

1 Stabilizing Control of a Urine Nitrification Process in 2 the Presence of Sensor Drift

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7 **Abstract**

Sensor drift is commonly observed across engineering disciplines, particularly in harsh media such as wastewater. In this study, a novel stabilizing controller for nitrification of high strength ammonia solutions is designed based on online signal derivatives. The controller uses the derivative of a drifting nitrite signal to determine if nitrite-oxidizing bacteria (NOB) are substrate limited or substrate inhibited. To ensure a meaningful interpretation of the derivative signal, the process is excited in a cyclic manner by repeatedly exposing the NOB to substrate-limited and substrate-inhibited conditions. The resulting control system successfully prevented nitrite accumulations for a period of 72 days in a laboratory-scale reactor. Slow disturbances in the form of feed composition changes and temperature changes were successfully handled by the controller while short-term temperature disturbances are shown to pose a challenge to the current version of this controller. Most importantly, we demonstrate that drift-tolerant control for the purpose of process stabilization can be achieved without sensor redundancy by combin-

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ing deliberate input excitation, qualitative trend analysis, and coarse process knowledge.

8 *Keywords:* nitrite control, inflection point, shape constrained splines,
9 relative measurement, online experiment, nitrification

10 **1. Introduction**

11 Control loops relying on absolute sensor values often suffer from sensor
12 faults. This study presents a novel control concept to stabilise a reactor for
13 nitrification of high strength ammonia solutions in the presence of sensor
14 drift. To this end, the controller is designed to exploit information from the
15 signal derivatives in a deliberately excited process. In wastewater, biological,
16 chemical, and physical factors lead to particularly intense wear and tear
17 of sensors. Hence, even mature sensor hardware such as pH sensors still
18 exhibit drift when exposed to this harsh medium. This drift occurs at time
19 scales that are much longer than typical process dynamics, challenging a
20 comparison with the sensor data history (temporal redundancy) (Ohmura
21 et al., Submitted). Furthermore, drift tends to occur in all sensors exposed
22 to the same medium challenging its detection based on redundant placement
23 of sensors (spatial redundancy). Lack of spatial and temporal redundancy
24 impedes the application of tools such as active fault tolerant control that
25 correct drift automatically based on redundant information (Blanke et al.,
26 2016).

27 The root causes of sensor drift are generally assumed to be known well

28 - e.g., biofilm formation, salt deposition, electrode oxidation etc. - but are
29 typically hard to quantify. There are a few attempts to investigate drift of
30 sensors quantitatively by controlled offline experiments (Ohmura et al., Sub-
31 mitted) or by online experiments (Samuelsson et al., 2018). However, drift
32 is typically identified by means of on-site manual reference measurements in
33 practice. This makes drift expensive to detect and correct, particularly when
34 remote or decentralised systems are considered.

35 The limited capacity to quantify sensor drift in wastewater processes on
36 the one hand and the need to control these processes on the other hand,
37 led to the development of methods that disregard absolute sensor values and
38 extract information that is represented in the derivatives of the sensor sig-
39 nal. The most discussed (soft-)sensor signals that reveal relevant information
40 without relying on a classical notions of accuracy are pH, oxidation-reduction
41 potential (ORP) (Al-Ghusain et al., 1995), and oxygen uptake rate (Baeza
42 et al., 2002). Al-Ghusain et al. (1995) used the derivatives of pH and ORP
43 to operate an aerobic/anoxic sludge digestion reactor. In these cases, the
44 sequenced operation creates the dynamics in the recorded sensor signals that
45 enable information extraction. In continuously operated processes, trend-
46 based monitoring and control is possible thanks to naturally occurring peri-
47 odicity of the (unmeasured) process input disturbances (e.g. hydraulic load,
48 nitrogen load, Thürlimann et al., 2018).

49 The application of trend-based control concepts is expected to be more
50 challenging in systems without naturally occurring disturbances. The source-

51 separated collection and nitrification of anthropogenic urine for the purpose
52 of fertilizer recovery is an example of such a system. Separated collection
53 of undiluted urine at the building or household level enables to smoothen
54 the hydraulic load with a small buffer tank. Our experience (not shown)
55 suggests that short-term storage of anthropogenic urine does not affect the
56 total nitrogen concentration, meaning that the naturally occurring variations
57 in the nitrogen load to a nitrifying reactor are expected to be small. Despite
58 the apparent lack of input disturbances, the process is sensitive to inadvertent
59 nitrite accumulation events, which cause a complete failure of the process in
60 absence of corrective actions (Fumasoli et al., 2016; Sun et al., 2012).

61 An economically viable method to measure nitrite online is UV-Vis ab-
62 sorbance spectrophotometry. However, this measurement principle lacks
63 specificity and therefore needs a model to extract the nitrite concentrations
64 from the absorbance measurement. Despite the availability of robust hard-
65 ware, extrapolation of such models makes drift of the nitrite signal a very
66 likely phenomenon (Gruber et al., 2006; Brito et al., 2014; Etheridge et al.,
67 2014), as is also demonstrated below.

68 The lack of natural or operational dynamics, the presence of signal drift,
69 and the open-loop unstable process of urine nitrification motivates the devel-
70 opment of a specialized control concept. This control concept, as explained
71 in detail below, extracts the essential information needed to prevent dan-
72 gerous nitrite accumulation events by means of *(i)* deliberate induction of
73 process dynamics (excitation) and *(ii)* trend analysis of a drifting sensor sig-

nal. In turn, this information extraction process enables the construction of single-in-single-out (SISO) controller for stabilization of the urine nitrification process.

2. Material and methods

2.1. Conceptual model of the control problem

In this paragraph, a conceptual model of the urine nitrification process is presented. The concept illustrates the different process states (Gujer, 2008), growth rate of the ammonia oxidizing bacteria (μAOB) and growth rate of the nitrite oxidizing bacteria (μNOB) and connections indicating the causal relationships between these variables and the sign of the magnitude of each influence (positive/negative influence). In the control literature, these signs are known as the signs of gains (Åström and Murray, 2008). It is important to note that this conceptual model only includes the effects considered relevant to tackle the identified process stabilization challenge. Only dynamic effects with a lower time constant than the controller are considered (e.g., biomass concentration stays approximately constant within this time scale). In addition, direct inhibition of the AOB and NOB activity by ammonia is considered marginal in the studied operational region (pH 5.9 to 7.0). The indicated signs of gains are only valid if all other states and rates remain constant and under constraints given in Fig. 1.

