0	0	1	0	0	1	0
6	0	0	0	0	1	0	1	1	1	0	0	0
7	0	0	0	0	1	0	0	1	0	0	0	0
8	1	1	0	1	1	0	1	1	1	1	1	1
9	0	0	0	1	1	0	1	1	1	0	0	0
10	1	1	0	1	1	0	1	1	1	1	1	1
11	1	1	0	1	1	0	1	1	1	1	1	1

Table 4: WWTP3 (MUCT). Observability and redundancy labelling for example layouts. Note that absence of a sensor ($x_j = 0$) logically implies the absence of a redundant sensor ($z_j = 0$).

Flow j	Layout A			Layout B			Layout C			Layout D		
	x	y	z	x	y	z	x	y	z	x	y	z
1	0	0	0	0	1	0	0	1	0	1	1	1
2	0	0	0	0	1	0	0	1	0	0	1	0
3	0	0	0	0	1	0	0	1	0	0	1	0
4	0	0	0	1	1	0	1	1	1	1	1	1
5	0	0	0	0	1	0	0	1	0	0	1	0
6	0	0	0	0	1	0	0	1	0	0	1	0
7	0	0	0	0	1	0	1	1	1	0	0	0
8	0	1	0	0	1	0	0	1	0	0	0	0
9	1	1	0	1	1	0	1	1	1	0	0	0
10	1	1	0	1	1	0	1	1	1	1	1	1
11	1	1	0	1	1	0	1	1	1	1	1	1
12	1	1	0	1	1	0	1	1	1	1	1	1

S. Supplementary Information

S.1. Software

All software necessary to reproduce the results presented in this work is available as the self-sufficient SOAR package for Matlab or Octave. It is published under the GPL v3 open-source license and constitutes the S.I. together with this text.

S.2. Basics of the branch-and-bound algorithm

The following paragraphs explain the basic elements of the branch-and-bound algorithm for globally optimal deterministic multi-objective optimization.

S.2.1. Branching

By means of branching, one can enumerate all feasible layouts in an iterative and efficient manner. As before, consider that the decision variables are given as x_j. The length of the vector, n_j, corresponds to the maximal number of installed sensors. Finding optimal sensor layouts thus represents a combinatorial optimization problem. The complete set of sensor layouts consists of 2^{n_j} layouts. Enumeration of all sensor layouts is executed as follows. First, consider the first decision variable, x_1. Consider that it has the value 0, leading to the creation of a subset of 2^{n_j-1} sensor layouts. Now consider that this decision variable has the value 1, leading to a complementary subset also consisting of 2^{n_j-1}. The original set of feasible solutions is thus split into two non-overlapping sets of sensor layouts. This process is called branching and is depicted graphically in Fig. S.1. Quite logically, one can now continue branching by considering the second decision variable.

Each of the earlier sets, can be split into two non-overlapping sets containing 2^{n_j-2} sensor layouts. Within each of the four subsets, the first two decision variables are constant. At every step of the branching algorithm, each set which has not be branched from yet is called a leaf set or leaf. Other sets, which have been branched into subsets already, are called branches. The complete structure of branches and leaves is called the solution tree or tree. The original complete solution set at the top of the tree is called the root set or root. Without further modifications, the branching process will continue to branch until each leaf set contains one sensor layout only. Consequently, one enumerates all solutions and the computational time required to find the optimal solutions increases exponentially with the number of decision variables. The following two processes, bounding and fathoming, are aimed at reducing this computational complexity.

S.2.2. Bounding

For each newly generated leaf, one computes lower and upper bounds to the objective functions. These are defined as follows (for minimization problems as studied here):

- An upper bound to an objective function is a value for this objective function which can be attained by at least one solution within the considered set (leaf).

- A lower bound to an objective function is a value for this objective function which is guaranteed to be equal to or lower than all values for this objective function for all solutions within the considered set (leaf).
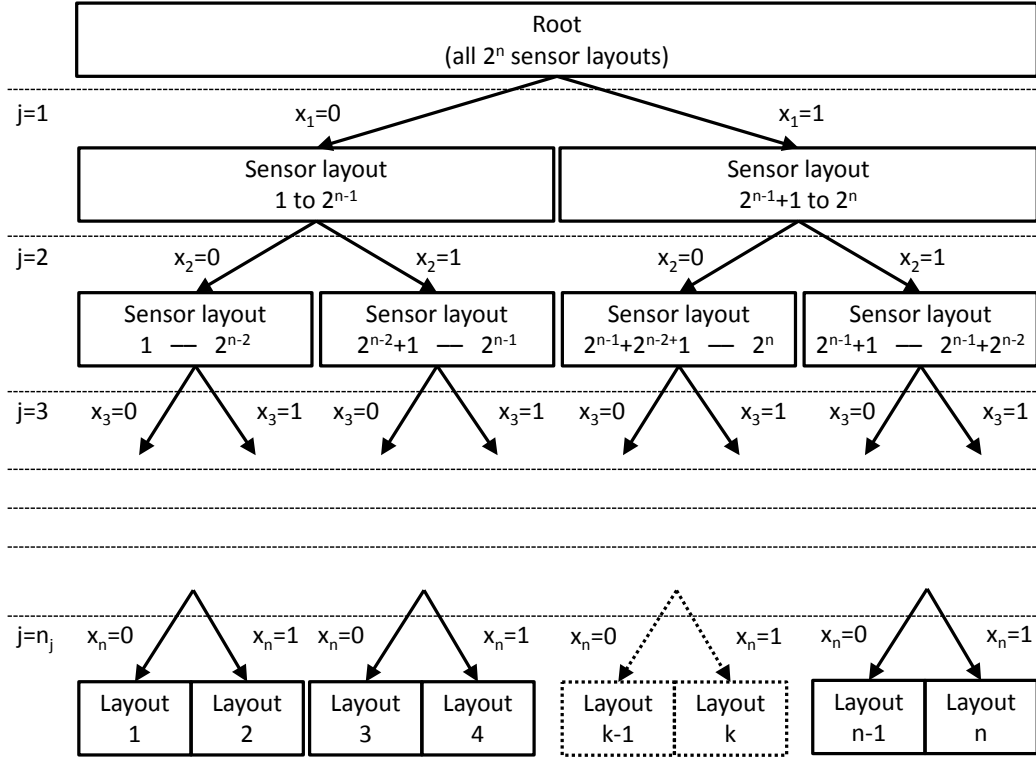
Figure S.1: Graphical representation of the branching procedure. At the top one finds the root set including all sensor layouts. Every solution set at level $j-1$ is split into sets without $(x_j = 0)$ and with $(x_j = 1)$ a sensor placed in flow j.

For multi-objective optimization, the definition of the upper bound needs to be modified as follows:

- The upper bounds to a set of competing objective functions is a set of values for these objective functions which can be simultaneously attained by at least one solution within the considered set (leaf).

The lower bounds for a multi-objective optimization remain the same, i.e., simultaneous attainment of the lower bound values is not necessary. The

computed bounds used in this study are explained in the main text.

S.2.3. Fathoming

At any branching step, consider two leaf sets $\mathcal{A}$ and $\mathcal{B}$. If it holds that all upper bounds computed for set $\mathcal{A}$ are lower than the lower bounds computed for set $\mathcal{B}$, then set $\mathcal{B}$ cannot contain any Pareto-optimal solution. Indeed, all solutions within set $\mathcal{B}$ are guaranteed to be dominated by at least one solution in the set $\mathcal{A}$. Practically, this means that further exploration of the branches stemming from set $\mathcal{B}$ can be halted. Set $\mathcal{B}$ is said to be *fathomed* and is also called a *dead leaf*. Leaf sets are not fathomed are called *live leafs*. Logically, the fathoming process can lead to substantial reductions in required computational time.

S.3. Additional results for WWTP1.

Table S.1: WWTP1. Overview of the Pareto front.

Pareto point	# sensors	# obs.	# red.	# layouts	layouts
1	0	0	0	1	1
2	1	2	0	2	$2-3$
3	2	4	0	10	$4-13$
4	3	7	0	24	$14-37$
5	2	2	2	1	38
6	3	4	3	4	$39-42$
7	4	7	4	5	$43-47$
8	5	7	5	15	$48-62$
9	6	7	6	7	$63-69$
10	7	7	7	1	70

Table S.2: WWTP1. List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow						
				1	2	3	4	5	6	7
1	0	0	0	0	0	0	0	0	0	0
2	1	2	0	0	0	1	0	0	0	0
3	1	2	0	0	1	0	0	0	0	0
4	2	4	0	0	0	0	1	1	0	0
5	2	4	0	0	0	1	0	0	1	0
6	2	4	0	0	0	1	0	1	0	0
7	2	4	0	0	0	1	1	0	0	0
8	2	4	0	0	1	0	0	0	1	0
9	2	4	0	0	1	0	0	1	0	0
10	2	4	0	0	1	0	1	0	0	0
11	2	4	0	1	0	0	0	0	1	0
12	2	4	0	1	0	1	0	0	0	0
13	2	4	0	1	1	0	0	0	0	0
14	3	7	0	0	0	0	1	0	1	1
15	3	7	0	0	0	0	1	1	0	1
16	3	7	0	0	0	0	1	1	1	0
17	3	7	0	0	0	1	0	0	1	1
18	3	7	0	0	0	1	0	1	0	1
19	3	7	0	0	0	1	0	1	1	0
20	3	7	0	0	0	1	1	0	0	1
21	3	7	0	0	0	1	1	0	1	0
22	3	7	0	0	1	0	0	0	1	1
23	3	7	0	0	1	0	0	1	0	1
24	3	7	0	0	1	0	0	1	1	0
25	3	7	0	0	1	0	1	0	0	1
26	3	7	0	0	1	0	1	0	1	0
27	3	7	0	1	0	0	0	0	1	1
28	3	7	0	1	0	0	0	1	0	1
29	3	7	0	1	0	0	0	1	1	0
30	3	7	0	1	0	0	1	0	1	0
31	3	7	0	1	0	0	1	1	0	0
32	3	7	0	1	0	1	0	0	0	1

Continued on next page

WWTP1. List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow						
				1	2	3	4	5	6	7
33	3	7	0	1	0	1	0	1	0	0
34	3	7	0	1	0	1	1	0	0	0
35	3	7	0	1	1	0	0	0	0	1
36	3	7	0	1	1	0	0	1	0	0
37	3	7	0	1	1	0	1	0	0	0
38	2	2	2	0	1	1	0	0	0	0
39	3	4	3	0	0	1	1	1	0	0
40	3	4	3	0	1	0	1	1	0	0
41	3	4	3	1	0	1	0	0	1	0
42	3	4	3	1	1	0	0	0	1	0
43	4	7	4	0	0	1	1	0	1	1
44	4	7	4	0	1	0	1	0	1	1
45	4	7	4	1	0	0	1	1	1	0
46	4	7	4	1	0	1	0	1	0	1
47	4	7	4	1	1	0	0	1	0	1
48	5	7	5	0	0	1	1	1	1	1
49	5	7	5	0	1	0	1	1	1	1
50	5	7	5	0	1	1	0	1	1	1
51	5	7	5	0	1	1	1	0	1	1
52	5	7	5	1	0	0	1	1	1	1
53	5	7	5	1	0	1	0	1	1	1
54	5	7	5	1	0	1	1	0	1	1
55	5	7	5	1	0	1	1	1	0	1
56	5	7	5	1	0	1	1	1	1	0
57	5	7	5	1	1	0	0	1	1	1
58	5	7	5	1	1	0	1	0	1	1
59	5	7	5	1	1	0	1	1	0	1
60	5	7	5	1	1	0	1	1	1	0
61	5	7	5	1	1	1	0	1	0	1
62	5	7	5	1	1	1	1	0	0	1
63	6	7	6	0	1	1	1	1	1	1
64	6	7	6	1	0	1	1	1	1	1
65	6	7	6	1	1	0	1	1	1	1
Continued on next page										

WWTP1. List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow						
				1	2	3	4	5	6	7
66	6	7	6	1	1	1	0	1	1	1
67	6	7	6	1	1	1	1	0	1	1
68	6	7	6	1	1	1	1	1	0	1
69	6	7	6	1	1	1	1	1	1	0
70	7	7	7	1	1	1	1	1	1	1

In Fig. S.2, the progress of the branch-and-bound algorithm is shown by indicating the live leaf nodes as grey bars at every iteration. With each iteration of the algorithm (bottom to top of the figure), live leaf nodes are split into new boxes of equal size. Until the 70th branching step, none of the resulting leaf nodes can be fathomed. The first fathoming, i.e. deletion of branches from the solution tree, occurs at the 70th branching step. This is visualized by not showing the deleted set, thus creating whitespace in the figure. At this stage of the algorithm, none of the live leaf nodes contain more than two solutions. As such, the performance of the branch-and-bound algorithm remains relatively close to a complete enumeration in this case.
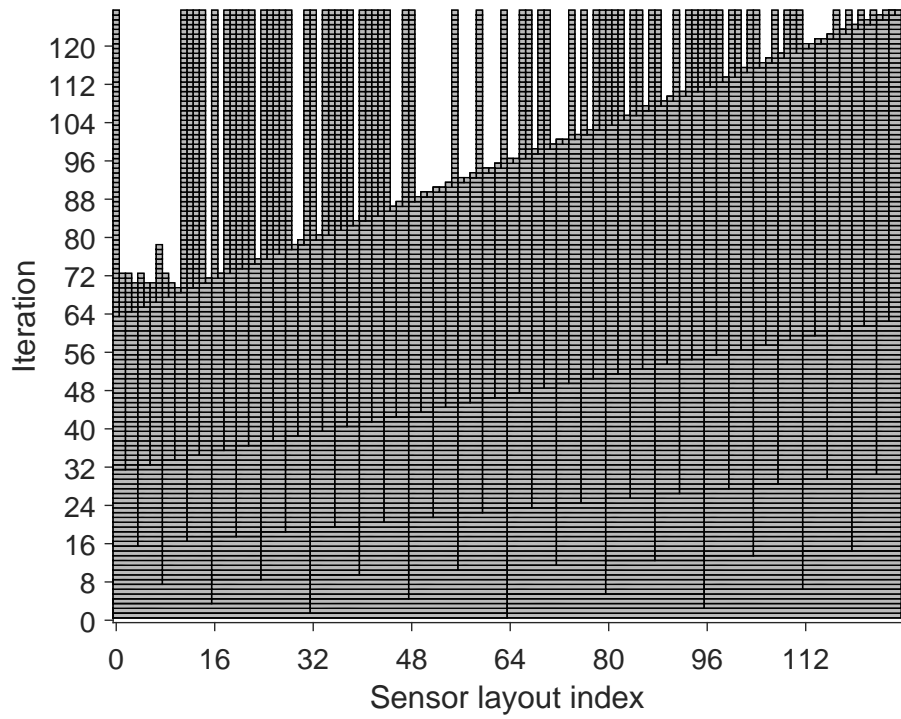
Figure S.2: WWTP1. Visualization of the branch-and-bound algorithm. All live leaf nodes are indicated by means of gray boxes spanning the layouts included within the corresponding sets. Fathomed sets appear as whitespace in the graph. The first fathoming of a set occurs at the 70$^{\text{th}}$ branching step.

S.4. Additional results for WWTP2 (MLE).

Table S.3: WWTP2 (LME). Overview of the Pareto front.

Pareto point	# sensors	# obs.	# red.	# layouts	layouts
1	0	0	0	1	1
2	1	1	0	11	$2-12$
3	2	3	0	21	$13-33$
4	3	6	0	16	$34-49$
5	4	8	0	125	$50-174$
6	5	11	0	209	$175-383$
7	3	3	3	7	$384-390$
8	4	6	4	3	$391-393$
9	5	8	5	8	$394-401$
10	6	11	6	7	$402-408$
11	7	11	7	57	$409-465$
12	8	11	8	86	$466-551$
13	9	11	9	46	$552-597$
14	10	11	10	11	$598-608$
15	11	11	11	1	609

Table S.4: WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1	1	0	0	0	0	0	0	0	0	0	0	0	1
3	1	1	0	0	0	0	0	0	0	0	0	0	1	0
4	1	1	0	0	0	0	0	0	0	0	0	1	0	0
5	1	1	0	0	0	0	0	0	0	0	1	0	0	0
6	1	1	0	0	0	0	0	0	0	1	0	0	0	0
7	1	1	0	0	0	0	0	0	1	0	0	0	0	0
8	1	1	0	0	0	0	0	1	0	0	0	0	0	0
9	1	1	0	0	0	0	1	0	0	0	0	0	0	0
10	1	1	0	0	0	1	0	0	0	0	0	0	0	0
11	1	1	0	0	1	0	0	0	0	0	0	0	0	0
12	1	1	0	1	0	0	0	0	0	0	0	0	0	0
13	2	3	0	0	0	0	0	0	0	0	0	1	1	0
14	2	3	0	0	0	0	0	0	0	1	0	0	1	0
15	2	3	0	0	0	0	0	0	0	1	0	1	0	0
16	2	3	0	0	0	0	0	0	1	1	0	0	0	0
17	2	3	0	0	0	0	0	1	0	0	0	0	0	1
18	2	3	0	0	0	0	0	1	0	0	1	0	0	0
19	2	3	0	0	0	0	0	1	0	1	0	0	0	0
20	2	3	0	0	0	0	0	1	1	0	0	0	0	0
21	2	3	0	0	0	0	1	0	0	0	0	0	0	1
22	2	3	0	0	0	0	1	0	0	0	1	0	0	0
23	2	3	0	0	0	0	1	1	0	0	0	0	0	0
24	2	3	0	0	0	1	0	0	0	0	0	0	0	1
25	2	3	0	0	0	1	0	0	0	0	1	0	0	0
26	2	3	0	0	0	1	1	0	0	0	0	0	0	0
27	2	3	0	0	1	0	0	0	0	0	0	0	0	1
28	2	3	0	0	1	0	0	0	0	0	0	0	1	0
29	2	3	0	0	1	0	0	0	0	0	1	0	0	0
30	2	3	0	0	1	0	0	1	0	0	0	0	0	0