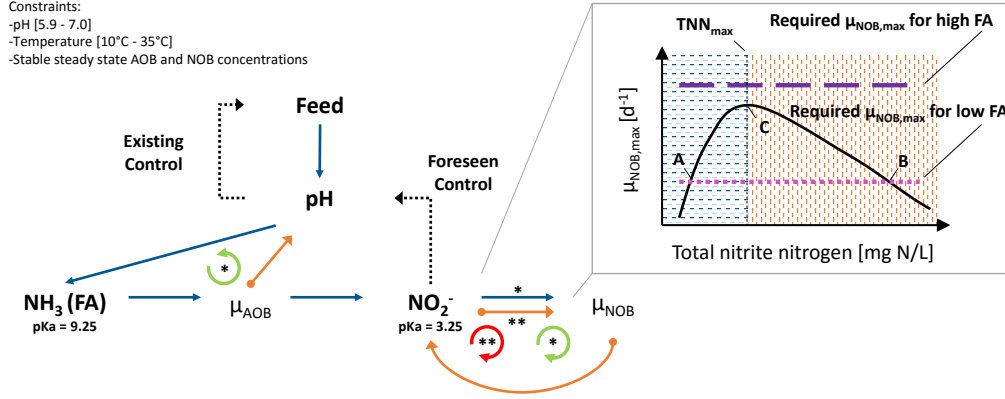


Figure 1: Conceptual model of urine nitrification. Left panel: Process states, growth rates, and gains. Blue arrows: positive gains; orange arrows with dot: negative gains; Green arrows: negative feedback loop; Red arrows: positive feedback loop. Right panel: Nitrite oxidizing bacteria growth rate (μ_{NOB}) as a schematic function of total nitrite nitrogen concentration. Low nitrite concentration (blue dashes): NOB substrate limited; High nitrite concentration (orange dashes): NOB substrate inhibited. The top (bottom) horizontal line indicates the required μ_{NOB} to oxidise all the nitrite produced by the AOB given a high (low) free ammonia concentration.

94 The blue arrows indicate a positive gain, the orange dot-arrows indicate a
 95 negative gain of the connected elements. For example, an increasing loading
 96 rate leads to an increased pH (i.e., positive gain) and an increasing AOB
 97 rate (μ_{AOB}) leads to a decreased pH (i.e., negative gain). The gains can
 98 create loops. Such loops are open loop stable if the product of the gains is
 99 negative (e.g., pH - NH_3 - μ_{AOB}) (green/* circle arrows). This means these
 100 loops are self-stabilizing. For example, an increase of the pH due to a process
 101 disturbance (e.g. higher hydraulic load, higher pH of influent) will increase

the free ammonia (NH_3 or FA) concentration in the bulk, which in turn raises the μAOB . In turn, this decreases the pH, therefore stabilising this part of the process. A loop with a positive product of its gains is a positive feedback loop and can lead, when not controlled properly, to a complete disappearance of elements in the loop (i.e., open loop unstable).

In the present case, nitrite has a negative gain to μNOB when the nitrite concentrations are high (i.e., orange arrow). A high nitrite concentration reduces the nitrite oxidation rate. This increases the net nitrite production rate in turn inducing to an even stronger inhibition of the NOB. Eventually, this leads to NOB wash-out and process failure. This part of the process is open loop stable if the nitrite concentration remains low (i.e. blue arrow). Under such circumstances, marginal increases of the nitrite concentration increase the NOB activity, which decreases the net nitrite production rate. Practically, the process can only be stabilised by reducing the AOB activity whenever the nitrite concentration reaches NOB-inhibiting levels. This is possible by making the reactor anoxic, in which case nitrite is reduced by denitrification. This may induce growth of denitrifiers however, in turn leading to a loss of nitrogen to the environment. For the purpose of fertilizer production, a better approach consists of reducing the nitrite production rate by decreasing the pH setpoint. Low pH values induce lower FA concentrations, so that eventually the nitrite oxidation rate is higher than the nitrite production rate (Fig. 1 right).

More details concerning the influence of the NO_2^- concentration on the

125 NOB activity (μNOB) are shown in the top right box of Fig. 1. It shows
 126 μNOB as a function of the total nitrite concentration (TNN) (full line). The
 127 growth rate is composed of both the substrate limiting effect and the inhibi-
 128 tion effect nitrite has on the NOB. Most studies, but not all, list nitrite as the
 129 substrate and free nitrous acid (FNA) as the inhibiting substance for NOB
 130 (Park and Bae, 2009). This means that the growth rate is pH dependent.
 131 For simplicity, we neglect any effect of the pH and assume that TNN is both
 132 the substrate and the inhibitory substance. In practice the exact value of
 133 the TNN concentration where the effect of substrate inhibition overpowers
 134 the effect of substrate affinity is known only coarsely due to a variety of fac-
 135 tors. These include process-related factors such as *(i)* the incompleteness of
 136 available knowledge describing the influences of biomass composition, urine
 137 composition, and temperature on the observed nitrite affinity and nitrite
 138 inhibition effects (van Hulle et al., 2007) and *(ii)* insufficient accuracy and
 139 precision of laboratory concentration measurements to determine the critical
 140 nitrite concentration precisely, even under otherwise stable conditions.

141 The black dashed arrows indicate the existing pH control loop as well as
 142 the newly proposed nitrite control loop for process stabilization. The pH con-
 143 trol loop is described below and is designed to protect the AOB from washout
 144 (cf. 2.2.3). The second dashed arrow indicates the proposed master control of
 145 the pH control loop in the reactor based on the nitrite concentration, which
 146 is aimed at preventing washout of the NOB.

147 2.2. Basic reactor set-up and operation

148 The reactor used for this study is a cylindrical 12 L continuous flow
149 stirred tank reactor (CSTR) nitrifying source-separated urine. The hydraulic
150 retention time (HRT) of the reactor system varied between 7 and 13 days,
151 as is discussed below. The reactor was operated without biomass retention
152 so that the sludge retention time (SRT) equals the HRT. The reactor was
153 in operation since 19 months prior to the start of this study. The reactor
154 includes two recirculation loops. One brings the reactor medium to the UV-
155 Vis spectrophotometer with a HRT of 10 s. The other brings medium to a pH
156 sensor pack used in another study (HRT: 20 s, Ohmura et al., Submitted).
157 The feed composition is described in 2.5.3. The available alkalinity limits the
158 fraction of the total ammonium converted via nitrite to nitrate to roughly
159 50% (detailed results below).

160 2.2.1. Analytics

161 Samples are taken regularly from the reactor to evaluate if the proposed
162 controller keeps the nitrite concentration low. To measure chemical species
163 the following steps are executed. Per sample at least 2 ml of reactor media
164 are filtered with 0.45 μm GF/PET filter (Art. Nr. 916 02, Macherey-Nagel,
165 Oensingen, Switzerland) mounted on a sampling syringe. Ammonium, ni-
166 trite, and nitrate concentrations are measured in every sample. The influent
167 ammonium and chemical oxygen demand (COD) concentrations are mea-
168 sured each time the influent tank was replaced. The exchange dates and con-

169 concentrations are listed in the Electronic Supplementary Material (Table S1 and
 170 S2). Ammonium concentrations are determined either through a Metrohm
 171 930 Compact IC Flex (Metrohm, Herisau, Switzerland, method: Metrohm
 172 Metrosep C6, 250/4.0), with flow injection analysis (FIA, Lachat QC8500,
 173 Hach Company, Loveland, USA) or with colorimetric test kits (LCK303,
 174 Hach-Lange, Berlin, as all LCK test kits). Nitrite reference concentrations
 175 are determined either colorimetrically with an LCK341 test kit or with strip
 176 tests (MQuant, Merck KGaA, Darmstadt, Germany) to confirm low nitrite
 177 concentrations. Due to dilution, the detection limit with the LCK341 kit
 178 is approximately 2 mg N/L. Nitrate is measured in the laboratory through
 179 a Metrohm 881 Compact IC Pro (Metrohm, Herisau, Switzerland, chemical
 180 suppression Metrosep A Supp 7, 250/4.0) or with an LCK340 kit. For the
 181 measurement of the COD, LCK314 kits are used. A standard deviation of
 182 the measurement including the dilution procedure is estimated with a sin-
 183 gle triplicate of measurements prior to this study: FIA ammonium: 0.60%
 184 at 2340 mg N/L, LCK 341 nitrite: 0.60% at 45.7 mg N/L, and IC nitrate:
 185 0.55% at 2226 mg N/L.

186 2.2.2. *Sensors*

187 A 2 mm path length spectro::lyser V1 (s::can, Vienna, Austria) is used
 188 to measure the UV-Vis absorbance spectrum of the reactor content in-situ.
 189 The sensor measures the absorbance from 200 to 750 nm with a resolution
 190 of 2.5 nm. The *Ex-situ wBM* model from Thürlimann et al. (Submitted) is

191 used to estimate the nitrite concentrations. Each minute a new absorbance
192 measurement and in turn a new estimation of the nitrite concentration is
193 obtained. Furthermore, two pH and two dissolved oxygen (DO) sensors are
194 installed, one of each is used for control (DO: COS61D and pH: CPS11D,
195 Endress&Hauser, Reinach, Switzerland)

196 2.2.3. Low-level control

197 The DO concentration is controlled between 5 and 6 mg O₂/L by on/off
198 control of the airflow through a fine-bubble diffuser (6 L/min). The feed
199 pump is pH controlled (cf. 2.3). The reactor is equipped with a water
200 based heating/cooling system (FN-25, Julabo, Seelbach GmbH, Germany).
201 The temperature of the reactor was controlled at 25°C with an accuracy of
202 $\pm 0.5^\circ\text{C}$ due to diurnal variations unless stated otherwise.

203 2.3. Stabilizing Nitrite Control

204 The ultimate goal of our controller is to ensure that both AOB and NOB
205 are retained and remain active in the studied reactor in the presence of
206 typical disturbances. The envisioned control system has to ensure that the
207 net nitrite production rate is zero, meaning that the ammonia oxidation is
208 the rate-limiting step and that no ammonia is accumulating in the system.
209 To this end, the master controller manages the nitrite oxidation (i.e., NOB)
210 and the slave controller manages the ammonia oxidation (i.e., AOB). At the
211 top of Fig. 2, the proposed cascaded control loops are illustrated. The slave
212 control loop, using pH to control the inflow was described by Udert et al.

213 (2003). It controls the AOB by manipulating the inflow rate based on the
214 pH setpoint given by the master control. The master control takes the nitrite
215 concentration estimation as an indicator to decide if the ammonia oxidation
216 rate is higher or lower than the theoretical maximum nitrite oxidation rate
217 and sets the pH set point accordingly. The slave controller turns on the
218 inflow pump when the pH drops below the pH setpoint. Instead of a higher
219 second pH setpoint the pump is turned off again based on a timer (6 s). In
220 each pump event 20 ± 5 mL of urine is fed to the reactor.

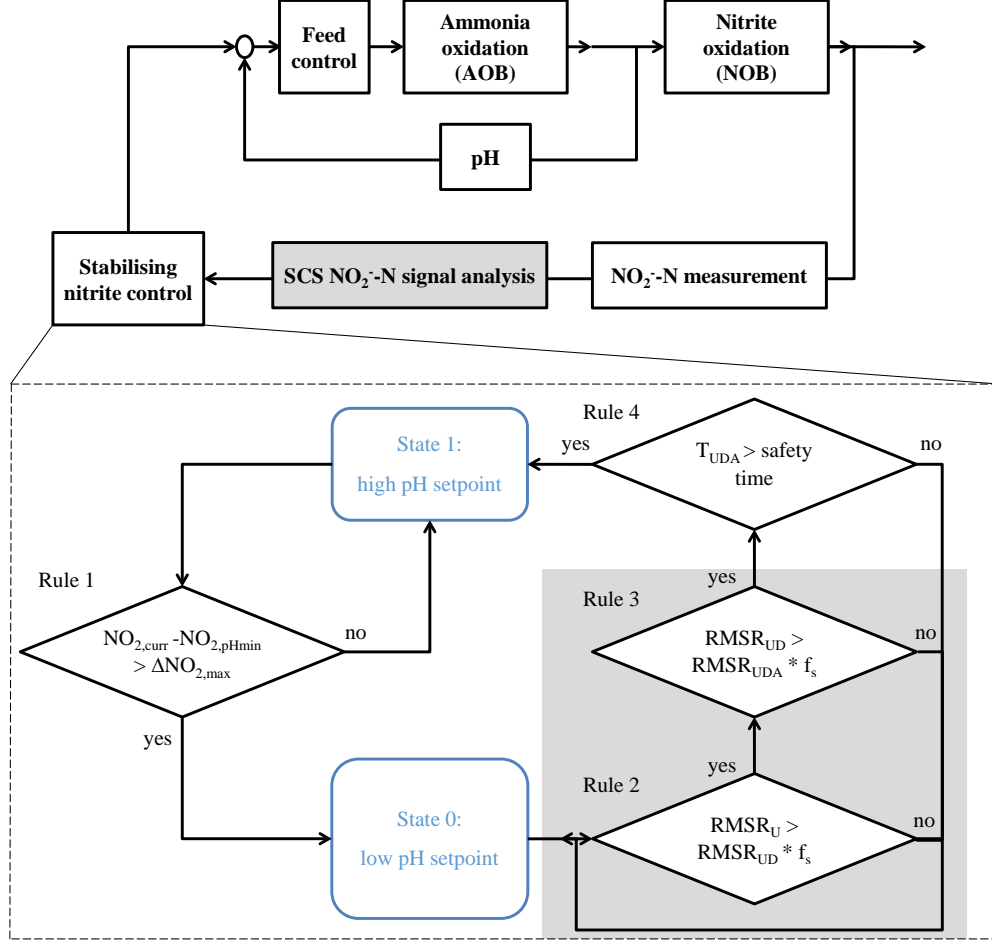


Figure 2: Control loops. Top: Cascade control of AOB and NOB. Bottom: rule based decision process to change master controller states. The grey box marks the rules based on the shape constrained splines method.

221 The master controller sets the pH setpoint to the high setpoint (6.8) when
 222 the nitrite concentration is such that the NOB are dominated by substrate
 223 limitation (i.e., open loop stable, Fig. 1 right, horizontally blue dashed area).