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S.11

WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
31	2	3	0	0	1	1	0	0	0	0	0	0	0	0
32	2	3	0	1	0	0	0	0	0	0	0	0	1	0
33	2	3	0	1	1	0	0	0	0	0	0	0	0	0
34	3	6	0	0	0	0	0	1	0	0	1	0	0	1
35	3	6	0	0	0	0	1	0	0	0	1	0	0	1
36	3	6	0	0	0	0	1	1	0	0	1	0	0	0
37	3	6	0	0	0	1	0	0	0	0	1	0	0	1
38	3	6	0	0	0	1	0	1	0	0	0	0	0	1
39	3	6	0	0	0	1	0	1	0	0	1	0	0	0
40	3	6	0	0	0	1	1	0	0	0	0	0	0	1
41	3	6	0	0	0	1	1	1	0	0	0	0	0	0
42	3	6	0	0	1	0	0	0	0	0	1	0	0	1
43	3	6	0	0	1	0	0	1	0	0	0	0	0	1
44	3	6	0	0	1	0	1	0	0	0	0	0	0	1
45	3	6	0	0	1	0	1	0	0	0	1	0	0	0
46	3	6	0	0	1	0	1	1	0	0	0	0	0	0
47	3	6	0	0	1	1	0	0	0	0	1	0	0	0
48	3	6	0	0	1	1	0	1	0	0	0	0	0	0
49	3	6	0	0	1	1	1	0	0	0	0	0	0	0
50	4	8	0	0	0	0	0	0	1	0	1	1	1	0
51	4	8	0	0	0	0	0	0	1	1	1	0	0	1
52	4	8	0	0	0	0	0	0	1	1	1	0	1	0
53	4	8	0	0	0	0	0	0	1	1	1	1	0	0
54	4	8	0	0	0	0	0	1	0	0	1	0	1	1
55	4	8	0	0	0	0	0	1	0	0	1	1	1	0
56	4	8	0	0	0	0	0	1	0	1	1	0	0	1
57	4	8	0	0	0	0	0	1	0	1	1	0	1	0
58	4	8	0	0	0	0	0	1	0	1	1	1	0	0
59	4	8	0	0	0	0	0	1	1	0	1	0	0	1
60	4	8	0	0	0	0	0	1	1	0	1	0	1	0
61	4	8	0	0	0	0	0	1	1	0	1	1	0	0
62	4	8	0	0	0	0	1	0	0	0	1	0	1	1
63	4	8	0	0	0	0	1	0	0	1	1	0	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
64	4	8	0	0	0	0	1	0	1	0	1	0	0	1
65	4	8	0	0	0	0	1	0	1	1	1	0	0	0
66	4	8	0	0	0	0	1	1	0	0	1	0	1	0
67	4	8	0	0	0	0	1	1	0	1	1	0	0	0
68	4	8	0	0	0	0	1	1	1	0	1	0	0	0
69	4	8	0	0	0	1	0	0	0	0	1	0	1	1
70	4	8	0	0	0	1	0	0	0	1	1	0	0	1
71	4	8	0	0	0	1	0	0	1	0	1	0	0	1
72	4	8	0	0	0	1	0	0	1	1	0	0	0	1
73	4	8	0	0	0	1	0	0	1	1	1	0	0	0
74	4	8	0	0	0	1	0	1	0	0	0	0	1	1
75	4	8	0	0	0	1	0	1	0	0	1	0	1	0
76	4	8	0	0	0	1	0	1	0	1	0	0	0	1
77	4	8	0	0	0	1	0	1	0	1	1	0	0	0
78	4	8	0	0	0	1	0	1	1	0	0	0	0	1
79	4	8	0	0	0	1	0	1	1	0	1	0	0	0
80	4	8	0	0	0	1	1	0	0	0	0	0	1	1
81	4	8	0	0	0	1	1	0	0	1	0	0	0	1
82	4	8	0	0	0	1	1	0	1	0	0	0	0	1
83	4	8	0	0	0	1	1	0	1	1	0	0	0	0
84	4	8	0	0	0	1	1	1	0	0	0	0	1	0
85	4	8	0	0	0	1	1	1	0	1	0	0	0	0
86	4	8	0	0	0	1	1	1	1	0	0	0	0	0
87	4	8	0	0	1	0	0	0	0	0	1	0	1	1
88	4	8	0	0	1	0	0	0	0	0	1	1	1	0
89	4	8	0	0	1	0	0	0	0	1	1	0	0	1
90	4	8	0	0	1	0	0	0	0	1	1	0	1	0
91	4	8	0	0	1	0	0	0	0	1	1	1	0	0
92	4	8	0	0	1	0	0	0	1	0	0	1	1	0
93	4	8	0	0	1	0	0	0	1	0	1	0	0	1
94	4	8	0	0	1	0	0	0	1	0	1	0	1	0
95	4	8	0	0	1	0	0	0	1	0	1	1	0	0
96	4	8	0	0	1	0	0	0	1	1	0	0	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
97	4	8	0	0	1	0	0	0	1	1	0	0	1	0
98	4	8	0	0	1	0	0	0	1	1	0	1	0	0
99	4	8	0	0	1	0	0	1	0	0	0	0	1	1
100	4	8	0	0	1	0	0	1	0	0	0	1	1	0
101	4	8	0	0	1	0	0	1	0	1	0	0	0	1
102	4	8	0	0	1	0	0	1	0	1	0	0	1	0
103	4	8	0	0	1	0	0	1	0	1	0	1	0	0
104	4	8	0	0	1	0	0	1	1	0	0	0	0	1
105	4	8	0	0	1	0	0	1	1	0	0	0	1	0
106	4	8	0	0	1	0	0	1	1	0	0	1	0	0
107	4	8	0	0	1	0	1	0	0	0	0	0	1	1
108	4	8	0	0	1	0	1	0	0	0	1	0	1	0
109	4	8	0	0	1	0	1	0	0	1	0	0	0	1
110	4	8	0	0	1	0	1	0	0	1	1	0	0	0
111	4	8	0	0	1	0	1	0	1	0	0	0	0	1
112	4	8	0	0	1	0	1	0	1	0	1	0	0	0
113	4	8	0	0	1	0	1	0	1	1	0	0	0	0
114	4	8	0	0	1	0	1	1	0	0	0	0	1	0
115	4	8	0	0	1	0	1	1	0	1	0	0	0	0
116	4	8	0	0	1	0	1	1	1	0	0	0	0	0
117	4	8	0	0	1	1	0	0	0	0	1	0	1	0
118	4	8	0	0	1	1	0	0	0	1	1	0	0	0
119	4	8	0	0	1	1	0	0	1	0	1	0	0	0
120	4	8	0	0	1	1	0	0	1	1	0	0	0	0
121	4	8	0	0	1	1	0	1	0	0	0	0	1	0
122	4	8	0	0	1	1	0	1	0	1	0	0	0	0
123	4	8	0	0	1	1	0	1	1	0	0	0	0	0
124	4	8	0	0	1	1	1	0	0	0	0	0	1	0
125	4	8	0	0	1	1	1	0	0	1	0	0	0	0
126	4	8	0	0	1	1	1	0	1	0	0	0	0	0
127	4	8	0	1	0	0	0	0	0	0	1	0	1	1
128	4	8	0	1	0	0	0	0	0	0	1	1	1	0
129	4	8	0	1	0	0	0	0	0	1	1	0	1	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
130	4	8	0	1	0	0	0	0	0	1	1	1	0	0
131	4	8	0	1	0	0	0	0	1	0	0	1	1	0
132	4	8	0	1	0	0	0	0	1	0	1	0	1	0
133	4	8	0	1	0	0	0	0	1	1	0	0	1	0
134	4	8	0	1	0	0	0	0	1	1	0	1	0	0
135	4	8	0	1	0	0	0	0	1	1	1	0	0	0
136	4	8	0	1	0	0	0	1	0	0	0	0	1	1
137	4	8	0	1	0	0	0	1	0	0	0	1	1	0
138	4	8	0	1	0	0	0	1	0	0	1	0	0	1
139	4	8	0	1	0	0	0	1	0	0	1	1	0	0
140	4	8	0	1	0	0	0	1	0	1	0	0	1	0
141	4	8	0	1	0	0	0	1	0	1	0	1	0	0
142	4	8	0	1	0	0	0	1	0	1	1	0	0	0
143	4	8	0	1	0	0	0	1	1	0	0	0	1	0
144	4	8	0	1	0	0	0	1	1	0	0	1	0	0
145	4	8	0	1	0	0	0	1	1	0	1	0	0	0
146	4	8	0	1	0	0	1	0	0	0	0	0	1	1
147	4	8	0	1	0	0	1	0	0	0	1	0	0	1
148	4	8	0	1	0	0	1	0	0	0	1	0	1	0
149	4	8	0	1	0	0	1	1	0	0	0	0	1	0
150	4	8	0	1	0	0	1	1	0	0	1	0	0	0
151	4	8	0	1	0	1	0	0	0	0	1	0	0	1
152	4	8	0	1	0	1	0	0	0	0	1	0	1	0
153	4	8	0	1	0	1	0	1	0	0	0	0	0	1
154	4	8	0	1	0	1	0	1	0	0	0	0	1	0
155	4	8	0	1	0	1	0	1	0	0	1	0	0	0
156	4	8	0	1	0	1	1	0	0	0	0	0	0	1
157	4	8	0	1	0	1	1	0	0	0	0	0	1	0
158	4	8	0	1	0	1	1	1	0	0	0	0	0	0
159	4	8	0	1	1	0	0	0	0	0	1	0	0	1
160	4	8	0	1	1	0	0	0	0	0	1	1	0	0
161	4	8	0	1	1	0	0	0	0	1	1	0	0	0
162	4	8	0	1	1	0	0	0	1	0	0	1	0	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
163	4	8	0	1	1	0	0	0	1	0	1	0	0	0
164	4	8	0	1	1	0	0	0	1	1	0	0	0	0
165	4	8	0	1	1	0	0	1	0	0	0	0	0	1
166	4	8	0	1	1	0	0	1	0	0	0	1	0	0
167	4	8	0	1	1	0	0	1	0	1	0	0	0	0
168	4	8	0	1	1	0	0	1	1	0	0	0	0	0
169	4	8	0	1	1	0	1	0	0	0	0	0	0	1
170	4	8	0	1	1	0	1	0	0	0	1	0	0	0
171	4	8	0	1	1	0	1	1	0	0	0	0	0	0
172	4	8	0	1	1	1	0	0	0	0	1	0	0	0
173	4	8	0	1	1	1	0	1	0	0	0	0	0	0
174	4	8	0	1	1	1	1	0	0	0	0	0	0	0
175	5	11	0	0	0	0	0	0	1	0	1	1	1	1
176	5	11	0	0	0	0	0	0	1	1	1	0	1	1
177	5	11	0	0	0	0	0	0	1	1	1	1	0	1
178	5	11	0	0	0	0	0	1	0	0	1	1	1	1
179	5	11	0	0	0	0	0	1	0	1	1	0	1	1
180	5	11	0	0	0	0	0	1	0	1	1	1	0	1
181	5	11	0	0	0	0	0	1	1	0	1	0	1	1
182	5	11	0	0	0	0	0	1	1	0	1	1	0	1
183	5	11	0	0	0	0	1	0	0	0	1	1	1	1
184	5	11	0	0	0	0	1	0	0	1	1	0	1	1
185	5	11	0	0	0	0	1	0	0	1	1	1	0	1
186	5	11	0	0	0	0	1	0	1	0	1	0	1	1
187	5	11	0	0	0	0	1	0	1	0	1	1	0	1
188	5	11	0	0	0	0	1	0	1	0	1	1	1	0
189	5	11	0	0	0	0	1	0	1	1	1	0	1	0
190	5	11	0	0	0	0	1	0	1	1	1	1	0	0
191	5	11	0	0	0	0	1	1	0	0	1	1	1	0
192	5	11	0	0	0	0	1	1	0	1	1	0	1	0
193	5	11	0	0	0	0	1	1	0	1	1	1	0	0
194	5	11	0	0	0	0	1	1	1	0	1	0	1	0
195	5	11	0	0	0	0	1	1	1	0	1	1	0	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
196	5	11	0	0	0	1	0	0	0	0	1	1	1	1
197	5	11	0	0	0	1	0	0	0	1	1	0	1	1
198	5	11	0	0	0	1	0	0	0	1	1	1	0	1
199	5	11	0	0	0	1	0	0	1	0	0	1	1	1
200	5	11	0	0	0	1	0	0	1	0	1	0	1	1
201	5	11	0	0	0	1	0	0	1	0	1	1	0	1
202	5	11	0	0	0	1	0	0	1	0	1	1	1	0
203	5	11	0	0	0	1	0	0	1	1	0	0	1	1
204	5	11	0	0	0	1	0	0	1	1	0	1	0	1
205	5	11	0	0	0	1	0	0	1	1	1	0	1	0
206	5	11	0	0	0	1	0	0	1	1	1	1	0	0
207	5	11	0	0	0	1	0	1	0	0	0	1	1	1
208	5	11	0	0	0	1	0	1	0	0	1	1	1	0
209	5	11	0	0	0	1	0	1	0	1	0	0	1	1
210	5	11	0	0	0	1	0	1	0	1	0	1	0	1
211	5	11	0	0	0	1	0	1	0	1	1	0	1	0
212	5	11	0	0	0	1	0	1	0	1	1	1	0	0
213	5	11	0	0	0	1	0	1	1	0	0	0	1	1
214	5	11	0	0	0	1	0	1	1	0	0	1	0	1
215	5	11	0	0	0	1	0	1	1	0	1	0	1	0
216	5	11	0	0	0	1	0	1	1	0	1	1	0	0
217	5	11	0	0	0	1	1	0	0	0	0	1	1	1
218	5	11	0	0	0	1	1	0	0	1	0	0	1	1
219	5	11	0	0	0	1	1	0	0	1	0	1	0	1
220	5	11	0	0	0	1	1	0	1	0	0	0	1	1
221	5	11	0	0	0	1	1	0	1	0	0	1	0	1
222	5	11	0	0	0	1	1	0	1	0	0	1	1	0
223	5	11	0	0	0	1	1	0	1	1	0	0	1	0
224	5	11	0	0	0	1	1	0	1	1	0	1	0	0
225	5	11	0	0	0	1	1	1	0	0	0	1	1	0
226	5	11	0	0	0	1	1	1	0	1	0	0	1	0
227	5	11	0	0	0	1	1	1	0	1	0	1	0	0
228	5	11	0	0	0	1	1	1	1	0	0	0	1	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
229	5	11	0	0	0	1	1	1	1	0	0	1	0	0
230	5	11	0	0	1	0	0	0	0	0	1	1	1	1
231	5	11	0	0	1	0	0	0	0	1	1	0	1	1
232	5	11	0	0	1	0	0	0	0	1	1	1	0	1
233	5	11	0	0	1	0	0	0	1	0	0	1	1	1
234	5	11	0	0	1	0	0	0	1	0	1	0	1	1
235	5	11	0	0	1	0	0	0	1	0	1	1	0	1
236	5	11	0	0	1	0	0	0	1	1	0	0	1	1
237	5	11	0	0	1	0	0	0	1	1	0	1	0	1
238	5	11	0	0	1	0	0	1	0	0	0	1	1	1
239	5	11	0	0	1	0	0	1	0	1	0	0	1	1
240	5	11	0	0	1	0	0	1	0	1	0	1	0	1
241	5	11	0	0	1	0	0	1	1	0	0	0	1	1
242	5	11	0	0	1	0	0	1	1	0	0	1	0	1
243	5	11	0	0	1	0	1	0	0	0	0	1	1	1
244	5	11	0	0	1	0	1	0	0	0	1	1	1	0
245	5	11	0	0	1	0	1	0	0	1	0	0	1	1
246	5	11	0	0	1	0	1	0	0	1	0	1	0	1
247	5	11	0	0	1	0	1	0	0	1	1	0	1	0
248	5	11	0	0	1	0	1	0	0	1	1	1	0	0
249	5	11	0	0	1	0	1	0	1	0	0	0	1	1
250	5	11	0	0	1	0	1	0	1	0	0	1	0	1
251	5	11	0	0	1	0	1	0	1	0	0	1	1	0
252	5	11	0	0	1	0	1	0	1	0	1	0	1	0
253	5	11	0	0	1	0	1	0	1	0	1	1	0	0
254	5	11	0	0	1	0	1	0	1	1	0	0	1	0
255	5	11	0	0	1	0	1	0	1	1	0	1	0	0
256	5	11	0	0	1	0	1	1	0	0	0	1	1	0
257	5	11	0	0	1	0	1	1	0	1	0	0	1	0
258	5	11	0	0	1	0	1	1	0	1	0	1	0	0
259	5	11	0	0	1	0	1	1	1	0	0	0	1	0
260	5	11	0	0	1	0	1	1	1	0	0	1	0	0
261	5	11	0	0	1	1	0	0	0	0	1	1	1	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
262	5	11	0	0	1	1	0	0	0	1	1	0	1	0
263	5	11	0	0	1	1	0	0	0	1	1	1	0	0
264	5	11	0	0	1	1	0	0	1	0	0	1	1	0
265	5	11	0	0	1	1	0	0	1	0	1	0	1	0
266	5	11	0	0	1	1	0	0	1	0	1	1	0	0
267	5	11	0	0	1	1	0	0	1	1	0	0	1	0
268	5	11	0	0	1	1	0	0	1	1	0	1	0	0
269	5	11	0	0	1	1	0	1	0	0	0	1	1	0
270	5	11	0	0	1	1	0	1	0	1	0	0	1	0
271	5	11	0	0	1	1	0	1	0	1	0	1	0	0
272	5	11	0	0	1	1	0	1	1	0	0	0	1	0
273	5	11	0	0	1	1	0	1	1	0	0	1	0	0
274	5	11	0	0	1	1	1	0	0	0	0	1	1	0
275	5	11	0	0	1	1	1	0	0	1	0	0	1	0
276	5	11	0	0	1	1	1	0	0	1	0	1	0	0
277	5	11	0	0	1	1	1	0	1	0	0	0	1	0
278	5	11	0	0	1	1	1	0	1	0	0	1	0	0
279	5	11	0	1	0	0	0	0	0	0	1	1	1	1
280	5	11	0	1	0	0	0	0	0	1	1	0	1	1
281	5	11	0	1	0	0	0	0	0	1	1	1	0	1
282	5	11	0	1	0	0	0	0	1	0	0	1	1	1
283	5	11	0	1	0	0	0	0	1	0	1	0	1	1
284	5	11	0	1	0	0	0	0	1	1	0	0	1	1
285	5	11	0	1	0	0	0	0	1	1	0	1	0	1
286	5	11	0	1	0	0	0	0	1	1	1	0	0	1
287	5	11	0	1	0	0	0	1	0	0	0	1	1	1
288	5	11	0	1	0	0	0	1	0	0	1	1	0	1
289	5	11	0	1	0	0	0	1	0	1	0	0	1	1
290	5	11	0	1	0	0	0	1	0	1	0	1	0	1
291	5	11	0	1	0	0	0	1	0	1	1	0	0	1
292	5	11	0	1	0	0	0	1	1	0	0	0	1	1
293	5	11	0	1	0	0	0	1	1	0	0	1	0	1
294	5	11	0	1	0	0	0	1	1	0	1	0	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
295	5	11	0	1	0	0	1	0	0	0	0	1	1	1
296	5	11	0	1	0	0	1	0	0	0	1	1	0	1
297	5	11	0	1	0	0	1	0	0	0	1	1	1	0
298	5	11	0	1	0	0	1	0	0	1	0	0	1	1
299	5	11	0	1	0	0	1	0	0	1	0	1	0	1
300	5	11	0	1	0	0	1	0	0	1	1	0	0	1
301	5	11	0	1	0	0	1	0	0	1	1	0	1	0
302	5	11	0	1	0	0	1	0	0	1	1	1	0	0
303	5	11	0	1	0	0	1	0	1	0	0	0	1	1
304	5	11	0	1	0	0	1	0	1	0	0	1	0	1
305	5	11	0	1	0	0	1	0	1	0	0	1	1	0
306	5	11	0	1	0	0	1	0	1	0	1	0	0	1
307	5	11	0	1	0	0	1	0	1	0	1	0	1	0
308	5	11	0	1	0	0	1	0	1	1	0	0	1	0
309	5	11	0	1	0	0	1	0	1	1	0	1	0	0
310	5	11	0	1	0	0	1	0	1	1	1	0	0	0
311	5	11	0	1	0	0	1	1	0	0	0	1	1	0
312	5	11	0	1	0	0	1	1	0	0	1	1	0	0
313	5	11	0	1	0	0	1	1	0	1	0	0	1	0
314	5	11	0	1	0	0	1	1	0	1	0	1	0	0
315	5	11	0	1	0	0	1	1	0	1	1	0	0	0
316	5	11	0	1	0	0	1	1	1	0	0	0	1	0
317	5	11	0	1	0	0	1	1	1	0	0	1	0	0
318	5	11	0	1	0	0	1	1	1	0	1	0	0	0
319	5	11	0	1	0	1	0	0	0	0	1	1	0	1
320	5	11	0	1	0	1	0	0	0	0	1	1	1	0
321	5	11	0	1	0	1	0	0	0	1	1	0	0	1
322	5	11	0	1	0	1	0	0	0	1	1	0	1	0
323	5	11	0	1	0	1	0	0	0	1	1	1	0	0
324	5	11	0	1	0	1	0	0	1	0	0	1	0	1
325	5	11	0	1	0	1	0	0	1	0	0	1	1	0
326	5	11	0	1	0	1	0	0	1	0	1	0	0	1
327	5	11	0	1	0	1	0	0	1	0	1	0	1	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
328	5	11	0	1	0	1	0	0	1	1	0	0	0	1
329	5	11	0	1	0	1	0	0	1	1	0	0	1	0
330	5	11	0	1	0	1	0	0	1	1	0	1	0	0
331	5	11	0	1	0	1	0	0	1	1	1	0	0	0
332	5	11	0	1	0	1	0	1	0	0	0	1	0	1
333	5	11	0	1	0	1	0	1	0	0	0	1	1	0
334	5	11	0	1	0	1	0	1	0	0	1	1	0	0
335	5	11	0	1	0	1	0	1	0	1	0	0	0	1
336	5	11	0	1	0	1	0	1	0	1	0	0	1	0
337	5	11	0	1	0	1	0	1	0	1	0	1	0	0
338	5	11	0	1	0	1	0	1	0	1	1	0	0	0
339	5	11	0	1	0	1	0	1	1	0	0	0	0	1
340	5	11	0	1	0	1	0	1	1	0	0	0	1	0
341	5	11	0	1	0	1	0	1	1	0	0	1	0	0
342	5	11	0	1	0	1	0	1	1	0	1	0	0	0
343	5	11	0	1	0	1	1	0	0	0	0	1	0	1
344	5	11	0	1	0	1	1	0	0	0	0	1	1	0
345	5	11	0	1	0	1	1	0	0	1	0	0	0	1
346	5	11	0	1	0	1	1	0	0	1	0	0	1	0
347	5	11	0	1	0	1	1	0	0	1	0	1	0	0
348	5	11	0	1	0	1	1	0	1	0	0	0	0	1
349	5	11	0	1	0	1	1	0	1	0	0	0	1	0
350	5	11	0	1	0	1	1	0	1	1	0	0	0	0
351	5	11	0	1	0	1	1	1	0	0	0	1	0	0
352	5	11	0	1	0	1	1	1	0	1	0	0	0	0
353	5	11	0	1	0	1	1	1	1	0	0	0	0	0
354	5	11	0	1	1	0	0	0	0	0	1	1	0	1
355	5	11	0	1	1	0	0	0	0	1	1	0	0	1
356	5	11	0	1	1	0	0	0	1	0	0	1	0	1
357	5	11	0	1	1	0	0	0	1	0	1	0	0	1
358	5	11	0	1	1	0	0	0	1	1	0	0	0	1
359	5	11	0	1	1	0	0	1	0	0	0	1	0	1
360	5	11	0	1	1	0	0	1	0	1	0	0	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
361	5	11	0	1	1	0	0	1	1	0	0	0	0	1
362	5	11	0	1	1	0	1	0	0	0	0	1	0	1
363	5	11	0	1	1	0	1	0	0	0	1	1	0	0
364	5	11	0	1	1	0	1	0	0	1	0	0	0	1
365	5	11	0	1	1	0	1	0	0	1	1	0	0	0
366	5	11	0	1	1	0	1	0	1	0	0	0	0	1
367	5	11	0	1	1	0	1	0	1	0	0	1	0	0
368	5	11	0	1	1	0	1	0	1	0	1	0	0	0
369	5	11	0	1	1	0	1	0	1	1	0	0	0	0
370	5	11	0	1	1	0	1	1	0	0	0	1	0	0
371	5	11	0	1	1	0	1	1	0	1	0	0	0	0
372	5	11	0	1	1	0	1	1	1	0	0	0	0	0
373	5	11	0	1	1	1	0	0	0	0	1	1	0	0
374	5	11	0	1	1	1	0	0	0	1	1	0	0	0
375	5	11	0	1	1	1	0	0	1	0	0	1	0	0
376	5	11	0	1	1	1	0	0	1	0	1	0	0	0
377	5	11	0	1	1	1	0	0	1	1	0	0	0	0
378	5	11	0	1	1	1	0	1	0	0	0	1	0	0
379	5	11	0	1	1	1	0	1	0	1	0	0	0	0
380	5	11	0	1	1	1	0	1	1	0	0	0	0	0
381	5	11	0	1	1	1	1	0	0	0	0	1	0	0
382	5	11	0	1	1	1	1	0	0	1	0	0	0	0
383	5	11	0	1	1	1	1	0	1	0	0	0	0	0
384	3	3	3	0	0	0	0	0	0	1	0	1	1	0
385	3	3	3	0	0	0	0	1	1	1	0	0	0	0
386	3	3	3	0	0	0	1	1	0	0	0	0	0	1
387	3	3	3	0	0	1	1	0	0	0	1	0	0	0
388	3	3	3	0	1	0	0	1	0	0	1	0	0	0
389	3	3	3	0	1	1	0	0	0	0	0	0	0	1
390	3	3	3	1	1	0	0	0	0	0	0	0	1	0
391	4	6	4	0	0	1	0	1	0	0	1	0	0	1
392	4	6	4	0	1	0	1	0	0	0	1	0	0	1
393	4	6	4	0	1	1	1	1	0	0	0	0	0	0