224 This is referred to as controller state 1. If nitrite is so high that the NOB
 225 are dominated by substrate inhibition (i.e., open loop unstable, Fig. 1 right,
 226 vertically orange dashed area) the controller sets the pH to the low setpoint
 227 (6.1). This is further referred to as controller state 0. The drift in the
 228 controller input signal forces to design the controller such that it relies on
 229 the information contained in the first and second derivative of the signal to
 230 distinguish between NOB inhibitory and NOB limiting nitrite concentration
 231 levels. The information that is actually used in the controller is the identified
 232 presence of the inflection point in the downward trend (i.e., negative first
 233 derivative, second derivative sign switches from negative to positive). It
 234 is assumed, that in the period during which the inflection point appears
 235 μAOB is constant: First, at this time, the pH has already reached its low
 236 setpoint value and the influent composition is assumed constant, thus there
 237 are no changes in the FA concentration. Second, the temperature is assumed
 238 constant. Furthermore, it is assumed that AOB activity is almost insensitive
 239 to changes in the nitrite concentration at the nitrite concentration level where
 240 the μNOB starts to be dominated by substrate limitation (Fig. 1, TNN_{max})
 241 (Wang et al., 2014). Consequently, when the inflection point appears, the
 242 nitrite dynamics are only driven by the NOB.

243 When NOB are dominated by substrate inhibition and a low pH results
 244 in low FA availability for AOB (Fig. 1, right, pink dotted line), the NOB ac-
 245 tivity increases as nitrite concentrations are decreasing (Fig. 1, moving from
 246 Point B to Point C). At the landmark value (Kuipers, 1986) TNN_{max} , the

247 μ NOB and in turn the net nitrite degradation rate reach their maxima and
248 then start to decrease (Fig. 1, moving from Point C to Point A). Thus under
249 normal circumstances, the appearance of the infection point in the decreasing
250 signal is linked with the NOB achieving their maximum growth rate (point
251 C) and the start of substrate limitation dominating the NOB. Note that the
252 precise value of TNN_{\max} is considered unknown.

253 Identifying an inflection point in the downward trend requires first and fore-
254 most that the nitrite concentration has been high enough to induce observable
255 inhibition of the NOB. Thus, the controller has to be designed in such a way
256 that NOB-inhibiting conditions are reached in a way that allows reducing the
257 nitrite concentration as soon as inhibiting conditions are detected. Accord-
258 ingly, the master controller increases the pH setpoint such that the increased
259 FA concentration leads to an ammonia oxidation rate (i.e., nitrite production
260 rate) higher than the maximal nitrite consumption rate (Fig. 1, right, purple
261 dashed line). The nitrite increase is controlled by monitoring the absolute
262 increase of the signal value. In our case, the last nitrite value prior to the pH
263 increase is taken as a reference for a relative increase of 15 mg N/L. Once
264 this threshold is reached the controller switches from state 1 to state 0.

265 In control state 0, the controller re-stabilises the process by decreasing
266 the pH (Fig. 1, right, pink dotted line). As long as the nitrite concentration
267 in the previous increase never exceeds point B (Fig. 1, right), the reduction
268 in the FA concentration to the lower line puts the steady state concentration
269 back to point A and a net nitrite reduction starts. The controller gets the

270 confirmation of reaching a stable nitration by identifying the inflection
271 point in the downward trend. This ends one control cycle. Details concerning
272 the practical implementation of this controller can be found in the Electronic
273 Supplementary Material.

274 *2.4. Identification of inflection point*

275 To identify the inflection point in the downward nitrite signal, the signal
276 is analyzed by means of a qualitative trend analysis (QTA) method. For this
277 purpose, the shape-constrained spline function (SCS) method described in
278 earlier works (Villez et al., 2013; Villez and Habermacher, 2016; Derlon et al.,
279 2017; Mašić et al., 2017) is selected. The detailed modifications necessary
280 for this work, particularly to enable online deployment, are described in the
281 Electronic Supplementary Material. We illustrate the essence of this method
282 next.

283 Fig. 3 illustrates two different time points in the analysis of the same
284 event. The top panels show the data (black dotted) and the three shape-
285 constrained spline models fitted to the data. These three models are increas-
286 ingly flexible. One model (U) is constrained to be isotonic (monotonically
287 increasing). The next model (UD) is constrained to exhibit a unimodal shape
288 (single maximum, no minimum) with a concave profile after the identified
289 maximum. The last model (UDA) has a unimodal shape also but is allowed
290 to have a single inflection point after the identified maximum. The bottom
291 panels show the corresponding root mean squared residual (RMSR) of the

three models evaluated with all the data available until this time. In the left plot, the data already exhibited a maximum and the U model, constrained to be continuously increasing, starts to fit worse than the two other models. This can be seen in the almost flat shape the U model (red, wide-dashed) has from hour 6 on and thus results in an increasing RMSR of the U model (RMSR_U). Both the UD and UDA models approximate the time series well as their shape constraints are flexible enough.

The right panel shows the time point at which the full data set of the event is available. Visual inspection reveals that the data exhibits a maximum and an inflection point in the downward trend - as expected. Shortly after hour 9 it becomes clear that a maximum is present in the time series given that RMSR_U increases dramatically. As desired, the RMSR_{UD} increases once the curve exhibits a convex form (hour 14), thus leading to the detection of the downward inflection point shortly after. A video illustrating the incremental data acquisition and concurrent data analysis can be found in the Electronic Supplementary Material.

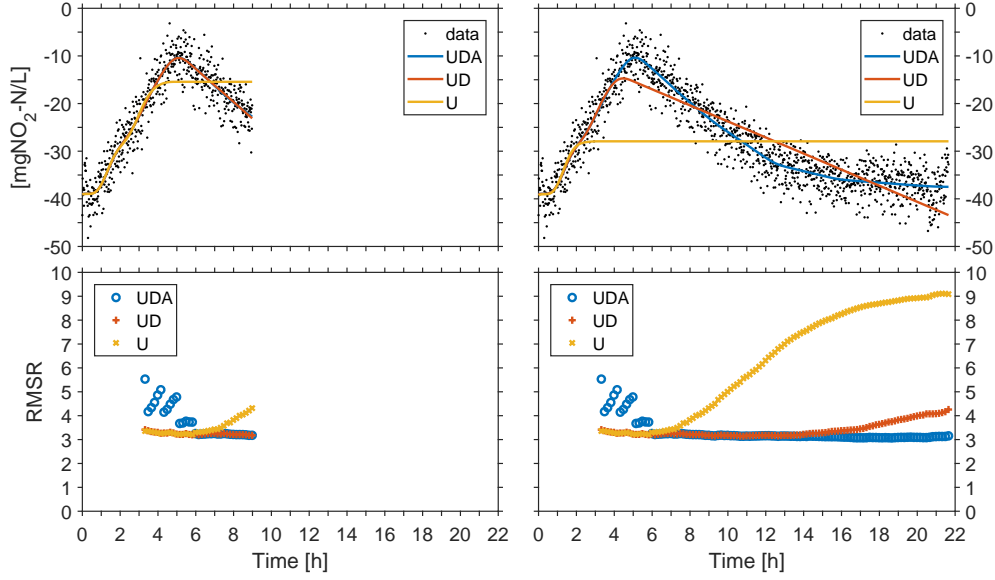


Figure 3: Shape constrained spline model fitting. Top panels: Raw data with three different qualitative sequence models fitted to the available data iduring an *event*. Bottom panels: Computed root mean squared residuals as a function of time. Left: Information available after 9h. Right: Information available at the end of the event.

308 2.5. Unmeasured process disturbances

309 Three unmeasured disturbances are tested or monitored to evaluate the
 310 robustness of the controller. First, the signal drift itself, which is expected to
 311 occur under any given practical operational condition. Thus, sensor drift is
 312 not actively induced but allowed to occur in a passive manner instead. Sec-
 313 ond, the robustness of the controller is tested against temperature dynamics
 314 and thirdly against influent composition dynamics.

315 2.5.1. Determination of drift rate

316 The nitrite reference measurements are compared with the estimation
317 of the UV-Vis nitrite signal to monitor if the sensor signal actually drifts.
318 The rate at which the difference of these two values change is the drift rate.
319 Periods of drift are selected visually and then described by a piece-wise linear
320 trend line. Drift is monitored in the whole experimental period (19.03.2018
321 - 30.05.2018, 72 days) including the periods in which the temperature and
322 switch of influent source experiments (see below) take place.

323 2.5.2. Temperature experiments

324 In the ambient temperature range ($10 - 35^{\circ}\text{C}$) the μAOB increases faster
325 with temperature than the μNOB (Hellenga et al., 1998). To evaluate whether
326 such disturbances pose a challenge to our control system the reactor is cooled
327 or heated by means of the water based cooling and heating jacket. A *temper-*
328 *ature low* experiment was executed twice. Each time the reactor was cooled
329 down from 25°C to 22°C within 10-12 h and then heated back to 25°C within
330 10-12 h (16./17.04.2018 and 19./20.04.2018). A *temperature high* experiment
331 was executed in two versions. In a long version (23.04.2018-25.04.2018), the
332 temperature was increased within 8 h from 25 to 28°C , kept there for 36 h
333 and then cooled down back to 25°C within 10 h. For the two short version
334 experiments (26.04.2018 and 27.04.2018), the temperature was raised from
335 25 to 28°C within 10 h and then immediately cooled back to 25°C within
336 10 h. Note that these temperatures are typical for indoor applications and

337 subtropical regions of the world.

338 2.5.3. *Switch of influent source*

339 Changes in the feed composition are another source of unmeasured pro-
340 cess disturbances. To evaluate whether the controller is robust to this type
341 of disturbances, we devised an experiment in the reactor feed composition is
342 changed deliberately. On April 30th, 2018 at 09:13, the influent was changed
343 from source-separated urine collected from male toilets and urinals to source-
344 separated urine collected from female toilets. Both female and male urine
345 collection system are located in the Forum Chriesbach Building at Eawag
346 Dübendorf in Switzerland. The urine from female toilets has a lower concen-
347 tration of ammonia (-31%) and COD (-37%) due to dilution with flushing
348 water in the NoMix toilets. A more comprehensive overview can be found in
349 Fumasoli et al. (2016). More details can be found in the Electronic Supple-
350 mentary Material (Table S2.1 and S2.2).

351 3. Results

352 3.1. *Control behaviour*

353 The following paragraph describes one control cycle during which the
354 complete control system was in autonomous use (Fig. 4). At around 12:00,
355 the controller state is 1 and the pH controller setpoint is 6.8 (*high pH set-*
356 *point*, 3rd panel). This induces an increase in nitrite, as expected (top panel).
357 After reaching the threshold for a maximal difference to the previously de-
358 fined baseline (i.e., *Rule 1*) the controller state is set to 0. The pH setpoint

359 is reduced to 6.1 (*low pH setpoint*, 2nd panel). From this time on, the nitrite
 360 signal is recorded for analysis by the SCS models. After collecting the mini-
 361 mal number of nitrite measurements in this time series, the SCS models are
 362 fit for the first time. In the 4th panel one can see the incremental changes of
 363 the RMSR of the three different models U, UD, and UDA as new nitrite mea-
 364 surements are added to the analyzed data series. One can see that RMSR_U
 365 is always larger than RMSR_{UD} and RMSR_{UDA} . The interpretation is that
 366 the control algorithm recognises that the peak nitrite concentration has al-
 367 ready occurred before this first time of comparative analysis. At 02:30 the
 368 RMSR_{UD} starts to deviate visually from the RMSR_{UDA} . The vertical line in
 369 the bottom panel indicates when *Rule 3* was evaluated as true shortly before
 370 07:00, meaning that the controller now considers the presence of an inflection
 371 point in the nitrite signal as a sure thing. Shortly before 09:00 the 2 h timer
 372 *Rule 4* is also evaluated true and the controller switches back to state 1 (high
 373 pH setpoint). Consequently, the controller memorises the last nitrite value
 374 to reference the next nitrite increase and increases the pH setpoint to 6.8.
 375 This completes one autonomous cycle of the proposed controller.

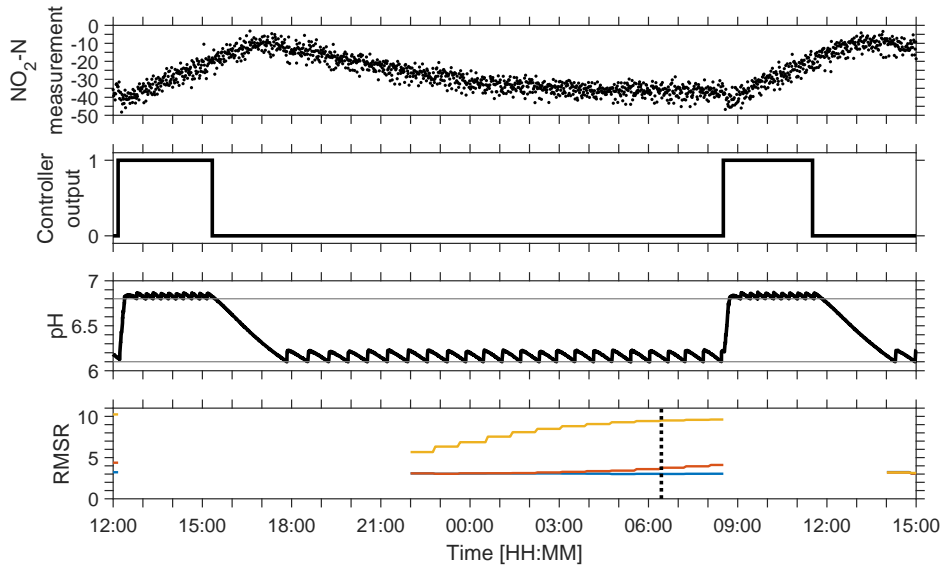


Figure 4: Operational data from one event as a function of time. 1st panel: Nitrite signal (controller input). 2nd panel: Controller state. 3rd panel: pH sensor signal with two setpoints. 4th panel: RMSR of the three fitted SCS models.