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
394	5	8	5	0	0	1	0	0	1	1	1	0	0	1
395	5	8	5	0	1	0	0	0	1	0	1	1	1	0
396	5	8	5	0	1	1	1	0	1	1	0	0	0	0
397	5	8	5	1	0	0	0	0	1	1	1	0	1	0
398	5	8	5	1	0	0	0	1	0	1	1	1	0	0
399	5	8	5	1	0	0	1	0	0	0	1	0	1	1
400	5	8	5	1	0	1	1	1	0	0	0	0	1	0
401	5	8	5	1	1	0	0	1	1	0	0	1	0	0
402	6	11	6	0	0	1	0	0	1	0	1	1	1	1
403	6	11	6	0	1	1	1	0	1	0	0	1	1	0
404	6	11	6	1	0	0	1	0	0	1	1	1	0	1
405	6	11	6	1	0	1	0	1	1	0	0	1	0	1
406	6	11	6	1	0	1	1	0	1	1	0	0	1	0
407	6	11	6	1	0	1	1	1	0	1	0	1	0	0
408	6	11	6	1	1	0	1	0	1	0	0	1	0	1
409	7	11	7	0	0	1	0	0	1	1	1	1	1	1
410	7	11	7	0	0	1	0	1	0	1	1	1	1	1
411	7	11	7	0	0	1	0	1	1	0	1	1	1	1
412	7	11	7	0	0	1	1	0	1	0	1	1	1	1
413	7	11	7	0	0	1	1	1	1	0	1	1	1	0
414	7	11	7	0	1	0	1	0	0	1	1	1	1	1
415	7	11	7	0	1	0	1	0	1	0	1	1	1	1
416	7	11	7	0	1	1	0	0	1	0	1	1	1	1
417	7	11	7	0	1	1	0	1	1	0	0	1	1	1
418	7	11	7	0	1	1	1	0	1	0	0	1	1	1
419	7	11	7	0	1	1	1	0	1	0	1	1	1	0
420	7	11	7	0	1	1	1	0	1	1	0	1	1	0
421	7	11	7	0	1	1	1	1	0	1	0	1	1	0
422	7	11	7	0	1	1	1	1	1	0	0	1	1	0
423	7	11	7	1	0	0	1	0	0	1	1	1	1	1
424	7	11	7	1	0	0	1	0	1	0	1	1	1	1
425	7	11	7	1	0	0	1	0	1	1	1	0	1	1
426	7	11	7	1	0	0	1	0	1	1	1	1	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
427	7	11	7	1	0	0	1	1	0	1	1	1	0	1
428	7	11	7	1	0	0	1	1	1	0	1	1	0	1
429	7	11	7	1	0	1	0	0	1	0	1	1	1	1
430	7	11	7	1	0	1	0	0	1	1	1	0	1	1
431	7	11	7	1	0	1	0	0	1	1	1	1	0	1
432	7	11	7	1	0	1	0	1	0	1	1	1	0	1
433	7	11	7	1	0	1	0	1	1	0	0	1	1	1
434	7	11	7	1	0	1	0	1	1	0	1	1	0	1
435	7	11	7	1	0	1	0	1	1	1	0	0	1	1
436	7	11	7	1	0	1	0	1	1	1	0	1	0	1
437	7	11	7	1	0	1	1	0	0	1	1	1	0	1
438	7	11	7	1	0	1	1	0	1	0	0	1	1	1
439	7	11	7	1	0	1	1	0	1	1	0	0	1	1
440	7	11	7	1	0	1	1	0	1	1	0	1	0	1
441	7	11	7	1	0	1	1	0	1	1	0	1	1	0
442	7	11	7	1	0	1	1	0	1	1	1	0	1	0
443	7	11	7	1	0	1	1	1	0	1	0	1	0	1
444	7	11	7	1	0	1	1	1	0	1	0	1	1	0
445	7	11	7	1	0	1	1	1	0	1	1	1	0	0
446	7	11	7	1	0	1	1	1	1	0	0	1	0	1
447	7	11	7	1	0	1	1	1	1	0	0	1	1	0
448	7	11	7	1	0	1	1	1	1	1	0	0	1	0
449	7	11	7	1	0	1	1	1	1	1	0	1	0	0
450	7	11	7	1	1	0	1	0	0	1	1	1	0	1
451	7	11	7	1	1	0	1	0	1	0	0	1	1	1
452	7	11	7	1	1	0	1	0	1	0	1	1	0	1
453	7	11	7	1	1	0	1	0	1	1	0	0	1	1
454	7	11	7	1	1	0	1	0	1	1	0	1	0	1
455	7	11	7	1	1	0	1	1	0	1	0	1	0	1
456	7	11	7	1	1	0	1	1	1	0	0	1	0	1
457	7	11	7	1	1	1	0	0	1	0	1	1	0	1
458	7	11	7	1	1	1	0	1	1	0	0	1	0	1
459	7	11	7	1	1	1	1	0	0	1	1	1	0	0

WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
460	7	11	7	1	1	1	1	0	1	0	0	1	0	1
461	7	11	7	1	1	1	1	0	1	0	0	1	1	0
462	7	11	7	1	1	1	1	0	1	1	0	0	1	0
463	7	11	7	1	1	1	1	0	1	1	0	1	0	0
464	7	11	7	1	1	1	1	1	0	1	0	1	0	0
465	7	11	7	1	1	1	1	1	1	0	0	1	0	0
466	8	11	8	0	0	1	0	1	1	1	1	1	1	1
467	8	11	8	0	0	1	1	0	1	1	1	1	1	1
468	8	11	8	0	0	1	1	1	0	1	1	1	1	1
469	8	11	8	0	0	1	1	1	1	0	1	1	1	1
470	8	11	8	0	0	1	1	1	1	1	1	1	1	0
471	8	11	8	0	1	0	1	0	1	1	1	1	1	1
472	8	11	8	0	1	0	1	1	0	1	1	1	1	1
473	8	11	8	0	1	0	1	1	1	0	1	1	1	1
474	8	11	8	0	1	1	0	0	1	1	1	1	1	1
475	8	11	8	0	1	1	0	1	0	1	1	1	1	1
476	8	11	8	0	1	1	0	1	1	0	1	1	1	1
477	8	11	8	0	1	1	0	1	1	1	0	1	1	1
478	8	11	8	0	1	1	1	0	0	1	1	1	1	1
479	8	11	8	0	1	1	1	0	1	0	1	1	1	1
480	8	11	8	0	1	1	1	0	1	1	0	1	1	1
481	8	11	8	0	1	1	1	0	1	1	1	1	1	0
482	8	11	8	0	1	1	1	1	0	1	0	1	1	1
483	8	11	8	0	1	1	1	1	0	1	1	1	1	0
484	8	11	8	0	1	1	1	1	1	0	0	1	1	1
485	8	11	8	0	1	1	1	1	1	0	1	1	1	0
486	8	11	8	0	1	1	1	1	1	1	0	1	1	0
487	8	11	8	1	0	0	1	0	1	1	1	1	1	1
488	8	11	8	1	0	0	1	1	0	1	1	1	1	1
489	8	11	8	1	0	0	1	1	1	0	1	1	1	1
490	8	11	8	1	0	0	1	1	1	1	1	0	1	1
491	8	11	8	1	0	0	1	1	1	1	1	1	0	1
492	8	11	8	1	0	1	0	0	1	1	1	1	1	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
493	8	11	8	1	0	1	0	1	0	1	1	1	1	1
494	8	11	8	1	0	1	0	1	1	0	1	1	1	1
495	8	11	8	1	0	1	0	1	1	1	0	1	1	1
496	8	11	8	1	0	1	0	1	1	1	1	0	1	1
497	8	11	8	1	0	1	0	1	1	1	1	1	0	1
498	8	11	8	1	0	1	1	0	0	1	1	1	1	1
499	8	11	8	1	0	1	1	0	1	0	1	1	1	1
500	8	11	8	1	0	1	1	0	1	1	0	1	1	1
501	8	11	8	1	0	1	1	0	1	1	1	0	1	1
502	8	11	8	1	0	1	1	0	1	1	1	1	0	1
503	8	11	8	1	0	1	1	0	1	1	1	1	1	0
504	8	11	8	1	0	1	1	1	0	1	0	1	1	1
505	8	11	8	1	0	1	1	1	0	1	1	1	0	1
506	8	11	8	1	0	1	1	1	0	1	1	1	1	0
507	8	11	8	1	0	1	1	1	1	0	0	1	1	1
508	8	11	8	1	0	1	1	1	1	0	1	1	0	1
509	8	11	8	1	0	1	1	1	1	0	1	1	1	0
510	8	11	8	1	0	1	1	1	1	1	0	0	1	1
511	8	11	8	1	0	1	1	1	1	1	0	1	0	1
512	8	11	8	1	0	1	1	1	1	1	0	1	1	0
513	8	11	8	1	0	1	1	1	1	1	1	0	1	0
514	8	11	8	1	0	1	1	1	1	1	1	1	0	0
515	8	11	8	1	1	0	1	0	0	1	1	1	1	1
516	8	11	8	1	1	0	1	0	1	0	1	1	1	1
517	8	11	8	1	1	0	1	0	1	1	0	1	1	1
518	8	11	8	1	1	0	1	0	1	1	1	0	1	1
519	8	11	8	1	1	0	1	0	1	1	1	1	0	1
520	8	11	8	1	1	0	1	1	0	1	0	1	1	1
521	8	11	8	1	1	0	1	1	0	1	1	1	0	1
522	8	11	8	1	1	0	1	1	1	0	0	1	1	1
523	8	11	8	1	1	0	1	1	1	0	1	1	0	1
524	8	11	8	1	1	0	1	1	1	1	0	0	1	1
525	8	11	8	1	1	0	1	1	1	1	0	1	0	1
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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
526	8	11	8	1	1	1	0	0	1	0	1	1	1	1
527	8	11	8	1	1	1	0	0	1	1	1	0	1	1
528	8	11	8	1	1	1	0	0	1	1	1	1	0	1
529	8	11	8	1	1	1	0	1	0	1	1	1	0	1
530	8	11	8	1	1	1	0	1	1	0	0	1	1	1
531	8	11	8	1	1	1	0	1	1	0	1	1	0	1
532	8	11	8	1	1	1	0	1	1	1	0	0	1	1
533	8	11	8	1	1	1	0	1	1	1	0	1	0	1
534	8	11	8	1	1	1	1	0	0	1	1	1	0	1
535	8	11	8	1	1	1	1	0	0	1	1	1	1	0
536	8	11	8	1	1	1	1	0	1	0	0	1	1	1
537	8	11	8	1	1	1	1	0	1	0	1	1	0	1
538	8	11	8	1	1	1	1	0	1	0	1	1	1	0
539	8	11	8	1	1	1	1	0	1	1	0	0	1	1
540	8	11	8	1	1	1	1	0	1	1	0	1	0	1
541	8	11	8	1	1	1	1	0	1	1	0	1	1	0
542	8	11	8	1	1	1	1	0	1	1	1	0	1	0
543	8	11	8	1	1	1	1	0	1	1	1	1	0	0
544	8	11	8	1	1	1	1	1	0	1	0	1	0	1
545	8	11	8	1	1	1	1	1	0	1	0	1	1	0
546	8	11	8	1	1	1	1	1	0	1	1	1	0	0
547	8	11	8	1	1	1	1	1	1	0	0	1	0	1
548	8	11	8	1	1	1	1	1	1	0	0	1	1	0
549	8	11	8	1	1	1	1	1	1	0	1	1	0	0
550	8	11	8	1	1	1	1	1	1	1	0	0	1	0
551	8	11	8	1	1	1	1	1	1	1	0	1	0	0
552	9	11	9	0	0	1	1	1	1	1	1	1	1	1
553	9	11	9	0	1	0	1	1	1	1	1	1	1	1
554	9	11	9	0	1	1	0	1	1	1	1	1	1	1
555	9	11	9	0	1	1	1	0	1	1	1	1	1	1
556	9	11	9	0	1	1	1	1	0	1	1	1	1	1
557	9	11	9	0	1	1	1	1	1	0	1	1	1	1
558	9	11	9	0	1	1	1	1	1	1	0	1	1	1
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S.27

WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
559	9	11	9	0	1	1	1	1	1	1	1	1	1	0
560	9	11	9	1	0	0	1	1	1	1	1	1	1	1
561	9	11	9	1	0	1	0	1	1	1	1	1	1	1
562	9	11	9	1	0	1	1	0	1	1	1	1	1	1
563	9	11	9	1	0	1	1	1	0	1	1	1	1	1
564	9	11	9	1	0	1	1	1	1	0	1	1	1	1
565	9	11	9	1	0	1	1	1	1	1	0	1	1	1
566	9	11	9	1	0	1	1	1	1	1	1	0	1	1
567	9	11	9	1	0	1	1	1	1	1	1	1	0	1
568	9	11	9	1	0	1	1	1	1	1	1	1	1	0
569	9	11	9	1	1	0	1	0	1	1	1	1	1	1
570	9	11	9	1	1	0	1	1	0	1	1	1	1	1
571	9	11	9	1	1	0	1	1	1	0	1	1	1	1
572	9	11	9	1	1	0	1	1	1	1	0	1	1	1
573	9	11	9	1	1	0	1	1	1	1	1	0	1	1
574	9	11	9	1	1	0	1	1	1	1	1	1	0	1
575	9	11	9	1	1	1	0	0	1	1	1	1	1	1
576	9	11	9	1	1	1	0	1	0	1	1	1	1	1
577	9	11	9	1	1	1	0	1	1	0	1	1	1	1
578	9	11	9	1	1	1	0	1	1	1	0	1	1	1
579	9	11	9	1	1	1	0	1	1	1	1	0	1	1
580	9	11	9	1	1	1	0	1	1	1	1	1	0	1
581	9	11	9	1	1	1	1	0	0	1	1	1	1	1
582	9	11	9	1	1	1	1	0	1	0	1	1	1	1
583	9	11	9	1	1	1	1	0	1	1	0	1	1	1
584	9	11	9	1	1	1	1	0	1	1	1	0	1	1
585	9	11	9	1	1	1	1	0	1	1	1	1	0	1
586	9	11	9	1	1	1	1	0	1	1	1	1	1	0
587	9	11	9	1	1	1	1	1	0	1	0	1	1	1
588	9	11	9	1	1	1	1	1	0	1	1	1	0	1
589	9	11	9	1	1	1	1	1	0	1	1	1	1	0
590	9	11	9	1	1	1	1	1	1	0	0	1	1	1
591	9	11	9	1	1	1	1	1	1	0	1	1	0	1

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WWTP2 (LME). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow										
				1	2	3	4	5	6	7	8	9	10	11
592	9	11	9	1	1	1	1	1	1	0	1	1	1	0
593	9	11	9	1	1	1	1	1	1	1	0	0	1	1
594	9	11	9	1	1	1	1	1	1	1	0	1	0	1
595	9	11	9	1	1	1	1	1	1	1	0	1	1	0
596	9	11	9	1	1	1	1	1	1	1	1	0	1	0
597	9	11	9	1	1	1	1	1	1	1	1	1	0	0
598	10	11	10	0	1	1	1	1	1	1	1	1	1	1
599	10	11	10	1	0	1	1	1	1	1	1	1	1	1
600	10	11	10	1	1	0	1	1	1	1	1	1	1	1
601	10	11	10	1	1	1	0	1	1	1	1	1	1	1
602	10	11	10	1	1	1	1	0	1	1	1	1	1	1
603	10	11	10	1	1	1	1	1	0	1	1	1	1	1
604	10	11	10	1	1	1	1	1	1	0	1	1	1	1
605	10	11	10	1	1	1	1	1	1	1	0	1	1	1
606	10	11	10	1	1	1	1	1	1	1	1	0	1	1
607	10	11	10	1	1	1	1	1	1	1	1	1	0	1
608	10	11	10	1	1	1	1	1	1	1	1	1	1	0
609	11	11	11	1	1	1	1	1	1	1	1	1	1	1

The Pareto front shown in Fig. 4 was completed after 1922 iterations of the branch-and-bound algorithm. The evolution of the live leaf sets during the Pareto search is shown in Fig. S.3. As for WWTP1, fathoming only results after all live leafs contain at most two solutions. However, the algorithm effectively avoids the execution of the labeling algorithm for 125 sensor layouts (out of 2048).
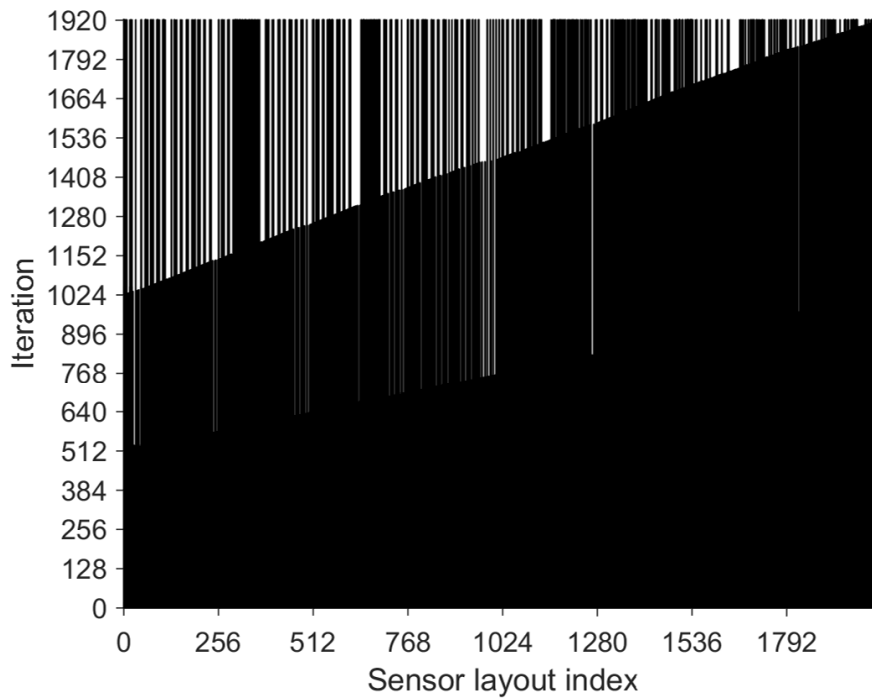
Figure S.3: WWTP2 (MLE). Visualization of the branch-and-bound algorithm. All live leaf nodes are indicated by means of boxes spanning the layouts included within the corresponding sets.

S.5. Additional results for WWTP3 (MUCT).

Table S.5: WWTP3 (MUCT). Overview of the Pareto front.

Pareto point	# sensors	# obs.	# red.	# layouts	layouts
1	0	0	0	1	1
2	1	1	0	12	2 − 13
3	2	3	0	30	14 − 43
4	3	6	0	48	44 − 91
5	4	9	0	150	92 − 241
6	5	12	0	336	242 − 577
7	3	3	3	10	578 − 587
8	4	6	4	9	588 − 596
9	5	9	5	12	597 − 608
10	6	12	6	10	609 − 618
11	7	12	7	101	619 − 719
12	8	12	8	206	720 − 925
13	9	12	9	156	926 − 1081
14	10	12	10	60	1082 − 1141
15	11	12	11	12	1142 − 1153
16	12	12	12	1	1154

Table S.6: WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2	1	1	0	0	0	0	0	0	0	0	0	0	0	0	1
3	1	1	0	0	0	0	0	0	0	0	0	0	0	1	0
4	1	1	0	0	0	0	0	0	0	0	0	0	1	0	0
5	1	1	0	0	0	0	0	0	0	0	0	1	0	0	0
6	1	1	0	0	0	0	0	0	0	0	1	0	0	0	0
7	1	1	0	0	0	0	0	0	0	1	0	0	0	0	0
8	1	1	0	0	0	0	0	0	1	0	0	0	0	0	0
9	1	1	0	0	0	0	0	1	0	0	0	0	0	0	0
10	1	1	0	0	0	0	1	0	0	0	0	0	0	0	0
11	1	1	0	0	0	1	0	0	0	0	0	0	0	0	0
12	1	1	0	0	1	0	0	0	0	0	0	0	0	0	0
13	1	1	0	1	0	0	0	0	0	0	0	0	0	0	0
14	2	3	0	0	0	0	0	0	0	0	0	1	1	0	0
15	2	3	0	0	0	0	0	0	0	0	1	0	1	0	0
16	2	3	0	0	0	0	0	0	0	0	1	1	0	0	0
17	2	3	0	0	0	0	0	0	0	1	0	1	0	0	0
18	2	3	0	0	0	0	0	0	0	1	1	0	0	0	0
19	2	3	0	0	0	0	0	0	1	0	0	0	0	0	1
20	2	3	0	0	0	0	0	0	1	0	0	0	0	1	0
21	2	3	0	0	0	0	0	0	1	0	0	0	1	0	0
22	2	3	0	0	0	0	0	0	1	0	1	0	0	0	0
23	2	3	0	0	0	0	0	0	1	1	0	0	0	0	0
24	2	3	0	0	0	0	0	1	0	0	0	0	0	0	1
25	2	3	0	0	0	0	0	1	0	0	0	0	0	1	0
26	2	3	0	0	0	0	0	1	1	0	0	0	0	0	0
27	2	3	0	0	0	0	1	0	0	0	0	0	0	0	1
28	2	3	0	0	0	0	1	0	0	0	0	0	0	1	0
29	2	3	0	0	0	0	1	1	0	0	0	0	0	0	0
30	2	3	0	0	0	1	0	0	0	0	0	0	0	0	1
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S.32

WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
31	2	3	0	0	0	1	0	0	0	0	0	0	0	1	0
32	2	3	0	0	0	1	0	0	0	0	0	0	1	0	0
33	2	3	0	0	0	1	0	0	1	0	0	0	0	0	0
34	2	3	0	0	0	1	1	0	0	0	0	0	0	0	0
35	2	3	0	0	1	0	0	0	0	0	0	0	0	0	1
36	2	3	0	0	1	0	0	0	0	0	0	0	1	0	0
37	2	3	0	0	1	1	0	0	0	0	0	0	0	0	0
38	2	3	0	1	0	0	0	0	0	0	0	0	0	0	1
39	2	3	0	1	0	0	0	0	0	0	0	0	1	0	0
40	2	3	0	1	0	0	0	0	0	0	0	1	0	0	0
41	2	3	0	1	0	0	0	0	0	1	0	0	0	0	0
42	2	3	0	1	0	0	0	0	1	0	0	0	0	0	0
43	2	3	0	1	1	0	0	0	0	0	0	0	0	0	0
44	3	6	0	0	0	0	0	0	0	1	0	1	1	0	0
45	3	6	0	0	0	0	0	0	0	1	1	0	1	0	0
46	3	6	0	0	0	0	0	0	0	1	1	1	0	0	0
47	3	6	0	0	0	0	0	0	1	0	0	0	0	1	1
48	3	6	0	0	0	0	0	0	1	0	0	0	1	0	1
49	3	6	0	0	0	0	0	0	1	0	0	1	1	0	0
50	3	6	0	0	0	0	0	0	1	0	1	0	1	0	0
51	3	6	0	0	0	0	0	0	1	0	1	1	0	0	0
52	3	6	0	0	0	0	0	0	1	1	0	0	1	0	0
53	3	6	0	0	0	0	0	0	1	1	0	1	0	0	0
54	3	6	0	0	0	0	0	1	0	0	0	0	0	1	1
55	3	6	0	0	0	0	0	1	1	0	0	0	0	0	1
56	3	6	0	0	0	0	1	0	0	0	0	0	0	1	1
57	3	6	0	0	0	0	1	0	1	0	0	0	0	0	1
58	3	6	0	0	0	0	1	0	1	0	0	0	0	1	0
59	3	6	0	0	0	0	1	1	0	0	0	0	0	1	0
60	3	6	0	0	0	0	1	1	1	0	0	0	0	0	0
61	3	6	0	0	0	1	0	0	0	0	0	0	0	1	1
62	3	6	0	0	0	1	0	0	0	0	0	0	1	0	1
63	3	6	0	0	0	1	0	0	1	0	0	0	0	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
64	3	6	0	0	0	1	0	0	1	0	0	0	1	0	0
65	3	6	0	0	0	1	0	1	0	0	0	0	0	0	1
66	3	6	0	0	0	1	0	1	0	0	0	0	0	1	0
67	3	6	0	0	0	1	0	1	1	0	0	0	0	0	0
68	3	6	0	0	0	1	1	0	0	0	0	0	0	0	1
69	3	6	0	0	0	1	1	0	1	0	0	0	0	0	0
70	3	6	0	0	0	1	1	1	0	0	0	0	0	0	0
71	3	6	0	0	1	0	0	0	0	0	0	0	1	0	1
72	3	6	0	0	1	0	0	0	1	0	0	0	0	0	1
73	3	6	0	0	1	0	0	0	1	0	0	0	1	0	0
74	3	6	0	0	1	1	0	0	0	0	0	0	0	0	1
75	3	6	0	0	1	1	0	0	1	0	0	0	0	0	0
76	3	6	0	1	0	0	0	0	0	0	0	0	1	0	1
77	3	6	0	1	0	0	0	0	0	0	0	1	1	0	0
78	3	6	0	1	0	0	0	0	0	0	1	0	1	0	0
79	3	6	0	1	0	0	0	0	0	0	1	1	0	0	0
80	3	6	0	1	0	0	0	0	0	1	0	0	1	0	0
81	3	6	0	1	0	0	0	0	0	1	1	0	0	0	0
82	3	6	0	1	0	0	0	0	1	0	0	0	0	0	1
83	3	6	0	1	0	0	0	0	1	0	0	1	0	0	0
84	3	6	0	1	0	0	0	0	1	0	1	0	0	0	0
85	3	6	0	1	0	0	0	0	1	1	0	0	0	0	0
86	3	6	0	1	0	1	0	0	0	0	0	0	0	0	1
87	3	6	0	1	0	1	0	0	0	0	0	0	1	0	0
88	3	6	0	1	0	1	0	0	1	0	0	0	0	0	0
89	3	6	0	1	1	0	0	0	0	0	0	0	1	0	0
90	3	6	0	1	1	0	0	0	1	0	0	0	0	0	0
91	3	6	0	1	1	1	0	0	0	0	0	0	0	0	0
92	4	9	0	0	0	0	0	0	0	1	0	1	1	0	1
93	4	9	0	0	0	0	0	0	0	1	1	0	1	0	1
94	4	9	0	0	0	0	0	0	0	1	1	1	0	0	1
95	4	9	0	0	0	0	0	0	1	0	0	0	1	1	1
96	4	9	0	0	0	0	0	0	1	0	0	1	1	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
97	4	9	0	0	0	0	0	0	1	0	1	0	1	0	1
98	4	9	0	0	0	0	0	0	1	0	1	1	0	0	1
99	4	9	0	0	0	0	0	0	1	1	0	0	1	0	1
100	4	9	0	0	0	0	0	0	1	1	0	1	0	0	1
101	4	9	0	0	0	0	0	1	0	0	0	0	1	1	1
102	4	9	0	0	0	0	0	1	1	0	0	0	1	0	1
103	4	9	0	0	0	0	1	0	0	0	0	0	1	1	1
104	4	9	0	0	0	0	1	0	1	0	0	0	1	0	1
105	4	9	0	0	0	0	1	0	1	0	0	0	1	1	0
106	4	9	0	0	0	0	1	1	0	0	0	0	1	1	0
107	4	9	0	0	0	0	1	1	1	0	0	0	1	0	0
108	4	9	0	0	0	1	0	0	0	0	0	0	1	1	1
109	4	9	0	0	0	1	0	0	0	0	0	1	1	0	1
110	4	9	0	0	0	1	0	0	0	0	1	0	1	0	1
111	4	9	0	0	0	1	0	0	0	0	1	1	0	0	1
112	4	9	0	0	0	1	0	0	0	1	0	0	1	0	1
113	4	9	0	0	0	1	0	0	0	1	0	1	0	0	1
114	4	9	0	0	0	1	0	0	0	1	0	1	1	0	0
115	4	9	0	0	0	1	0	0	0	1	1	0	1	0	0
116	4	9	0	0	0	1	0	0	0	1	1	1	0	0	0
117	4	9	0	0	0	1	0	0	1	0	0	0	1	1	0
118	4	9	0	0	0	1	0	0	1	0	0	1	1	0	0
119	4	9	0	0	0	1	0	0	1	0	1	0	1	0	0
120	4	9	0	0	0	1	0	0	1	0	1	1	0	0	0
121	4	9	0	0	0	1	0	0	1	1	0	0	1	0	0
122	4	9	0	0	0	1	0	0	1	1	0	1	0	0	0
123	4	9	0	0	0	1	0	1	0	0	0	0	1	0	1
124	4	9	0	0	0	1	0	1	0	0	0	0	1	1	0
125	4	9	0	0	0	1	0	1	1	0	0	0	1	0	0
126	4	9	0	0	0	1	1	0	0	0	0	0	1	0	1
127	4	9	0	0	0	1	1	0	1	0	0	0	1	0	0
128	4	9	0	0	0	1	1	1	0	0	0	0	1	0	0
129	4	9	0	0	1	0	0	0	0	0	0	0	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
130	4	9	0	0	1	0	0	0	0	0	0	1	1	0	1
131	4	9	0	0	1	0	0	0	0	0	1	0	1	0	1
132	4	9	0	0	1	0	0	0	0	0	1	1	0	0	1
133	4	9	0	0	1	0	0	0	0	1	0	0	1	0	1
134	4	9	0	0	1	0	0	0	0	1	0	1	1	0	0
135	4	9	0	0	1	0	0	0	0	1	1	0	0	0	1
136	4	9	0	0	1	0	0	0	0	1	1	0	1	0	0
137	4	9	0	0	1	0	0	0	0	1	1	1	0	0	0
138	4	9	0	0	1	0	0	0	1	0	0	0	0	1	1
139	4	9	0	0	1	0	0	0	1	0	0	0	1	1	0
140	4	9	0	0	1	0	0	0	1	0	0	1	0	0	1
141	4	9	0	0	1	0	0	0	1	0	0	1	1	0	0
142	4	9	0	0	1	0	0	0	1	0	1	0	0	0	1
143	4	9	0	0	1	0	0	0	1	0	1	0	1	0	0
144	4	9	0	0	1	0	0	0	1	0	1	1	0	0	0
145	4	9	0	0	1	0	0	0	1	1	0	0	0	0	1
146	4	9	0	0	1	0	0	0	1	1	0	0	1	0	0
147	4	9	0	0	1	0	0	0	1	1	0	1	0	0	0
148	4	9	0	0	1	0	0	1	0	0	0	0	0	1	1
149	4	9	0	0	1	0	0	1	0	0	0	0	1	0	1
150	4	9	0	0	1	0	0	1	0	0	0	0	1	1	0
151	4	9	0	0	1	0	0	1	1	0	0	0	0	0	1
152	4	9	0	0	1	0	0	1	1	0	0	0	1	0	0
153	4	9	0	0	1	0	1	0	0	0	0	0	0	1	1
154	4	9	0	0	1	0	1	0	0	0	0	0	1	0	1
155	4	9	0	0	1	0	1	0	1	0	0	0	0	0	1
156	4	9	0	0	1	0	1	0	1	0	0	0	0	1	0
157	4	9	0	0	1	0	1	0	1	0	0	0	1	0	0
158	4	9	0	0	1	0	1	1	0	0	0	0	0	1	0
159	4	9	0	0	1	0	1	1	0	0	0	0	1	0	0
160	4	9	0	0	1	0	1	1	1	0	0	0	0	0	0
161	4	9	0	0	1	1	0	0	0	0	0	0	0	1	1
162	4	9	0	0	1	1	0	0	0	0	0	1	0	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
163	4	9	0	0	1	1	0	0	0	0	1	0	0	0	1
164	4	9	0	0	1	1	0	0	0	1	0	0	0	0	1
165	4	9	0	0	1	1	0	0	0	1	0	1	0	0	0
166	4	9	0	0	1	1	0	0	0	1	1	0	0	0	0
167	4	9	0	0	1	1	0	0	1	0	0	0	0	1	0
168	4	9	0	0	1	1	0	0	1	0	0	1	0	0	0
169	4	9	0	0	1	1	0	0	1	0	1	0	0	0	0
170	4	9	0	0	1	1	0	0	1	1	0	0	0	0	0
171	4	9	0	0	1	1	0	1	0	0	0	0	0	0	1
172	4	9	0	0	1	1	0	1	0	0	0	0	0	1	0
173	4	9	0	0	1	1	0	1	1	0	0	0	0	0	0
174	4	9	0	0	1	1	1	0	0	0	0	0	0	0	1
175	4	9	0	0	1	1	1	0	1	0	0	0	0	0	0
176	4	9	0	0	1	1	1	1	0	0	0	0	0	0	0
177	4	9	0	1	0	0	0	0	0	0	0	0	1	1	1
178	4	9	0	1	0	0	0	0	0	0	0	1	1	0	1
179	4	9	0	1	0	0	0	0	0	0	1	0	1	0	1
180	4	9	0	1	0	0	0	0	0	0	1	1	0	0	1
181	4	9	0	1	0	0	0	0	0	1	0	0	1	0	1
182	4	9	0	1	0	0	0	0	0	1	1	0	0	0	1
183	4	9	0	1	0	0	0	0	1	0	0	0	0	1	1
184	4	9	0	1	0	0	0	0	1	0	0	1	0	0	1
185	4	9	0	1	0	0	0	0	1	0	1	0	0	0	1
186	4	9	0	1	0	0	0	0	1	1	0	0	0	0	1
187	4	9	0	1	0	0	0	1	0	0	0	0	0	1	1
188	4	9	0	1	0	0	0	1	0	0	0	0	1	0	1
189	4	9	0	1	0	0	0	1	1	0	0	0	0	0	1
190	4	9	0	1	0	0	1	0	0	0	0	0	0	1	1
191	4	9	0	1	0	0	1	0	0	0	0	0	1	0	1
192	4	9	0	1	0	0	1	0	0	0	0	0	1	1	0
193	4	9	0	1	0	0	1	0	1	0	0	0	0	0	1
194	4	9	0	1	0	0	1	0	1	0	0	0	0	1	0
195	4	9	0	1	0	0	1	1	0	0	0	0	0	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
196	4	9	0	1	0	0	1	1	0	0	0	0	1	0	0
197	4	9	0	1	0	0	1	1	1	0	0	0	0	0	0
198	4	9	0	1	0	1	0	0	0	0	0	0	0	1	1
199	4	9	0	1	0	1	0	0	0	0	0	0	1	1	0
200	4	9	0	1	0	1	0	0	0	0	0	1	0	0	1
201	4	9	0	1	0	1	0	0	0	0	0	1	1	0	0
202	4	9	0	1	0	1	0	0	0	0	1	0	0	0	1
203	4	9	0	1	0	1	0	0	0	0	1	0	1	0	0
204	4	9	0	1	0	1	0	0	0	0	1	1	0	0	0
205	4	9	0	1	0	1	0	0	0	1	0	0	0	0	1
206	4	9	0	1	0	1	0	0	0	1	0	0	1	0	0
207	4	9	0	1	0	1	0	0	0	1	1	0	0	0	0
208	4	9	0	1	0	1	0	0	1	0	0	0	0	1	0
209	4	9	0	1	0	1	0	0	1	0	0	1	0	0	0
210	4	9	0	1	0	1	0	0	1	0	1	0	0	0	0
211	4	9	0	1	0	1	0	0	1	1	0	0	0	0	0
212	4	9	0	1	0	1	0	1	0	0	0	0	0	0	1
213	4	9	0	1	0	1	0	1	0	0	0	0	0	1	0
214	4	9	0	1	0	1	0	1	0	0	0	0	1	0	0
215	4	9	0	1	0	1	0	1	1	0	0	0	0	0	0
216	4	9	0	1	0	1	1	0	0	0	0	0	0	0	1
217	4	9	0	1	0	1	1	0	0	0	0	0	1	0	0
218	4	9	0	1	0	1	1	0	1	0	0	0	0	0	0
219	4	9	0	1	0	1	1	1	0	0	0	0	0	0	0
220	4	9	0	1	1	0	0	0	0	0	0	0	1	1	0
221	4	9	0	1	1	0	0	0	0	0	0	1	1	0	0
222	4	9	0	1	1	0	0	0	0	0	1	0	1	0	0
223	4	9	0	1	1	0	0	0	0	0	1	1	0	0	0
224	4	9	0	1	1	0	0	0	0	1	0	0	1	0	0
225	4	9	0	1	1	0	0	0	0	1	1	0	0	0	0
226	4	9	0	1	1	0	0	0	1	0	0	0	0	1	0
227	4	9	0	1	1	0	0	0	1	0	0	1	0	0	0
228	4	9	0	1	1	0	0	0	1	0	1	0	0	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
229	4	9	0	1	1	0	0	0	1	1	0	0	0	0	0
230	4	9	0	1	1	0	0	1	0	0	0	0	0	1	0
231	4	9	0	1	1	0	0	1	0	0	0	0	1	0	0
232	4	9	0	1	1	0	0	1	1	0	0	0	0	0	0
233	4	9	0	1	1	0	1	0	0	0	0	0	0	1	0
234	4	9	0	1	1	0	1	0	0	0	0	0	1	0	0
235	4	9	0	1	1	0	1	0	1	0	0	0	0	0	0
236	4	9	0	1	1	1	0	0	0	0	0	0	0	1	0
237	4	9	0	1	1	1	0	0	0	0	0	1	0	0	0
238	4	9	0	1	1	1	0	0	0	0	1	0	0	0	0
239	4	9	0	1	1	1	0	0	0	1	0	0	0	0	0
240	4	9	0	1	1	1	0	1	0	0	0	0	0	0	0
241	4	9	0	1	1	1	1	0	0	0	0	0	0	0	0
242	5	12	0	0	0	0	0	0	0	1	0	1	1	1	1
243	5	12	0	0	0	0	0	0	0	1	1	0	1	1	1
244	5	12	0	0	0	0	0	0	0	1	1	1	0	1	1
245	5	12	0	0	0	0	0	0	1	0	0	1	1	1	1
246	5	12	0	0	0	0	0	0	1	0	1	0	1	1	1
247	5	12	0	0	0	0	0	0	1	0	1	1	0	1	1
248	5	12	0	0	0	0	0	0	1	1	0	0	1	1	1
249	5	12	0	0	0	0	0	0	1	1	0	1	0	1	1
250	5	12	0	0	0	0	0	1	0	0	0	1	1	1	1
251	5	12	0	0	0	0	0	1	0	0	1	0	1	1	1
252	5	12	0	0	0	0	0	1	0	0	1	1	0	1	1
253	5	12	0	0	0	0	0	1	0	1	0	0	1	1	1
254	5	12	0	0	0	0	0	1	0	1	0	1	0	1	1
255	5	12	0	0	0	0	0	1	0	1	0	1	1	0	1
256	5	12	0	0	0	0	0	1	0	1	1	0	1	0	1
257	5	12	0	0	0	0	0	1	0	1	1	1	0	0	1
258	5	12	0	0	0	0	0	1	1	0	0	1	1	0	1
259	5	12	0	0	0	0	0	1	1	0	1	0	1	0	1
260	5	12	0	0	0	0	0	1	1	0	1	1	0	0	1
261	5	12	0	0	0	0	0	1	1	1	0	0	1	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
262	5	12	0	0	0	0	0	1	1	1	0	1	0	0	1
263	5	12	0	0	0	0	1	0	0	0	0	1	1	1	1
264	5	12	0	0	0	0	1	0	0	0	1	0	1	1	1
265	5	12	0	0	0	0	1	0	0	0	1	1	0	1	1
266	5	12	0	0	0	0	1	0	0	1	0	0	1	1	1
267	5	12	0	0	0	0	1	0	0	1	0	1	0	1	1
268	5	12	0	0	0	0	1	0	0	1	0	1	1	0	1
269	5	12	0	0	0	0	1	0	0	1	0	1	1	1	0
270	5	12	0	0	0	0	1	0	0	1	1	0	1	0	1
271	5	12	0	0	0	0	1	0	0	1	1	0	1	1	0
272	5	12	0	0	0	0	1	0	0	1	1	1	0	0	1
273	5	12	0	0	0	0	1	0	0	1	1	1	0	1	0
274	5	12	0	0	0	0	1	0	1	0	0	1	1	0	1
275	5	12	0	0	0	0	1	0	1	0	0	1	1	1	0
276	5	12	0	0	0	0	1	0	1	0	1	0	1	0	1
277	5	12	0	0	0	0	1	0	1	0	1	0	1	1	0
278	5	12	0	0	0	0	1	0	1	0	1	1	0	0	1
279	5	12	0	0	0	0	1	0	1	0	1	1	0	1	0
280	5	12	0	0	0	0	1	0	1	1	0	0	1	0	1
281	5	12	0	0	0	0	1	0	1	1	0	0	1	1	0
282	5	12	0	0	0	0	1	0	1	1	0	1	0	0	1
283	5	12	0	0	0	0	1	0	1	1	0	1	0	1	0
284	5	12	0	0	0	0	1	1	0	0	0	1	1	1	0
285	5	12	0	0	0	0	1	1	0	0	1	0	1	1	0
286	5	12	0	0	0	0	1	1	0	0	1	1	0	1	0
287	5	12	0	0	0	0	1	1	0	1	0	0	1	1	0
288	5	12	0	0	0	0	1	1	0	1	0	1	0	1	0
289	5	12	0	0	0	0	1	1	0	1	0	1	1	0	0
290	5	12	0	0	0	0	1	1	0	1	1	0	1	0	0
291	5	12	0	0	0	0	1	1	0	1	1	1	0	0	0
292	5	12	0	0	0	0	1	1	1	0	0	1	1	0	0
293	5	12	0	0	0	0	1	1	1	0	1	0	1	0	0
294	5	12	0	0	0	0	1	1	1	0	1	1	0	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
295	5	12	0	0	0	0	1	1	1	1	0	0	1	0	0
296	5	12	0	0	0	0	1	1	1	1	0	1	0	0	0
297	5	12	0	0	0	1	0	0	0	0	0	1	1	1	1
298	5	12	0	0	0	1	0	0	0	0	1	0	1	1	1
299	5	12	0	0	0	1	0	0	0	0	1	1	0	1	1
300	5	12	0	0	0	1	0	0	0	1	0	0	1	1	1
301	5	12	0	0	0	1	0	0	0	1	0	1	0	1	1
302	5	12	0	0	0	1	0	0	0	1	0	1	1	1	0
303	5	12	0	0	0	1	0	0	0	1	1	0	1	1	0
304	5	12	0	0	0	1	0	0	0	1	1	1	0	1	0
305	5	12	0	0	0	1	0	0	1	0	0	1	1	1	0
306	5	12	0	0	0	1	0	0	1	0	1	0	1	1	0
307	5	12	0	0	0	1	0	0	1	0	1	1	0	1	0
308	5	12	0	0	0	1	0	0	1	1	0	0	1	1	0
309	5	12	0	0	0	1	0	0	1	1	0	1	0	1	0
310	5	12	0	0	0	1	0	1	0	0	0	1	1	0	1
311	5	12	0	0	0	1	0	1	0	0	0	1	1	1	0
312	5	12	0	0	0	1	0	1	0	0	1	0	1	0	1
313	5	12	0	0	0	1	0	1	0	0	1	0	1	1	0
314	5	12	0	0	0	1	0	1	0	0	1	1	0	0	1
315	5	12	0	0	0	1	0	1	0	0	1	1	0	1	0
316	5	12	0	0	0	1	0	1	0	1	0	0	1	0	1
317	5	12	0	0	0	1	0	1	0	1	0	0	1	1	0
318	5	12	0	0	0	1	0	1	0	1	0	1	0	0	1
319	5	12	0	0	0	1	0	1	0	1	0	1	0	1	0
320	5	12	0	0	0	1	0	1	0	1	0	1	1	0	0
321	5	12	0	0	0	1	0	1	0	1	1	0	1	0	0
322	5	12	0	0	0	1	0	1	0	1	1	1	0	0	0
323	5	12	0	0	0	1	0	1	1	0	0	1	1	0	0
324	5	12	0	0	0	1	0	1	1	0	1	0	1	0	0
325	5	12	0	0	0	1	0	1	1	0	1	1	0	0	0
326	5	12	0	0	0	1	0	1	1	1	0	0	1	0	0
327	5	12	0	0	0	1	0	1	1	1	0	1	0	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
328	5	12	0	0	0	1	1	0	0	0	0	1	1	0	1
329	5	12	0	0	0	1	1	0	0	0	1	0	1	0	1
330	5	12	0	0	0	1	1	0	0	0	1	1	0	0	1
331	5	12	0	0	0	1	1	0	0	1	0	0	1	0	1
332	5	12	0	0	0	1	1	0	0	1	0	1	0	0	1
333	5	12	0	0	0	1	1	0	0	1	0	1	1	0	0
334	5	12	0	0	0	1	1	0	0	1	1	0	1	0	0
335	5	12	0	0	0	1	1	0	0	1	1	1	0	0	0
336	5	12	0	0	0	1	1	0	1	0	0	1	1	0	0
337	5	12	0	0	0	1	1	0	1	0	1	0	1	0	0
338	5	12	0	0	0	1	1	0	1	0	1	1	0	0	0
339	5	12	0	0	0	1	1	0	1	1	0	0	1	0	0
340	5	12	0	0	0	1	1	0	1	1	0	1	0	0	0
341	5	12	0	0	0	1	1	1	0	0	0	1	1	0	0
342	5	12	0	0	0	1	1	1	0	0	1	0	1	0	0
343	5	12	0	0	0	1	1	1	0	0	1	1	0	0	0
344	5	12	0	0	0	1	1	1	0	1	0	0	1	0	0
345	5	12	0	0	0	1	1	1	0	1	0	1	0	0	0
346	5	12	0	0	1	0	0	0	0	0	0	1	1	1	1
347	5	12	0	0	1	0	0	0	0	0	1	0	1	1	1
348	5	12	0	0	1	0	0	0	0	0	1	1	0	1	1
349	5	12	0	0	1	0	0	0	0	1	0	0	1	1	1
350	5	12	0	0	1	0	0	0	0	1	0	1	1	1	0
351	5	12	0	0	1	0	0	0	0	1	1	0	0	1	1
352	5	12	0	0	1	0	0	0	0	1	1	0	1	1	0
353	5	12	0	0	1	0	0	0	0	1	1	1	0	1	0
354	5	12	0	0	1	0	0	0	1	0	0	1	0	1	1
355	5	12	0	0	1	0	0	0	1	0	0	1	1	1	0
356	5	12	0	0	1	0	0	0	1	0	1	0	0	1	1
357	5	12	0	0	1	0	0	0	1	0	1	0	1	1	0
358	5	12	0	0	1	0	0	0	1	0	1	1	0	1	0
359	5	12	0	0	1	0	0	0	1	1	0	0	0	1	1
360	5	12	0	0	1	0	0	0	1	1	0	0	1	1	0

WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
361	5	12	0	0	1	0	0	0	1	1	0	1	0	1	0
362	5	12	0	0	1	0	0	1	0	0	0	1	0	1	1
363	5	12	0	0	1	0	0	1	0	0	0	1	1	0	1
364	5	12	0	0	1	0	0	1	0	0	0	1	1	1	0
365	5	12	0	0	1	0	0	1	0	0	1	0	0	1	1
366	5	12	0	0	1	0	0	1	0	0	1	0	1	0	1
367	5	12	0	0	1	0	0	1	0	0	1	0	1	1	0
368	5	12	0	0	1	0	0	1	0	0	1	1	0	0	1
369	5	12	0	0	1	0	0	1	0	0	1	1	0	1	0
370	5	12	0	0	1	0	0	1	0	1	0	0	0	1	1
371	5	12	0	0	1	0	0	1	0	1	0	0	1	0	1
372	5	12	0	0	1	0	0	1	0	1	0	0	1	1	0
373	5	12	0	0	1	0	0	1	0	1	0	1	0	1	0
374	5	12	0	0	1	0	0	1	0	1	0	1	1	0	0
375	5	12	0	0	1	0	0	1	0	1	1	0	0	0	1
376	5	12	0	0	1	0	0	1	0	1	1	0	1	0	0
377	5	12	0	0	1	0	0	1	0	1	1	1	0	0	0
378	5	12	0	0	1	0	0	1	1	0	0	1	0	0	1
379	5	12	0	0	1	0	0	1	1	0	0	1	1	0	0
380	5	12	0	0	1	0	0	1	1	0	1	0	0	0	1
381	5	12	0	0	1	0	0	1	1	0	1	0	1	0	0
382	5	12	0	0	1	0	0	1	1	0	1	1	0	0	0
383	5	12	0	0	1	0	0	1	1	1	0	0	0	0	1
384	5	12	0	0	1	0	0	1	1	1	0	0	1	0	0
385	5	12	0	0	1	0	0	1	1	1	0	1	0	0	0
386	5	12	0	0	1	0	1	0	0	0	0	1	0	1	1
387	5	12	0	0	1	0	1	0	0	0	0	1	1	0	1
388	5	12	0	0	1	0	1	0	0	0	1	0	0	1	1
389	5	12	0	0	1	0	1	0	0	0	1	0	1	0	1
390	5	12	0	0	1	0	1	0	0	0	1	1	0	0	1
391	5	12	0	0	1	0	1	0	0	1	0	0	0	1	1
392	5	12	0	0	1	0	1	0	0	1	0	0	1	0	1
393	5	12	0	0	1	0	1	0	0	1	0	1	0	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
394	5	12	0	0	1	0	1	0	0	1	0	1	1	0	0
395	5	12	0	0	1	0	1	0	0	1	1	0	0	0	1
396	5	12	0	0	1	0	1	0	0	1	1	0	0	1	0
397	5	12	0	0	1	0	1	0	0	1	1	0	1	0	0
398	5	12	0	0	1	0	1	0	0	1	1	1	0	0	0
399	5	12	0	0	1	0	1	0	1	0	0	1	0	0	1
400	5	12	0	0	1	0	1	0	1	0	0	1	0	1	0
401	5	12	0	0	1	0	1	0	1	0	0	1	1	0	0
402	5	12	0	0	1	0	1	0	1	0	1	0	0	0	1
403	5	12	0	0	1	0	1	0	1	0	1	0	0	1	0
404	5	12	0	0	1	0	1	0	1	0	1	0	1	0	0
405	5	12	0	0	1	0	1	0	1	0	1	1	0	0	0
406	5	12	0	0	1	0	1	0	1	1	0	0	0	0	1
407	5	12	0	0	1	0	1	0	1	1	0	0	0	1	0
408	5	12	0	0	1	0	1	0	1	1	0	0	1	0	0
409	5	12	0	0	1	0	1	0	1	1	0	1	0	0	0
410	5	12	0	0	1	0	1	1	0	0	0	1	0	1	0
411	5	12	0	0	1	0	1	1	0	0	0	1	1	0	0
412	5	12	0	0	1	0	1	1	0	0	1	0	0	1	0
413	5	12	0	0	1	0	1	1	0	0	1	0	1	0	0
414	5	12	0	0	1	0	1	1	0	0	1	1	0	0	0
415	5	12	0	0	1	0	1	1	0	1	0	0	0	1	0
416	5	12	0	0	1	0	1	1	0	1	0	0	1	0	0
417	5	12	0	0	1	0	1	1	0	1	1	0	0	0	0
418	5	12	0	0	1	0	1	1	1	0	0	1	0	0	0
419	5	12	0	0	1	0	1	1	1	0	1	0	0	0	0
420	5	12	0	0	1	0	1	1	1	1	0	0	0	0	0
421	5	12	0	0	1	1	0	0	0	0	0	1	0	1	1
422	5	12	0	0	1	1	0	0	0	0	1	0	0	1	1
423	5	12	0	0	1	1	0	0	0	1	0	0	0	1	1
424	5	12	0	0	1	1	0	0	0	1	0	1	0	1	0
425	5	12	0	0	1	1	0	0	0	1	1	0	0	1	0
426	5	12	0	0	1	1	0	0	1	0	0	1	0	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
427	5	12	0	0	1	1	0	0	1	0	1	0	0	1	0
428	5	12	0	0	1	1	0	0	1	1	0	0	0	1	0
429	5	12	0	0	1	1	0	1	0	0	0	1	0	0	1
430	5	12	0	0	1	1	0	1	0	0	0	1	0	1	0
431	5	12	0	0	1	1	0	1	0	0	1	0	0	0	1
432	5	12	0	0	1	1	0	1	0	0	1	0	0	1	0
433	5	12	0	0	1	1	0	1	0	1	0	0	0	0	1
434	5	12	0	0	1	1	0	1	0	1	0	0	0	1	0
435	5	12	0	0	1	1	0	1	0	1	0	1	0	0	0
436	5	12	0	0	1	1	0	1	0	1	1	0	0	0	0
437	5	12	0	0	1	1	0	1	1	0	0	1	0	0	0
438	5	12	0	0	1	1	0	1	1	0	1	0	0	0	0
439	5	12	0	0	1	1	0	1	1	1	0	0	0	0	0
440	5	12	0	0	1	1	1	0	0	0	0	1	0	0	1
441	5	12	0	0	1	1	1	0	0	0	1	0	0	0	1
442	5	12	0	0	1	1	1	0	0	1	0	0	0	0	1
443	5	12	0	0	1	1	1	0	0	1	0	1	0	0	0
444	5	12	0	0	1	1	1	0	0	1	1	0	0	0	0
445	5	12	0	0	1	1	1	0	1	0	0	1	0	0	0
446	5	12	0	0	1	1	1	0	1	0	1	0	0	0	0
447	5	12	0	0	1	1	1	0	1	1	0	0	0	0	0
448	5	12	0	0	1	1	1	1	0	0	0	1	0	0	0
449	5	12	0	0	1	1	1	1	0	0	1	0	0	0	0
450	5	12	0	0	1	1	1	1	0	1	0	0	0	0	0
451	5	12	0	1	0	0	0	0	0	0	0	1	1	1	1
452	5	12	0	1	0	0	0	0	0	0	1	0	1	1	1
453	5	12	0	1	0	0	0	0	0	0	1	1	0	1	1
454	5	12	0	1	0	0	0	0	0	1	0	0	1	1	1
455	5	12	0	1	0	0	0	0	0	1	1	0	0	1	1
456	5	12	0	1	0	0	0	0	1	0	0	1	0	1	1
457	5	12	0	1	0	0	0	0	1	0	1	0	0	1	1
458	5	12	0	1	0	0	0	0	1	1	0	0	0	1	1
459	5	12	0	1	0	0	0	1	0	0	0	1	0	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
460	5	12	0	1	0	0	0	1	0	0	0	1	1	0	1
461	5	12	0	1	0	0	0	1	0	0	1	0	0	1	1
462	5	12	0	1	0	0	0	1	0	0	1	0	1	0	1
463	5	12	0	1	0	0	0	1	0	0	1	1	0	0	1
464	5	12	0	1	0	0	0	1	0	1	0	0	0	1	1
465	5	12	0	1	0	0	0	1	0	1	0	0	1	0	1
466	5	12	0	1	0	0	0	1	0	1	1	0	0	0	1
467	5	12	0	1	0	0	0	1	1	0	0	1	0	0	1
468	5	12	0	1	0	0	0	1	1	0	1	0	0	0	1
469	5	12	0	1	0	0	0	1	1	1	0	0	0	0	1
470	5	12	0	1	0	0	1	0	0	0	0	1	0	1	1
471	5	12	0	1	0	0	1	0	0	0	0	1	1	0	1
472	5	12	0	1	0	0	1	0	0	0	0	1	1	1	0
473	5	12	0	1	0	0	1	0	0	0	1	0	0	1	1
474	5	12	0	1	0	0	1	0	0	0	1	0	1	0	1
475	5	12	0	1	0	0	1	0	0	0	1	0	1	1	0
476	5	12	0	1	0	0	1	0	0	0	1	1	0	0	1
477	5	12	0	1	0	0	1	0	0	0	1	1	0	1	0
478	5	12	0	1	0	0	1	0	0	1	0	0	0	1	1
479	5	12	0	1	0	0	1	0	0	1	0	0	1	0	1
480	5	12	0	1	0	0	1	0	0	1	0	0	1	1	0
481	5	12	0	1	0	0	1	0	0	1	1	0	0	0	1
482	5	12	0	1	0	0	1	0	0	1	1	0	0	1	0
483	5	12	0	1	0	0	1	0	1	0	0	1	0	0	1
484	5	12	0	1	0	0	1	0	1	0	0	1	0	1	0
485	5	12	0	1	0	0	1	0	1	0	1	0	0	0	1
486	5	12	0	1	0	0	1	0	1	0	1	0	0	1	0
487	5	12	0	1	0	0	1	0	1	1	0	0	0	0	1
488	5	12	0	1	0	0	1	0	1	1	0	0	0	1	0
489	5	12	0	1	0	0	1	1	0	0	0	1	0	1	0
490	5	12	0	1	0	0	1	1	0	0	0	1	1	0	0
491	5	12	0	1	0	0	1	1	0	0	1	0	0	1	0
492	5	12	0	1	0	0	1	1	0	0	1	0	1	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
493	5	12	0	1	0	0	1	1	0	0	1	1	0	0	0
494	5	12	0	1	0	0	1	1	0	1	0	0	0	1	0
495	5	12	0	1	0	0	1	1	0	1	0	0	1	0	0
496	5	12	0	1	0	0	1	1	0	1	1	0	0	0	0
497	5	12	0	1	0	0	1	1	1	0	0	1	0	0	0
498	5	12	0	1	0	0	1	1	1	0	1	0	0	0	0
499	5	12	0	1	0	0	1	1	1	1	0	0	0	0	0
500	5	12	0	1	0	1	0	0	0	0	0	1	0	1	1
501	5	12	0	1	0	1	0	0	0	0	0	1	1	1	0
502	5	12	0	1	0	1	0	0	0	0	1	0	0	1	1
503	5	12	0	1	0	1	0	0	0	0	1	0	1	1	0
504	5	12	0	1	0	1	0	0	0	0	1	1	0	1	0
505	5	12	0	1	0	1	0	0	0	1	0	0	0	1	1
506	5	12	0	1	0	1	0	0	0	1	0	0	1	1	0
507	5	12	0	1	0	1	0	0	0	1	1	0	0	1	0
508	5	12	0	1	0	1	0	0	1	0	0	1	0	1	0
509	5	12	0	1	0	1	0	0	1	0	1	0	0	1	0
510	5	12	0	1	0	1	0	0	1	1	0	0	0	1	0
511	5	12	0	1	0	1	0	1	0	0	0	1	0	0	1
512	5	12	0	1	0	1	0	1	0	0	0	1	0	1	0
513	5	12	0	1	0	1	0	1	0	0	0	1	1	0	0
514	5	12	0	1	0	1	0	1	0	0	1	0	0	0	1
515	5	12	0	1	0	1	0	1	0	0	1	0	0	1	0
516	5	12	0	1	0	1	0	1	0	0	1	0	1	0	0
517	5	12	0	1	0	1	0	1	0	0	1	1	0	0	0
518	5	12	0	1	0	1	0	1	0	1	0	0	0	0	1
519	5	12	0	1	0	1	0	1	0	1	0	0	0	1	0
520	5	12	0	1	0	1	0	1	0	1	0	0	1	0	0
521	5	12	0	1	0	1	0	1	0	1	1	0	0	0	0
522	5	12	0	1	0	1	0	1	1	0	0	1	0	0	0
523	5	12	0	1	0	1	0	1	1	0	1	0	0	0	0
524	5	12	0	1	0	1	0	1	1	1	0	0	0	0	0
525	5	12	0	1	0	1	1	0	0	0	0	1	0	0	1

WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
526	5	12	0	1	0	1	1	0	0	0	0	1	1	0	0
527	5	12	0	1	0	1	1	0	0	0	1	0	0	0	1
528	5	12	0	1	0	1	1	0	0	0	1	0	1	0	0
529	5	12	0	1	0	1	1	0	0	0	1	1	0	0	0
530	5	12	0	1	0	1	1	0	0	1	0	0	0	0	1
531	5	12	0	1	0	1	1	0	0	1	0	0	1	0	0
532	5	12	0	1	0	1	1	0	0	1	1	0	0	0	0
533	5	12	0	1	0	1	1	0	1	0	0	1	0	0	0
534	5	12	0	1	0	1	1	0	1	0	1	0	0	0	0
535	5	12	0	1	0	1	1	0	1	1	0	0	0	0	0
536	5	12	0	1	0	1	1	1	0	0	0	1	0	0	0
537	5	12	0	1	0	1	1	1	0	0	1	0	0	0	0
538	5	12	0	1	0	1	1	1	0	1	0	0	0	0	0
539	5	12	0	1	1	0	0	0	0	0	0	1	1	1	0
540	5	12	0	1	1	0	0	0	0	0	1	0	1	1	0
541	5	12	0	1	1	0	0	0	0	0	1	1	0	1	0
542	5	12	0	1	1	0	0	0	0	1	0	0	1	1	0
543	5	12	0	1	1	0	0	0	0	1	1	0	0	1	0
544	5	12	0	1	1	0	0	0	1	0	0	1	0	1	0
545	5	12	0	1	1	0	0	0	1	0	1	0	0	1	0
546	5	12	0	1	1	0	0	0	1	1	0	0	0	1	0
547	5	12	0	1	1	0	0	1	0	0	0	1	0	1	0
548	5	12	0	1	1	0	0	1	0	0	0	1	1	0	0
549	5	12	0	1	1	0	0	1	0	0	1	0	0	1	0
550	5	12	0	1	1	0	0	1	0	0	1	0	1	0	0
551	5	12	0	1	1	0	0	1	0	0	1	1	0	0	0
552	5	12	0	1	1	0	0	1	0	1	0	0	0	1	0
553	5	12	0	1	1	0	0	1	0	1	0	0	1	0	0
554	5	12	0	1	1	0	0	1	0	1	1	0	0	0	0
555	5	12	0	1	1	0	0	1	1	0	0	1	0	0	0
556	5	12	0	1	1	0	0	1	1	0	1	0	0	0	0
557	5	12	0	1	1	0	0	1	1	1	0	0	0	0	0
558	5	12	0	1	1	0	1	0	0	0	0	1	0	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
559	5	12	0	1	1	0	1	0	0	0	0	1	1	0	0
560	5	12	0	1	1	0	1	0	0	0	1	0	0	1	0
561	5	12	0	1	1	0	1	0	0	0	1	0	1	0	0
562	5	12	0	1	1	0	1	0	0	0	1	1	0	0	0
563	5	12	0	1	1	0	1	0	0	1	0	0	0	1	0
564	5	12	0	1	1	0	1	0	0	1	0	0	1	0	0
565	5	12	0	1	1	0	1	0	0	1	1	0	0	0	0
566	5	12	0	1	1	0	1	0	1	0	0	1	0	0	0
567	5	12	0	1	1	0	1	0	1	0	1	0	0	0	0
568	5	12	0	1	1	0	1	0	1	1	0	0	0	0	0
569	5	12	0	1	1	1	0	0	0	0	0	1	0	1	0
570	5	12	0	1	1	1	0	0	0	0	1	0	0	1	0
571	5	12	0	1	1	1	0	0	0	1	0	0	0	1	0
572	5	12	0	1	1	1	0	1	0	0	0	1	0	0	0
573	5	12	0	1	1	1	0	1	0	0	1	0	0	0	0
574	5	12	0	1	1	1	0	1	0	1	0	0	0	0	0
575	5	12	0	1	1	1	1	0	0	0	0	1	0	0	0
576	5	12	0	1	1	1	1	0	0	0	1	0	0	0	0
577	5	12	0	1	1	1	1	0	0	1	0	0	0	0	0
578	3	3	3	0	0	0	0	0	0	0	1	1	1	0	0
579	3	3	3	0	0	0	0	0	1	1	1	0	0	0	0
580	3	3	3	0	0	0	0	1	1	0	0	0	0	1	0
581	3	3	3	0	0	0	1	1	0	0	0	0	0	0	1
582	3	3	3	0	0	1	0	0	1	0	0	0	0	0	1
583	3	3	3	0	0	1	1	0	0	0	0	0	0	1	0
584	3	3	3	0	1	1	0	0	0	0	0	0	1	0	0
585	3	3	3	1	0	0	0	0	0	1	0	1	0	0	0
586	3	3	3	1	0	0	0	0	1	0	0	0	1	0	0
587	3	3	3	1	1	0	0	0	0	0	0	0	0	0	1
588	4	6	4	0	0	0	0	0	1	1	0	1	1	0	0
589	4	6	4	0	0	0	1	0	1	0	0	0	0	1	1
590	4	6	4	0	0	1	0	1	0	0	0	0	0	1	1
591	4	6	4	0	0	1	1	1	1	0	0	0	0	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
592	4	6	4	0	1	0	0	0	1	0	0	0	1	0	1
593	4	6	4	1	0	0	0	0	0	1	1	0	1	0	0
594	4	6	4	1	0	0	0	0	1	0	1	1	0	0	0
595	4	6	4	1	0	1	0	0	0	0	0	0	1	0	1
596	4	6	4	1	1	1	0	0	1	0	0	0	0	0	0
597	5	9	5	0	0	1	0	0	0	1	0	1	1	0	1
598	5	9	5	0	1	0	0	0	0	1	1	0	1	0	1
599	5	9	5	0	1	0	0	0	1	0	1	1	0	0	1
600	5	9	5	0	1	0	0	1	0	0	0	0	1	1	1
601	5	9	5	0	1	0	1	1	1	0	0	0	1	0	0
602	5	9	5	0	1	1	0	0	1	1	0	1	0	0	0
603	5	9	5	1	0	0	1	0	0	0	0	0	1	1	1
604	5	9	5	1	0	1	0	0	0	0	1	1	0	0	1
605	5	9	5	1	0	1	1	1	0	0	0	0	1	0	0
606	5	9	5	1	1	0	1	0	1	0	0	0	0	1	0
607	5	9	5	1	1	1	0	0	0	1	1	0	0	0	0
608	5	9	5	1	1	1	0	1	0	0	0	0	0	1	0
609	6	12	6	0	0	0	1	0	0	1	0	1	1	1	1
610	6	12	6	0	0	1	1	1	0	1	0	1	1	0	0
611	6	12	6	0	1	0	0	1	0	0	1	1	0	1	1
612	6	12	6	0	1	0	1	0	1	1	0	1	0	1	0
613	6	12	6	0	1	0	1	1	0	1	1	0	1	0	0
614	6	12	6	0	1	0	1	1	1	0	1	1	0	0	0
615	6	12	6	0	1	1	0	1	0	1	0	1	0	1	0
616	6	12	6	1	0	0	1	0	0	0	1	1	0	1	1
617	6	12	6	1	0	1	1	1	0	0	1	1	0	0	0
618	6	12	6	1	1	0	1	0	0	1	1	0	0	1	0
619	7	12	7	0	0	0	1	0	0	1	1	1	1	1	1
620	7	12	7	0	0	0	1	0	1	0	1	1	1	1	1
621	7	12	7	0	0	0	1	0	1	1	0	1	1	1	1
622	7	12	7	0	0	0	1	1	0	1	0	1	1	1	1
623	7	12	7	0	0	0	1	1	1	1	0	1	1	0	1
624	7	12	7	0	0	1	0	1	0	0	1	1	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
625	7	12	7	0	0	1	0	1	0	1	0	1	1	1	1
626	7	12	7	0	0	1	1	0	0	1	0	1	1	1	1
627	7	12	7	0	0	1	1	0	1	1	0	1	1	1	0
628	7	12	7	0	0	1	1	1	0	1	0	1	1	0	1
629	7	12	7	0	0	1	1	1	0	1	0	1	1	1	0
630	7	12	7	0	0	1	1	1	0	1	1	1	1	0	0
631	7	12	7	0	0	1	1	1	1	0	1	1	1	0	0
632	7	12	7	0	0	1	1	1	1	1	0	1	1	0	0
633	7	12	7	0	1	0	0	1	0	0	1	1	1	1	1
634	7	12	7	0	1	0	0	1	0	1	0	1	1	1	1
635	7	12	7	0	1	0	0	1	0	1	1	0	1	1	1
636	7	12	7	0	1	0	0	1	0	1	1	1	0	1	1
637	7	12	7	0	1	0	0	1	1	0	1	1	0	1	1
638	7	12	7	0	1	0	0	1	1	1	0	1	0	1	1
639	7	12	7	0	1	0	1	0	0	1	0	1	1	1	1
640	7	12	7	0	1	0	1	0	0	1	1	0	1	1	1
641	7	12	7	0	1	0	1	0	0	1	1	1	0	1	1
642	7	12	7	0	1	0	1	0	1	0	1	1	0	1	1
643	7	12	7	0	1	0	1	0	1	1	0	1	0	1	1
644	7	12	7	0	1	0	1	0	1	1	0	1	1	1	0
645	7	12	7	0	1	0	1	0	1	1	1	0	1	1	0
646	7	12	7	0	1	0	1	0	1	1	1	1	0	1	0
647	7	12	7	0	1	0	1	1	0	0	1	1	0	1	1
648	7	12	7	0	1	0	1	1	0	1	0	1	1	1	0
649	7	12	7	0	1	0	1	1	0	1	1	0	1	0	1
650	7	12	7	0	1	0	1	1	0	1	1	0	1	1	0
651	7	12	7	0	1	0	1	1	0	1	1	1	0	1	0
652	7	12	7	0	1	0	1	1	0	1	1	1	1	0	0
653	7	12	7	0	1	0	1	1	1	0	1	1	0	0	1
654	7	12	7	0	1	0	1	1	1	0	1	1	0	1	0
655	7	12	7	0	1	0	1	1	1	0	1	1	1	0	0
656	7	12	7	0	1	0	1	1	1	1	0	1	0	1	0
657	7	12	7	0	1	0	1	1	1	1	0	1	1	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
658	7	12	7	0	1	0	1	1	1	1	1	0	1	0	0
659	7	12	7	0	1	0	1	1	1	1	1	1	0	0	0
660	7	12	7	0	1	1	0	1	0	0	1	1	0	1	1
661	7	12	7	0	1	1	0	1	0	1	0	1	0	1	1
662	7	12	7	0	1	1	0	1	0	1	0	1	1	1	0
663	7	12	7	0	1	1	0	1	0	1	1	0	1	1	0
664	7	12	7	0	1	1	0	1	0	1	1	1	0	1	0
665	7	12	7	0	1	1	0	1	1	0	1	1	0	1	0
666	7	12	7	0	1	1	0	1	1	1	0	1	0	1	0
667	7	12	7	0	1	1	1	0	0	1	0	1	0	1	1
668	7	12	7	0	1	1	1	0	1	1	0	1	0	1	0
669	7	12	7	0	1	1	1	1	0	0	1	1	0	0	1
670	7	12	7	0	1	1	1	1	0	1	0	1	0	1	0
671	7	12	7	0	1	1	1	1	0	1	0	1	1	0	0
672	7	12	7	0	1	1	1	1	0	1	1	0	1	0	0
673	7	12	7	0	1	1	1	1	0	1	1	1	0	0	0
674	7	12	7	0	1	1	1	1	1	0	1	1	0	0	0
675	7	12	7	0	1	1	1	1	1	1	0	1	0	0	0
676	7	12	7	1	0	0	1	0	0	0	1	1	1	1	1
677	7	12	7	1	0	0	1	0	0	1	0	1	1	1	1
678	7	12	7	1	0	0	1	0	0	1	1	0	1	1	1
679	7	12	7	1	0	0	1	0	0	1	1	1	0	1	1
680	7	12	7	1	0	0	1	0	1	0	1	1	0	1	1
681	7	12	7	1	0	0	1	0	1	1	0	1	0	1	1
682	7	12	7	1	0	0	1	1	0	0	1	1	0	1	1
683	7	12	7	1	0	0	1	1	0	1	1	0	1	0	1
684	7	12	7	1	0	0	1	1	1	0	1	1	0	0	1
685	7	12	7	1	0	1	0	1	0	0	1	1	0	1	1
686	7	12	7	1	0	1	0	1	0	1	0	1	0	1	1
687	7	12	7	1	0	1	1	0	0	0	1	1	0	1	1
688	7	12	7	1	0	1	1	0	0	1	1	0	1	1	0
689	7	12	7	1	0	1	1	0	1	0	1	1	0	1	0
690	7	12	7	1	0	1	1	1	0	0	1	1	0	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
691	7	12	7	1	0	1	1	1	0	0	1	1	0	1	0
692	7	12	7	1	0	1	1	1	0	0	1	1	1	0	0
693	7	12	7	1	0	1	1	1	0	1	0	1	1	0	0
694	7	12	7	1	0	1	1	1	0	1	1	0	1	0	0
695	7	12	7	1	0	1	1	1	0	1	1	1	0	0	0
696	7	12	7	1	0	1	1	1	1	0	1	1	0	0	0
697	7	12	7	1	0	1	1	1	1	1	0	1	0	0	0
698	7	12	7	1	1	0	0	1	0	0	1	1	0	1	1
699	7	12	7	1	1	0	0	1	0	1	1	0	0	1	1
700	7	12	7	1	1	0	1	0	0	0	1	1	0	1	1
701	7	12	7	1	1	0	1	0	0	1	0	1	1	1	0
702	7	12	7	1	1	0	1	0	0	1	1	0	0	1	1
703	7	12	7	1	1	0	1	0	0	1	1	0	1	1	0
704	7	12	7	1	1	0	1	0	0	1	1	1	0	1	0
705	7	12	7	1	1	0	1	0	1	0	1	1	0	1	0
706	7	12	7	1	1	0	1	0	1	1	0	1	0	1	0
707	7	12	7	1	1	0	1	0	1	1	1	0	0	1	0
708	7	12	7	1	1	0	1	1	0	0	1	1	0	1	0
709	7	12	7	1	1	0	1	1	0	0	1	1	1	0	0
710	7	12	7	1	1	0	1	1	0	1	1	0	0	1	0
711	7	12	7	1	1	0	1	1	0	1	1	0	1	0	0
712	7	12	7	1	1	0	1	1	1	0	1	1	0	0	0
713	7	12	7	1	1	0	1	1	1	1	1	0	0	0	0
714	7	12	7	1	1	1	0	1	0	0	1	1	0	1	0
715	7	12	7	1	1	1	0	1	0	1	0	1	0	1	0
716	7	12	7	1	1	1	0	1	0	1	1	0	0	1	0
717	7	12	7	1	1	1	1	0	0	1	1	0	0	1	0
718	7	12	7	1	1	1	1	1	0	0	1	1	0	0	0
719	7	12	7	1	1	1	1	1	0	1	1	0	0	0	0
720	8	12	8	0	0	0	1	0	1	1	1	1	1	1	1
721	8	12	8	0	0	0	1	1	0	1	1	1	1	1	1
722	8	12	8	0	0	0	1	1	1	0	1	1	1	1	1
723	8	12	8	0	0	0	1	1	1	1	0	1	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
724	8	12	8	0	0	0	1	1	1	1	1	1	1	0	1
725	8	12	8	0	0	1	0	1	0	1	1	1	1	1	1
726	8	12	8	0	0	1	0	1	1	0	1	1	1	1	1
727	8	12	8	0	0	1	0	1	1	1	0	1	1	1	1
728	8	12	8	0	0	1	1	0	0	1	1	1	1	1	1
729	8	12	8	0	0	1	1	0	1	0	1	1	1	1	1
730	8	12	8	0	0	1	1	0	1	1	0	1	1	1	1
731	8	12	8	0	0	1	1	0	1	1	1	1	1	1	0
732	8	12	8	0	0	1	1	1	0	0	1	1	1	1	1
733	8	12	8	0	0	1	1	1	0	1	0	1	1	1	1
734	8	12	8	0	0	1	1	1	0	1	1	1	1	0	1
735	8	12	8	0	0	1	1	1	0	1	1	1	1	1	0
736	8	12	8	0	0	1	1	1	1	0	1	1	1	0	1
737	8	12	8	0	0	1	1	1	1	0	1	1	1	1	0
738	8	12	8	0	0	1	1	1	1	1	0	1	1	0	1
739	8	12	8	0	0	1	1	1	1	1	0	1	1	1	0
740	8	12	8	0	0	1	1	1	1	1	1	1	1	0	0
741	8	12	8	0	1	0	0	1	0	1	1	1	1	1	1
742	8	12	8	0	1	0	0	1	1	0	1	1	1	1	1
743	8	12	8	0	1	0	0	1	1	1	0	1	1	1	1
744	8	12	8	0	1	0	0	1	1	1	1	0	1	1	1
745	8	12	8	0	1	0	0	1	1	1	1	1	0	1	1
746	8	12	8	0	1	0	1	0	0	1	1	1	1	1	1
747	8	12	8	0	1	0	1	0	1	0	1	1	1	1	1
748	8	12	8	0	1	0	1	0	1	1	0	1	1	1	1
749	8	12	8	0	1	0	1	0	1	1	1	0	1	1	1
750	8	12	8	0	1	0	1	0	1	1	1	1	0	1	1
751	8	12	8	0	1	0	1	0	1	1	1	1	1	1	0
752	8	12	8	0	1	0	1	1	0	0	1	1	1	1	1
753	8	12	8	0	1	0	1	1	0	1	0	1	1	1	1
754	8	12	8	0	1	0	1	1	0	1	1	0	1	1	1
755	8	12	8	0	1	0	1	1	0	1	1	1	0	1	1
756	8	12	8	0	1	0	1	1	0	1	1	1	1	0	1
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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
757	8	12	8	0	1	0	1	1	0	1	1	1	1	1	0
758	8	12	8	0	1	0	1	1	1	0	1	1	0	1	1
759	8	12	8	0	1	0	1	1	1	0	1	1	1	0	1
760	8	12	8	0	1	0	1	1	1	0	1	1	1	1	0
761	8	12	8	0	1	0	1	1	1	1	0	1	0	1	1
762	8	12	8	0	1	0	1	1	1	1	0	1	1	0	1
763	8	12	8	0	1	0	1	1	1	1	0	1	1	1	0
764	8	12	8	0	1	0	1	1	1	1	1	0	1	0	1
765	8	12	8	0	1	0	1	1	1	1	1	0	1	1	0
766	8	12	8	0	1	0	1	1	1	1	1	1	0	0	1
767	8	12	8	0	1	0	1	1	1	1	1	1	0	1	0
768	8	12	8	0	1	0	1	1	1	1	1	1	1	0	0
769	8	12	8	0	1	1	0	1	0	0	1	1	1	1	1
770	8	12	8	0	1	1	0	1	0	1	0	1	1	1	1
771	8	12	8	0	1	1	0	1	0	1	1	0	1	1	1
772	8	12	8	0	1	1	0	1	0	1	1	1	0	1	1
773	8	12	8	0	1	1	0	1	0	1	1	1	1	1	0
774	8	12	8	0	1	1	0	1	1	0	1	1	0	1	1
775	8	12	8	0	1	1	0	1	1	0	1	1	1	1	0
776	8	12	8	0	1	1	0	1	1	1	0	1	0	1	1
777	8	12	8	0	1	1	0	1	1	1	0	1	1	1	0
778	8	12	8	0	1	1	0	1	1	1	1	0	1	1	0
779	8	12	8	0	1	1	0	1	1	1	1	1	0	1	0
780	8	12	8	0	1	1	1	0	0	1	0	1	1	1	1
781	8	12	8	0	1	1	1	0	0	1	1	0	1	1	1
782	8	12	8	0	1	1	1	0	0	1	1	1	0	1	1
783	8	12	8	0	1	1	1	0	1	0	1	1	0	1	1
784	8	12	8	0	1	1	1	0	1	1	0	1	0	1	1
785	8	12	8	0	1	1	1	0	1	1	0	1	1	1	0
786	8	12	8	0	1	1	1	0	1	1	1	0	1	1	0
787	8	12	8	0	1	1	1	0	1	1	1	1	0	1	0
788	8	12	8	0	1	1	1	1	0	0	1	1	0	1	1
789	8	12	8	0	1	1	1	1	0	0	1	1	1	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
790	8	12	8	0	1	1	1	1	0	1	0	1	0	1	1
791	8	12	8	0	1	1	1	1	0	1	0	1	1	0	1
792	8	12	8	0	1	1	1	1	0	1	0	1	1	1	0
793	8	12	8	0	1	1	1	1	0	1	1	0	1	0	1
794	8	12	8	0	1	1	1	1	0	1	1	0	1	1	0
795	8	12	8	0	1	1	1	1	0	1	1	1	0	0	1
796	8	12	8	0	1	1	1	1	0	1	1	1	0	1	0
797	8	12	8	0	1	1	1	1	0	1	1	1	1	0	0
798	8	12	8	0	1	1	1	1	1	0	1	1	0	0	1
799	8	12	8	0	1	1	1	1	1	0	1	1	0	1	0
800	8	12	8	0	1	1	1	1	1	0	1	1	1	0	0
801	8	12	8	0	1	1	1	1	1	1	0	1	0	0	1
802	8	12	8	0	1	1	1	1	1	1	0	1	0	1	0
803	8	12	8	0	1	1	1	1	1	1	0	1	1	0	0
804	8	12	8	0	1	1	1	1	1	1	1	0	1	0	0
805	8	12	8	0	1	1	1	1	1	1	1	1	0	0	0
806	8	12	8	1	0	0	1	0	0	1	1	1	1	1	1
807	8	12	8	1	0	0	1	0	1	0	1	1	1	1	1
808	8	12	8	1	0	0	1	0	1	1	0	1	1	1	1
809	8	12	8	1	0	0	1	0	1	1	1	0	1	1	1
810	8	12	8	1	0	0	1	0	1	1	1	1	0	1	1
811	8	12	8	1	0	0	1	1	0	0	1	1	1	1	1
812	8	12	8	1	0	0	1	1	0	1	0	1	1	1	1
813	8	12	8	1	0	0	1	1	0	1	1	0	1	1	1
814	8	12	8	1	0	0	1	1	0	1	1	1	0	1	1
815	8	12	8	1	0	0	1	1	0	1	1	1	1	0	1
816	8	12	8	1	0	0	1	1	1	0	1	1	0	1	1
817	8	12	8	1	0	0	1	1	1	0	1	1	1	0	1
818	8	12	8	1	0	0	1	1	1	1	0	1	0	1	1
819	8	12	8	1	0	0	1	1	1	1	0	1	1	0	1
820	8	12	8	1	0	0	1	1	1	1	1	0	1	0	1
821	8	12	8	1	0	0	1	1	1	1	1	1	0	0	1
822	8	12	8	1	0	1	0	1	0	0	1	1	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
823	8	12	8	1	0	1	0	1	0	1	0	1	1	1	1
824	8	12	8	1	0	1	0	1	0	1	1	0	1	1	1
825	8	12	8	1	0	1	0	1	0	1	1	1	0	1	1
826	8	12	8	1	0	1	0	1	1	0	1	1	0	1	1
827	8	12	8	1	0	1	0	1	1	1	0	1	0	1	1
828	8	12	8	1	0	1	1	0	0	0	1	1	1	1	1
829	8	12	8	1	0	1	1	0	0	1	0	1	1	1	1
830	8	12	8	1	0	1	1	0	0	1	1	0	1	1	1
831	8	12	8	1	0	1	1	0	0	1	1	1	0	1	1
832	8	12	8	1	0	1	1	0	0	1	1	1	1	1	0
833	8	12	8	1	0	1	1	0	1	0	1	1	0	1	1
834	8	12	8	1	0	1	1	0	1	0	1	1	1	1	0
835	8	12	8	1	0	1	1	0	1	1	0	1	0	1	1
836	8	12	8	1	0	1	1	0	1	1	0	1	1	1	0
837	8	12	8	1	0	1	1	0	1	1	1	0	1	1	0
838	8	12	8	1	0	1	1	0	1	1	1	1	0	1	0
839	8	12	8	1	0	1	1	1	0	0	1	1	0	1	1
840	8	12	8	1	0	1	1	1	0	0	1	1	1	0	1
841	8	12	8	1	0	1	1	1	0	0	1	1	1	1	0
842	8	12	8	1	0	1	1	1	0	1	0	1	0	1	1
843	8	12	8	1	0	1	1	1	0	1	0	1	1	0	1
844	8	12	8	1	0	1	1	1	0	1	0	1	1	1	0
845	8	12	8	1	0	1	1	1	0	1	1	0	1	0	1
846	8	12	8	1	0	1	1	1	0	1	1	0	1	1	0
847	8	12	8	1	0	1	1	1	0	1	1	1	0	0	1
848	8	12	8	1	0	1	1	1	0	1	1	1	0	1	0
849	8	12	8	1	0	1	1	1	0	1	1	1	1	0	0
850	8	12	8	1	0	1	1	1	1	0	1	1	0	0	1
851	8	12	8	1	0	1	1	1	1	0	1	1	0	1	0
852	8	12	8	1	0	1	1	1	1	0	1	1	1	0	0
853	8	12	8	1	0	1	1	1	1	1	0	1	0	0	1
854	8	12	8	1	0	1	1	1	1	1	0	1	0	1	0
855	8	12	8	1	0	1	1	1	1	1	0	1	1	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
856	8	12	8	1	0	1	1	1	1	1	1	0	1	0	0
857	8	12	8	1	0	1	1	1	1	1	1	1	0	0	0
858	8	12	8	1	1	0	0	1	0	0	1	1	1	1	1
859	8	12	8	1	1	0	0	1	0	1	0	1	1	1	1
860	8	12	8	1	1	0	0	1	0	1	1	0	1	1	1
861	8	12	8	1	1	0	0	1	0	1	1	1	0	1	1
862	8	12	8	1	1	0	0	1	1	0	1	1	0	1	1
863	8	12	8	1	1	0	0	1	1	1	0	1	0	1	1
864	8	12	8	1	1	0	0	1	1	1	1	0	0	1	1
865	8	12	8	1	1	0	1	0	0	0	1	1	1	1	1
866	8	12	8	1	1	0	1	0	0	1	0	1	1	1	1
867	8	12	8	1	1	0	1	0	0	1	1	0	1	1	1
868	8	12	8	1	1	0	1	0	0	1	1	1	0	1	1
869	8	12	8	1	1	0	1	0	0	1	1	1	1	1	0
870	8	12	8	1	1	0	1	0	1	0	1	1	0	1	1
871	8	12	8	1	1	0	1	0	1	0	1	1	1	1	0
872	8	12	8	1	1	0	1	0	1	1	0	1	0	1	1
873	8	12	8	1	1	0	1	0	1	1	0	1	1	1	0
874	8	12	8	1	1	0	1	0	1	1	1	0	0	1	1
875	8	12	8	1	1	0	1	0	1	1	1	0	1	1	0
876	8	12	8	1	1	0	1	0	1	1	1	1	0	1	0
877	8	12	8	1	1	0	1	1	0	0	1	1	0	1	1
878	8	12	8	1	1	0	1	1	0	0	1	1	1	0	1
879	8	12	8	1	1	0	1	1	0	0	1	1	1	1	0
880	8	12	8	1	1	0	1	1	0	1	0	1	1	1	0
881	8	12	8	1	1	0	1	1	0	1	1	0	0	1	1
882	8	12	8	1	1	0	1	1	0	1	1	0	1	0	1
883	8	12	8	1	1	0	1	1	0	1	1	0	1	1	0
884	8	12	8	1	1	0	1	1	0	1	1	1	0	1	0
885	8	12	8	1	1	0	1	1	0	1	1	1	1	0	0
886	8	12	8	1	1	0	1	1	1	0	1	1	0	0	1
887	8	12	8	1	1	0	1	1	1	0	1	1	0	1	0
888	8	12	8	1	1	0	1	1	1	0	1	1	1	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
889	8	12	8	1	1	0	1	1	1	1	0	1	0	1	0
890	8	12	8	1	1	0	1	1	1	1	0	1	1	0	0
891	8	12	8	1	1	0	1	1	1	1	1	0	0	0	1
892	8	12	8	1	1	0	1	1	1	1	1	0	0	1	0
893	8	12	8	1	1	0	1	1	1	1	1	0	1	0	0
894	8	12	8	1	1	0	1	1	1	1	1	1	0	0	0
895	8	12	8	1	1	1	0	1	0	0	1	1	0	1	1
896	8	12	8	1	1	1	0	1	0	0	1	1	1	1	0
897	8	12	8	1	1	1	0	1	0	1	0	1	0	1	1
898	8	12	8	1	1	1	0	1	0	1	0	1	1	1	0
899	8	12	8	1	1	1	0	1	0	1	1	0	0	1	1
900	8	12	8	1	1	1	0	1	0	1	1	0	1	1	0
901	8	12	8	1	1	1	0	1	0	1	1	1	0	1	0
902	8	12	8	1	1	1	0	1	1	0	1	1	0	1	0
903	8	12	8	1	1	1	0	1	1	1	0	1	0	1	0
904	8	12	8	1	1	1	0	1	1	1	1	0	0	1	0
905	8	12	8	1	1	1	1	0	0	0	1	1	0	1	1
906	8	12	8	1	1	1	1	0	0	1	0	1	0	1	1
907	8	12	8	1	1	1	1	0	0	1	0	1	1	1	0
908	8	12	8	1	1	1	1	0	0	1	1	0	0	1	1
909	8	12	8	1	1	1	1	0	0	1	1	0	1	1	0
910	8	12	8	1	1	1	1	0	0	1	1	1	0	1	0
911	8	12	8	1	1	1	1	0	1	0	1	1	0	1	0
912	8	12	8	1	1	1	1	0	1	1	0	1	0	1	0
913	8	12	8	1	1	1	1	0	1	1	1	0	0	1	0
914	8	12	8	1	1	1	1	1	0	0	1	1	0	0	1
915	8	12	8	1	1	1	1	1	0	0	1	1	0	1	0
916	8	12	8	1	1	1	1	1	0	0	1	1	1	0	0
917	8	12	8	1	1	1	1	1	0	1	0	1	0	1	0
918	8	12	8	1	1	1	1	1	0	1	0	1	1	0	0
919	8	12	8	1	1	1	1	1	0	1	1	0	0	0	1
920	8	12	8	1	1	1	1	1	0	1	1	0	0	1	0
921	8	12	8	1	1	1	1	1	0	1	1	0	1	0	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
922	8	12	8	1	1	1	1	1	0	1	1	1	0	0	0
923	8	12	8	1	1	1	1	1	1	0	1	1	0	0	0
924	8	12	8	1	1	1	1	1	1	1	0	1	0	0	0
925	8	12	8	1	1	1	1	1	1	1	1	0	0	0	0
926	9	12	9	0	0	0	1	1	1	1	1	1	1	1	1
927	9	12	9	0	0	1	0	1	1	1	1	1	1	1	1
928	9	12	9	0	0	1	1	0	1	1	1	1	1	1	1
929	9	12	9	0	0	1	1	1	0	1	1	1	1	1	1
930	9	12	9	0	0	1	1	1	1	0	1	1	1	1	1
931	9	12	9	0	0	1	1	1	1	1	0	1	1	1	1
932	9	12	9	0	0	1	1	1	1	1	1	1	1	0	1
933	9	12	9	0	0	1	1	1	1	1	1	1	1	1	0
934	9	12	9	0	1	0	0	1	1	1	1	1	1	1	1
935	9	12	9	0	1	0	1	0	1	1	1	1	1	1	1
936	9	12	9	0	1	0	1	1	0	1	1	1	1	1	1
937	9	12	9	0	1	0	1	1	1	0	1	1	1	1	1
938	9	12	9	0	1	0	1	1	1	1	0	1	1	1	1
939	9	12	9	0	1	0	1	1	1	1	1	0	1	1	1
940	9	12	9	0	1	0	1	1	1	1	1	1	0	1	1
941	9	12	9	0	1	0	1	1	1	1	1	1	1	0	1
942	9	12	9	0	1	0	1	1	1	1	1	1	1	1	0
943	9	12	9	0	1	1	0	1	0	1	1	1	1	1	1
944	9	12	9	0	1	1	0	1	1	0	1	1	1	1	1
945	9	12	9	0	1	1	0	1	1	1	0	1	1	1	1
946	9	12	9	0	1	1	0	1	1	1	1	0	1	1	1
947	9	12	9	0	1	1	0	1	1	1	1	1	0	1	1
948	9	12	9	0	1	1	0	1	1	1	1	1	1	1	0
949	9	12	9	0	1	1	1	0	0	1	1	1	1	1	1
950	9	12	9	0	1	1	1	0	1	0	1	1	1	1	1
951	9	12	9	0	1	1	1	0	1	1	0	1	1	1	1
952	9	12	9	0	1	1	1	0	1	1	1	0	1	1	1
953	9	12	9	0	1	1	1	0	1	1	1	1	0	1	1
954	9	12	9	0	1	1	1	0	1	1	1	1	1	1	0