3.2. Controller performance

Fig. 5 illustrates nitrite end of cycle concentrations (ECC) measured after the detection of the inflection point but before the pH is increased again (T5, see Electronic Supplementary Material). The recorded ECC values represent substrate limiting conditions for the NOB during the complete experimental period. The ECC progressively decreased during the period of autonomous control. The solid retention time (i.e., equals the hydraulic retention time) never exceeds 13 days (Fig. 6 bottom panel) meaning that the experimental period covers more than 5.5 time the HRT (and SRT). Thus, the controller not only kept the nitrite concentration low in the short term, but also suc-

386 cessfully prevented washout of the NOB population within a significant test
 387 period.

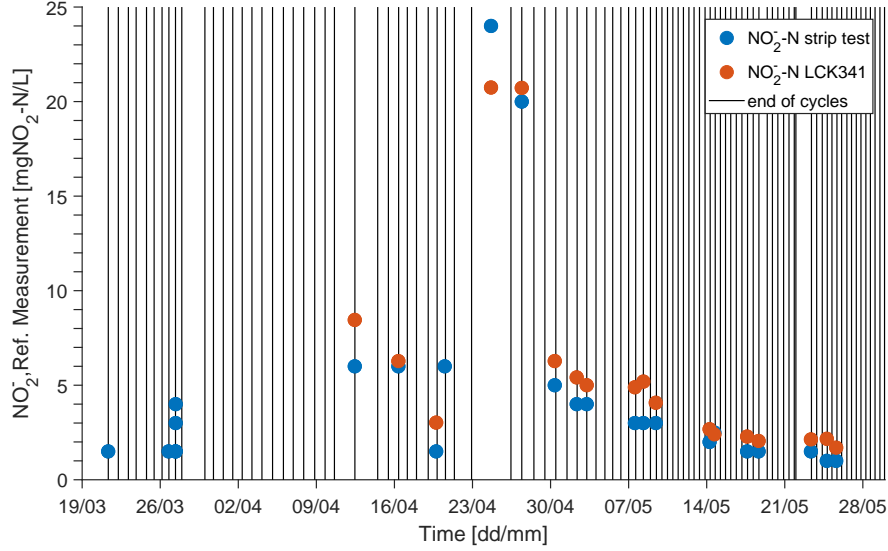


Figure 5: Nitrite end of cycle concentrations after identification of inflection point but before the start of next event (T5, see Electronic Supplementary Material). Vertical lines indicate the end of a cycle.

388 Despite the very noisy input signal, the visual inspection of the results
 389 reveals that the model selection by means of comparing the RMSRs of the
 390 three models has never resulted in a false negative or false positive identi-
 391 cation of the maximum or the inflection point. It has to be noted that most
 392 likely there is a certain delay in the identification due to the chosen value
 393 for the knot distance. To quantify the delay, in every cycle the ground truth
 394 about TNN_{\max} (Fig. 1) would need to be determined.

395 3.3. Unmeasured process disturbances

396 3.3.1. Drift

397 The controller input signal drift is illustrated in the top panel of Fig. 6.
398 Drift occurred during the entire experimental period. The estimated drift
399 rates, obtained with the fitted piece-wise linear trend line, range from - 0.8
400 to 1.1 mg NO₂⁻-N/L/d. Thus, one can conclude that the observed signal drift
401 poses a meaningful challenge for process control, which has been mitigated
402 successfully by the proposed control system. It is noted that the changes in
403 the drift rates can only be explained partially. The vertical grey dashed lines
404 indicate sensor cleaning. Sign changes of the drift rate are unexpected for
405 this kind of intervention (i.e., a signal jump is expected when biofilm and
406 solids are removed from the sensor.) Note that the initial difference between
407 the UV-Vis based nitrite value and the nitrite reference measurements has
408 been caused by drift in the 9 months in between the calibration period and
409 the start of this study.

410 3.3.2. Switch of influent source

411 The change in influent composition (Fig. 6, 30.04.2018, yellow dashed
412 line) induces a change in the sign of the drift rate from 1.1 to -0.4 mg N/L/d.
413 In the first 15 days after the influent switch the ammonia and nitrate concen-
414 tration in the reactor decrease from 2000 to 1300 mg N/L (Fig. 6, 2nd panel).
415 The controller reacted to the new lower concentrated influent and increased
416 the hydraulic loading, which is indicated by the decreased hydraulic residence

time (HRT) from around 13 to 7 days (Fig. 6, 3rd panel). Furthermore, also the control cycle length decreased from around 1 to 0.5 d (Fig. 5). Thus, the controller was able to reject this disturbance and keep nitrite levels low. At the same time, the slave controller was still acting as intended and compensated the decreased specific ammonia load with increased hydraulic loading.

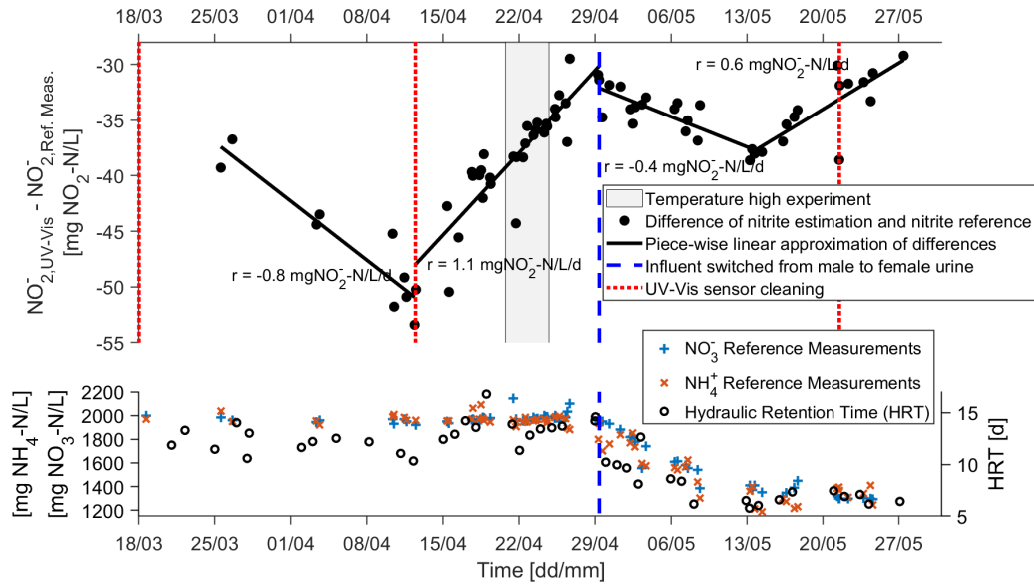


Figure 6: Drift rate, reactor nitrogen species concentrations, and hydraulic residence time. Top panel: deviations between the nitrite concentration signal and reference measurements as a function of time, piece-wise linear drift rate estimation, times of sensor cleaning, the time of influent source change from male to female urine, and the high temperature period. Bottom panel: Ammonia and nitrate concentrations in bulk and hydraulic retention time.

3.3.3. Temperature experiment

Fig. 7 shows the results of the temperature high experiment. The first complete cycle shown in this figure starts on April 21st and illustrates the

425 operation before the temperature change. On April 22nd , the controller sets
 426 the pH setpoint to 6.8 (Fig. 7, 2nd panel) before the temperature increase
 427 is visible (Fig. 7, 3rd panel). The nitrite concentration rises for some time
 428 (Fig. 7, 1st panel) while the temperature increases also. Shortly after, the
 429 controller decreases the pH setpoint while the temperature continues to in-
 430 crease. However, the nitrite signal remains at a high level (around -15 mg
 431 N/L) relative to the cycle before the temperature change (-30 mg N/L). Ni-
 432 trite reference measurements confirm that elevated nitrite concentrations are
 433 the cause for this difference in the signal, which remain around 20 mg N/L
 434 instead of around 5 mg N/L as in the previous cycle. This very small drop
 435 in nitrite compared to the peak concentration, also leads to a delay in the
 436 identification of the inflection point (Fig. 7, 4th panel) compared to the visual
 437 impression obtained by looking at the figure. The controller identified an in-
 438 flection point only in the afternoon of April, 24th . An increase in pH at this
 439 time point would lead to an even higher accumulation of nitrite. To ensure
 440 successful testing of the controller against other disturbances, the controller
 441 is deactivated temporally (cf. grey area 2nd panel) and the temperature set-
 442 point is again decreased to 25°C. The cooling of the bulk media leads to a
 443 decrease in the nitrite starting at midnight on the 25th . At noon of the same
 444 day, the nitrite signal and reference measurements drop to the levels reached
 445 in the first cycle (Fig. 7, 22nd) and the controller is restarted shortly after.
 446 Thus, the temperature high experiment indicated that fast temperature in-
 447 creases pose a threat to the proposed control system. The temperature low

448 experiment did not reveal any relevant finding with respect to the control
 449 performance. The only notable change compared to the 25°C operation is
 450 the reduction in the peak nitrite concentration by about 5 mg N/L.

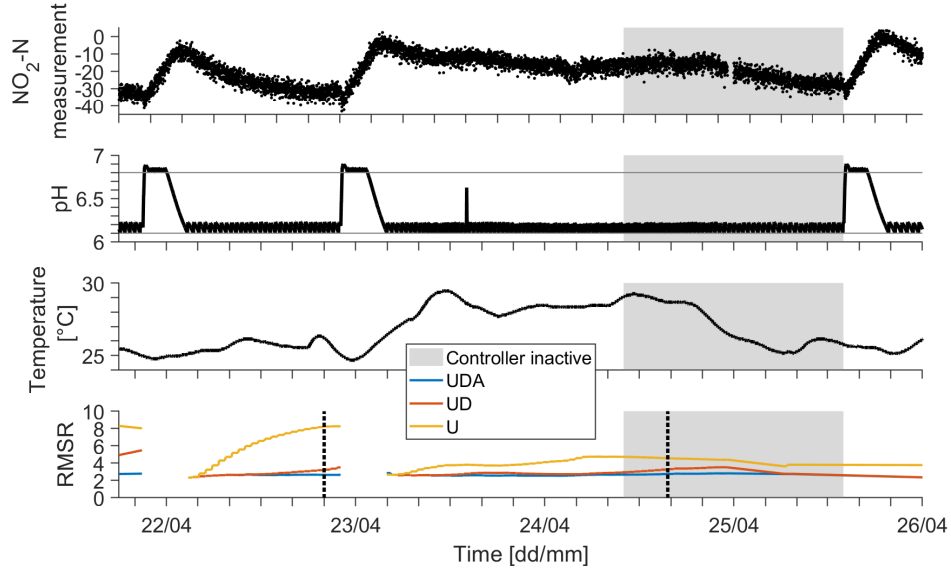


Figure 7: Temperature high experiment. 1st panel: Nitrite signal and nitrite reference measurements. 2nd panel: pH measurement. The grey area marks the period during which the controller was inactive. 3rd panel: Temperature measurement. 4th panel: RMSR of the three models U, UD, UDA including the time points at which the inflection point was identified.

451 4. Discussion

452 This study proposes a new concept for a stabilizing control in the pres-
 453 ence of signal drift and demonstrates its utility by means of an intensive
 454 measurement campaign in a laboratory-scale reactor for urine nitrification.

455 The proposed control system avoids the effects of signal drift by using infor-
456 mation in the first and second derivative to distinguish between stabilizing
457 and destabilizing process conditions. The results reveal that the controller
458 successfully stabilised the nitrification process despite using a sensor signal
459 that is drifting permanently. Importantly, this could be achieved without
460 redundant actuators or sensors and without a precise kinetic model of the
461 process.

462 *4.1. System performance*

463 The end of cycle nitrite concentrations at the end of the control cycles
464 were shown to decrease over time. This may indicate an adaption of the
465 NOB to the elevated nitrite levels or could also be caused by the influent
466 switch. Since steady state was not reached during the studied period, one
467 cannot determine with absolute certainty whether the reported decrease is
468 caused by a net decay of the AOB or a net growth of the NOB. Since the
469 average pH in the reactor is higher than in the conventional operation with
470 a constantly safe but low pH, this controller should theoretically also achieve
471 higher nitrification rates (Udert and Wächter, 2012). However, pH is only
472 one among many factors influencing the nitrification rates. Bürgmann et al.
473 (2011) showed that long-term exposure to nitrite could jeopardise the pro-
474 cess, while van Hulle et al. (2007) hypothesised that bacteria become more
475 tolerant when exposed long enough to elevated nitrite concentrations. Conse-
476 quently, future research should be aimed at understanding long-term reactor

477 performance indicators in the presence of stabilizing control loops.

478 4.2. *Unmeasured Disturbances*

479 Our study shows that fast introduction of unmeasured disturbances can
480 threaten the suitability of the proposed trend-based control concept. To
481 understand why this is the case, one must note that the controller is based on
482 the assumption that the appearance of an inflection point in the downward
483 nitrite signal can only be explained by a change of from NOB-inhibiting
484 to non-inhibiting nitrite concentration levels. To challenge this assumption
485 as well as the control concept, two confounding factors were disturbed on
486 purpose (temperature and influent composition).

487 The temperature increase experiment indicates that unmeasured distur-
488 bances can make the proposed control system fail. This is explained as an ef-
489 fect on the μ AOB to μ NOB ratio, which increases with temperature. Indeed,
490 the fast temperature increase of the bulk media introduced the appearance
491 of an inflection point. However, the assumption that the inflection point is
492 solely caused by NOB dynamics does not hold any longer and explains the
493 wrongful control action. While nitrite concentration does not yet reach the
494 NOB-inhibiting region after one cycle, the early increase of the pH setpoint,
495 induces an additional increase in the nitrite concentration. Such a higher
496 concentration will likely inhibit the NOB and activate a positive feedback
497 loop between the nitrite concentration, in turn inducing an increased risk
498 of NOB wash-out in the long term. The temperature high experiment did

499 reveal another important condition for correct functioning of the controller.
500 The low amplitude of the signal (Fig. 7, 24th afternoon) delays the identifi-
501 cation of the inflection point. This shows the need for sufficient excitement
502 of the process and the signal to reach a large enough signal-to-noise ratio.
503 However, increased excitation also increases the risk of irreversible process
504 failure (i.e., Fig. 1, exceed point B).