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
955	9	12	9	0	1	1	1	1	0	0	1	1	1	1	1
956	9	12	9	0	1	1	1	1	0	1	0	1	1	1	1
957	9	12	9	0	1	1	1	1	0	1	1	0	1	1	1
958	9	12	9	0	1	1	1	1	0	1	1	1	0	1	1
959	9	12	9	0	1	1	1	1	0	1	1	1	1	0	1
960	9	12	9	0	1	1	1	1	0	1	1	1	1	1	0
961	9	12	9	0	1	1	1	1	1	0	1	1	0	1	1
962	9	12	9	0	1	1	1	1	1	0	1	1	1	0	1
963	9	12	9	0	1	1	1	1	1	0	1	1	1	1	0
964	9	12	9	0	1	1	1	1	1	1	0	1	0	1	1
965	9	12	9	0	1	1	1	1	1	1	0	1	1	0	1
966	9	12	9	0	1	1	1	1	1	1	0	1	1	1	0
967	9	12	9	0	1	1	1	1	1	1	1	0	1	0	1
968	9	12	9	0	1	1	1	1	1	1	1	0	1	1	0
969	9	12	9	0	1	1	1	1	1	1	1	1	0	0	1
970	9	12	9	0	1	1	1	1	1	1	1	1	0	1	0
971	9	12	9	0	1	1	1	1	1	1	1	1	1	0	0
972	9	12	9	1	0	0	1	0	1	1	1	1	1	1	1
973	9	12	9	1	0	0	1	1	0	1	1	1	1	1	1
974	9	12	9	1	0	0	1	1	1	0	1	1	1	1	1
975	9	12	9	1	0	0	1	1	1	1	0	1	1	1	1
976	9	12	9	1	0	0	1	1	1	1	1	0	1	1	1
977	9	12	9	1	0	0	1	1	1	1	1	1	0	1	1
978	9	12	9	1	0	0	1	1	1	1	1	1	1	0	1
979	9	12	9	1	0	1	0	1	0	1	1	1	1	1	1
980	9	12	9	1	0	1	0	1	1	0	1	1	1	1	1
981	9	12	9	1	0	1	0	1	1	1	0	1	1	1	1
982	9	12	9	1	0	1	0	1	1	1	1	0	1	1	1
983	9	12	9	1	0	1	0	1	1	1	1	1	0	1	1
984	9	12	9	1	0	1	1	0	0	1	1	1	1	1	1
985	9	12	9	1	0	1	1	0	1	0	1	1	1	1	1
986	9	12	9	1	0	1	1	0	1	1	0	1	1	1	1
987	9	12	9	1	0	1	1	0	1	1	1	0	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
988	9	12	9	1	0	1	1	0	1	1	1	1	0	1	1
989	9	12	9	1	0	1	1	0	1	1	1	1	1	1	0
990	9	12	9	1	0	1	1	1	0	0	1	1	1	1	1
991	9	12	9	1	0	1	1	1	0	1	0	1	1	1	1
992	9	12	9	1	0	1	1	1	0	1	1	0	1	1	1
993	9	12	9	1	0	1	1	1	0	1	1	1	0	1	1
994	9	12	9	1	0	1	1	1	0	1	1	1	1	0	1
995	9	12	9	1	0	1	1	1	0	1	1	1	1	1	0
996	9	12	9	1	0	1	1	1	1	0	1	1	0	1	1
997	9	12	9	1	0	1	1	1	1	0	1	1	1	0	1
998	9	12	9	1	0	1	1	1	1	0	1	1	1	1	0
999	9	12	9	1	0	1	1	1	1	1	0	1	0	1	1
1000	9	12	9	1	0	1	1	1	1	1	0	1	1	0	1
1001	9	12	9	1	0	1	1	1	1	1	0	1	1	1	0
1002	9	12	9	1	0	1	1	1	1	1	1	0	1	0	1
1003	9	12	9	1	0	1	1	1	1	1	1	0	1	1	0
1004	9	12	9	1	0	1	1	1	1	1	1	1	0	0	1
1005	9	12	9	1	0	1	1	1	1	1	1	1	0	1	0
1006	9	12	9	1	0	1	1	1	1	1	1	1	1	0	0
1007	9	12	9	1	1	0	0	1	0	1	1	1	1	1	1
1008	9	12	9	1	1	0	0	1	1	0	1	1	1	1	1
1009	9	12	9	1	1	0	0	1	1	1	0	1	1	1	1
1010	9	12	9	1	1	0	0	1	1	1	1	0	1	1	1
1011	9	12	9	1	1	0	0	1	1	1	1	1	0	1	1
1012	9	12	9	1	1	0	1	0	0	1	1	1	1	1	1
1013	9	12	9	1	1	0	1	0	1	0	1	1	1	1	1
1014	9	12	9	1	1	0	1	0	1	1	0	1	1	1	1
1015	9	12	9	1	1	0	1	0	1	1	1	0	1	1	1
1016	9	12	9	1	1	0	1	0	1	1	1	1	0	1	1
1017	9	12	9	1	1	0	1	0	1	1	1	1	1	1	0
1018	9	12	9	1	1	0	1	1	0	0	1	1	1	1	1
1019	9	12	9	1	1	0	1	1	0	1	0	1	1	1	1
1020	9	12	9	1	1	0	1	1	0	1	1	0	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1021	9	12	9	1	1	0	1	1	0	1	1	1	0	1	1
1022	9	12	9	1	1	0	1	1	0	1	1	1	1	0	1
1023	9	12	9	1	1	0	1	1	0	1	1	1	1	1	0
1024	9	12	9	1	1	0	1	1	1	0	1	1	0	1	1
1025	9	12	9	1	1	0	1	1	1	0	1	1	1	0	1
1026	9	12	9	1	1	0	1	1	1	0	1	1	1	1	0
1027	9	12	9	1	1	0	1	1	1	1	0	1	0	1	1
1028	9	12	9	1	1	0	1	1	1	1	0	1	1	0	1
1029	9	12	9	1	1	0	1	1	1	1	0	1	1	1	0
1030	9	12	9	1	1	0	1	1	1	1	1	0	0	1	1
1031	9	12	9	1	1	0	1	1	1	1	1	0	1	0	1
1032	9	12	9	1	1	0	1	1	1	1	1	0	1	1	0
1033	9	12	9	1	1	0	1	1	1	1	1	1	0	0	1
1034	9	12	9	1	1	0	1	1	1	1	1	1	0	1	0
1035	9	12	9	1	1	0	1	1	1	1	1	1	1	0	0
1036	9	12	9	1	1	1	0	1	0	0	1	1	1	1	1
1037	9	12	9	1	1	1	0	1	0	1	0	1	1	1	1
1038	9	12	9	1	1	1	0	1	0	1	1	0	1	1	1
1039	9	12	9	1	1	1	0	1	0	1	1	1	0	1	1
1040	9	12	9	1	1	1	0	1	0	1	1	1	1	1	0
1041	9	12	9	1	1	1	0	1	1	0	1	1	0	1	1
1042	9	12	9	1	1	1	0	1	1	0	1	1	1	1	0
1043	9	12	9	1	1	1	0	1	1	1	0	1	0	1	1
1044	9	12	9	1	1	1	0	1	1	1	0	1	1	1	0
1045	9	12	9	1	1	1	0	1	1	1	1	0	0	1	1
1046	9	12	9	1	1	1	0	1	1	1	1	0	1	1	0
1047	9	12	9	1	1	1	0	1	1	1	1	1	0	1	0
1048	9	12	9	1	1	1	1	0	0	0	1	1	1	1	1
1049	9	12	9	1	1	1	1	0	0	1	0	1	1	1	1
1050	9	12	9	1	1	1	1	0	0	1	1	0	1	1	1
1051	9	12	9	1	1	1	1	0	0	1	1	1	0	1	1
1052	9	12	9	1	1	1	1	0	0	1	1	1	1	1	0
1053	9	12	9	1	1	1	1	0	1	0	1	1	0	1	1

WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1054	9	12	9	1	1	1	1	0	1	0	1	1	1	1	0
1055	9	12	9	1	1	1	1	0	1	1	0	1	0	1	1
1056	9	12	9	1	1	1	1	0	1	1	0	1	1	1	0
1057	9	12	9	1	1	1	1	0	1	1	1	0	0	1	1
1058	9	12	9	1	1	1	1	0	1	1	1	0	1	1	0
1059	9	12	9	1	1	1	1	0	1	1	1	1	0	1	0
1060	9	12	9	1	1	1	1	1	0	0	1	1	0	1	1
1061	9	12	9	1	1	1	1	1	0	0	1	1	1	0	1
1062	9	12	9	1	1	1	1	1	0	0	1	1	1	1	0
1063	9	12	9	1	1	1	1	1	0	1	0	1	0	1	1
1064	9	12	9	1	1	1	1	1	0	1	0	1	1	0	1
1065	9	12	9	1	1	1	1	1	0	1	0	1	1	1	0
1066	9	12	9	1	1	1	1	1	0	1	1	0	0	1	1
1067	9	12	9	1	1	1	1	1	0	1	1	0	1	0	1
1068	9	12	9	1	1	1	1	1	0	1	1	0	1	1	0
1069	9	12	9	1	1	1	1	1	0	1	1	1	0	0	1
1070	9	12	9	1	1	1	1	1	0	1	1	1	0	1	0
1071	9	12	9	1	1	1	1	1	0	1	1	1	1	0	0
1072	9	12	9	1	1	1	1	1	1	0	1	1	0	0	1
1073	9	12	9	1	1	1	1	1	1	0	1	1	0	1	0
1074	9	12	9	1	1	1	1	1	1	0	1	1	1	0	0
1075	9	12	9	1	1	1	1	1	1	1	0	1	0	0	1
1076	9	12	9	1	1	1	1	1	1	1	0	1	0	1	0
1077	9	12	9	1	1	1	1	1	1	1	0	1	1	0	0
1078	9	12	9	1	1	1	1	1	1	1	1	0	0	0	1
1079	9	12	9	1	1	1	1	1	1	1	1	0	0	1	0
1080	9	12	9	1	1	1	1	1	1	1	1	0	1	0	0
1081	9	12	9	1	1	1	1	1	1	1	1	1	0	0	0
1082	10	12	10	0	0	1	1	1	1	1	1	1	1	1	1
1083	10	12	10	0	1	0	1	1	1	1	1	1	1	1	1
1084	10	12	10	0	1	1	0	1	1	1	1	1	1	1	1
1085	10	12	10	0	1	1	1	0	1	1	1	1	1	1	1
1086	10	12	10	0	1	1	1	1	0	1	1	1	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1087	10	12	10	0	1	1	1	1	1	0	1	1	1	1	1
1088	10	12	10	0	1	1	1	1	1	1	0	1	1	1	1
1089	10	12	10	0	1	1	1	1	1	1	1	0	1	1	1
1090	10	12	10	0	1	1	1	1	1	1	1	1	0	1	1
1091	10	12	10	0	1	1	1	1	1	1	1	1	1	0	1
1092	10	12	10	0	1	1	1	1	1	1	1	1	1	1	0
1093	10	12	10	1	0	0	1	1	1	1	1	1	1	1	1
1094	10	12	10	1	0	1	0	1	1	1	1	1	1	1	1
1095	10	12	10	1	0	1	1	0	1	1	1	1	1	1	1
1096	10	12	10	1	0	1	1	1	0	1	1	1	1	1	1
1097	10	12	10	1	0	1	1	1	1	0	1	1	1	1	1
1098	10	12	10	1	0	1	1	1	1	1	0	1	1	1	1
1099	10	12	10	1	0	1	1	1	1	1	1	0	1	1	1
1100	10	12	10	1	0	1	1	1	1	1	1	1	0	1	1
1101	10	12	10	1	0	1	1	1	1	1	1	1	1	0	1
1102	10	12	10	1	0	1	1	1	1	1	1	1	1	1	0
1103	10	12	10	1	1	0	0	1	1	1	1	1	1	1	1
1104	10	12	10	1	1	0	1	0	1	1	1	1	1	1	1
1105	10	12	10	1	1	0	1	1	0	1	1	1	1	1	1
1106	10	12	10	1	1	0	1	1	1	0	1	1	1	1	1
1107	10	12	10	1	1	0	1	1	1	1	0	1	1	1	1
1108	10	12	10	1	1	0	1	1	1	1	1	0	1	1	1
1109	10	12	10	1	1	0	1	1	1	1	1	1	0	1	1
1110	10	12	10	1	1	0	1	1	1	1	1	1	1	0	1
1111	10	12	10	1	1	0	1	1	1	1	1	1	1	1	0
1112	10	12	10	1	1	1	0	1	0	1	1	1	1	1	1
1113	10	12	10	1	1	1	0	1	1	0	1	1	1	1	1
1114	10	12	10	1	1	1	0	1	1	1	0	1	1	1	1
1115	10	12	10	1	1	1	0	1	1	1	1	0	1	1	1
1116	10	12	10	1	1	1	0	1	1	1	1	1	0	1	1
1117	10	12	10	1	1	1	0	1	1	1	1	1	1	1	0
1118	10	12	10	1	1	1	1	0	0	1	1	1	1	1	1
1119	10	12	10	1	1	1	1	0	1	0	1	1	1	1	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1120	10	12	10	1	1	1	1	0	1	1	0	1	1	1	1
1121	10	12	10	1	1	1	1	0	1	1	1	0	1	1	1
1122	10	12	10	1	1	1	1	0	1	1	1	1	0	1	1
1123	10	12	10	1	1	1	1	0	1	1	1	1	1	1	0
1124	10	12	10	1	1	1	1	1	0	0	1	1	1	1	1
1125	10	12	10	1	1	1	1	1	0	1	0	1	1	1	1
1126	10	12	10	1	1	1	1	1	0	1	1	0	1	1	1
1127	10	12	10	1	1	1	1	1	0	1	1	1	0	1	1
1128	10	12	10	1	1	1	1	1	0	1	1	1	1	0	1
1129	10	12	10	1	1	1	1	1	0	1	1	1	1	1	0
1130	10	12	10	1	1	1	1	1	1	0	1	1	0	1	1
1131	10	12	10	1	1	1	1	1	1	0	1	1	1	0	1
1132	10	12	10	1	1	1	1	1	1	0	1	1	1	1	0
1133	10	12	10	1	1	1	1	1	1	1	0	1	0	1	1
1134	10	12	10	1	1	1	1	1	1	1	0	1	1	0	1
1135	10	12	10	1	1	1	1	1	1	1	0	1	1	1	0
1136	10	12	10	1	1	1	1	1	1	1	1	0	0	1	1
1137	10	12	10	1	1	1	1	1	1	1	1	0	1	0	1
1138	10	12	10	1	1	1	1	1	1	1	1	0	1	1	0
1139	10	12	10	1	1	1	1	1	1	1	1	1	0	0	1
1140	10	12	10	1	1	1	1	1	1	1	1	1	0	1	0
1141	10	12	10	1	1	1	1	1	1	1	1	1	1	0	0
1142	11	12	11	0	1	1	1	1	1	1	1	1	1	1	1
1143	11	12	11	1	0	1	1	1	1	1	1	1	1	1	1
1144	11	12	11	1	1	0	1	1	1	1	1	1	1	1	1
1145	11	12	11	1	1	1	0	1	1	1	1	1	1	1	1
1146	11	12	11	1	1	1	1	0	1	1	1	1	1	1	1
1147	11	12	11	1	1	1	1	1	0	1	1	1	1	1	1
1148	11	12	11	1	1	1	1	1	1	0	1	1	1	1	1
1149	11	12	11	1	1	1	1	1	1	1	0	1	1	1	1
1150	11	12	11	1	1	1	1	1	1	1	1	0	1	1	1
1151	11	12	11	1	1	1	1	1	1	1	1	1	0	1	1
1152	11	12	11	1	1	1	1	1	1	1	1	1	1	0	1

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WWTP3 (MUCT). List of Pareto-optimal solutions.

Layout	# sensors	# obs.	# red.	Flow											
				1	2	3	4	5	6	7	8	9	10	11	12
1153	11	12	11	1	1	1	1	1	1	1	1	1	1	1	0
1154	12	12	12	1	1	1	1	1	1	1	1	1	1	1	1