505 The influent switch experiment did not influence the observed signal pro-
506 files in a meaningful way. As a result, the controller was able to execute the
507 right control actions in a timely manner throughout the course of this test.
508 There are two explanations for this: First, the model to derive the nitrite
509 concentrations from the UV-Vis absorbance measurement is apparently quite
510 robust against changes in the reactor media composition, particularly large
511 changes of the nitrate concentration (Fig. 6). Second, the dynamics caused
512 by the influent switch are driven by the HRT and decreased from 13 to 7 d.
513 Thus, this disturbance is much smoother than the temperature experiments
514 with a time window of 0.5 d.

515 *4.3. Extension of controller*

516 The modifications applied to enable SCS analysis in an online environ-
517 ment worked without any complications. The main modification consisted of
518 embedding the SCS as a model selection tool in a moving horizon estimation
519 framework with a fixed start point. Despite concerns about the computa-
520 tional costs by Villez et al. (2013) the three SCS models could be fitted to

521 the data within less than 3 seconds on an Intel[®] core i7 4970k 4 GHz pro-
522 cessor. Thus, conventionally available computational resources are expected
523 to be sufficient for most biochemical process monitoring applications. Faster
524 computations, e.g. for fast processes or when dealing with high-frequency
525 data collection systems, can be facilitated by increasing the knot distance of
526 the spline functions. If computational cost is no concern at all, then the knot
527 distance can be reduced to improve the fit of the applied SCS models.

528 So far, the controller makes the nitrite concentration oscillate around
529 the optimal concentration for maximal μ NOB. The upper setpoint has to
530 ensure that nitrite is always accumulating to keep the signal informative.
531 The lower setpoint has to ensure net nitrite degradation to stabilise the
532 process. Choosing the setpoints can be challenging and some disturbances
533 may influence the system such that the chosen pH setpoints cannot push
534 the process into the intended operational region. Enabling the controller to
535 decide how the two pH setpoints itself should be set would also facilitate
536 process optimization.

537 One way to obtain a good ratio of the AOB activity to the NOB activity
538 at both pH setpoints was revealed in the high temperature experiment. The
539 increased temperature leads to a relatively high AOB rate at low pH. This in
540 turn resulted in slow net nitrite degradation and thus a flat decreasing trend
541 in the signal compared to the previous increase. Thus, the pH setpoints
542 and in turn, the overall process performance, was rather high for the given
543 NOB capacity. Potentially, computing the ratio of the increasing and the

544 decreasing slope in one cycle allows optimizing the pH setpoints and in turn
545 the process performance for the next cycle. Furthermore, using this kind
546 of information would also help to reject additional disturbances without the
547 need for additional instrumentation (cf. high temperature experiment).

548 4.4. *Links to existing control theory*

549 The proposed controller is based largely on a conceptual model of sub-
550 strate affinity and inhibition in nitrifying bacteria. Assuming that the NOB
551 activity, and thus also the nitrite conversion rate, has a unimodal shape with
552 respect to the nitrite concentration, one can expect to observe an inflection
553 point whenever the process shifts from conditions dominated by nitrite in-
554 hibition to conditions dominated by nitrite limitation. This information is
555 key to avoid the need for any explicit correction of the signal drift since it is
556 contained in the derivatives. Importantly, the actions taken by the controller
557 can also be interpreted as the execution of an online experiment to deter-
558 mine the NOB kinetics. Microbial populations adapt over time and thus it
559 is highly likely that the inhibition and affinity constants of these population
560 change. Consequently, a sensor signal without relevant drift as input would
561 allow tracking the optimal concentration of nitrite for a maximal μ_{NOB} .

562 This is also important with view on the many nitrification controllers
563 equating nitrification with ammonia removal while nitrite oxidation is as-
564 sumed to be completed simultaneously. Consequently, single indicators such
565 as ammonia concentration, pH valley, or OUR drop have been assumed in-

566 formative enough to control the process (Åmand et al., 2013; Jaramillo et al.,
 567 2018; Thürlimann et al., 2018). This is justifiable in some situations (e.g.,
 568 municipal WWTP). However, in certain situations, analysis of both ammonia
 569 oxidation and nitrite oxidation is key for process stability and optimization.
 570 Partial nitrification/anammox (Lotti et al., 2012) or on-site WWTP, which
 571 can be limited by alkalinity are examples of this. We speculate that the
 572 proposed control concept can be used whenever derivatives are informative
 573 about the concentration trend of a relevant substance. The benefits of con-
 574 trollers executing online experiments to determine process states in contin-
 575 uously operated reactors are rarely studied in wastewater treatment. Steyer
 576 et al. (1999) also deliberately induced process disturbances to gain infor-
 577 mation about the performance of an anaerobic reactor. In contrast to the
 578 presented controller, they compared the information against a simple model
 579 to determine the performance.

580 The intentional excitement or perturbation of a system also has a theo-
 581 retical basis in the form of extremum seeking control (ESC) (Liu and Krstic,
 582 2012). Both ESC and the presented trend-based controller are model-free,
 583 feedback controllers that purposely excite the system to gain information.
 584 However, by default ESC requires an excitement frequency that is much
 585 lower than the dominant process frequency. This is not the case here as
 586 the biomass growth dynamics ($\text{HRT} = 13 \text{ d}$) and the excitement frequency
 587 (1 d^{-1}) appear in the same time scale. Trollberg et al. (2014) found that
 588 the combination of a slow process and low excitement frequency as found in

wastewater treatment make current forms of ESC impractical. They further stated that knowledge about the system behaviour close to the optimum is crucial to facilitate the use of ESC. Using ESC could however facilitate the inclusion of the ideas presented in 4.3. Thus, ESC may be helpful urine nitrification process optimization, in addition to ensuring long-term stability of the process.

5. Conclusion

In this study, a stabilizing controller for nitrification in high strength wastewater was developed and critically evaluated. The controller successfully prevents the occurrence of destabilizing nitrite accumulation events in an alkalinity limited urine nitrification reactor for the entire test period of 72 days. These are the main conclusions:

- Information contained in the derivatives of a drifting signal combined with qualitative knowledge about kinetics allowed for the control of an open-loop unstable system without the need for drift rate estimation or correction.
- Systems without any dynamics due to input or operation can be excited deliberately in such a way that the signal derivatives contain the information of interest about the process states. In this study, the controller was designed to destabilise the nitrification such that the signal derivatives contain the necessary information about the pro-

610 cess state, in turn enabling stabilizing feedback control. Somewhat
611 counter-intuitively, deliberate short-term destabilization facilitates the
612 assurance of long-term process stability.

- 613 • The controller is based on a conceptual model of the process. This
614 model currently excludes the effect of unmeasured disturbances other
615 than the signal drift. This constitutes the most sensitive component of
616 our proposed controller. Whereas slow unmeasured disturbances were
617 successfully rejected, information in the controller input signal inform-
618 ing about fast, unmeasured disturbances were identified and considered
619 for inclusion into the control logic.

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