Exercise 2

Modelling Aquatic Ecosystems FS25

Today's agenda

- Q&A of last week's exercise
- Intro to phytoplankton zooplankton model
- Recap on elements in process rates
- Break
- Work on the exercise on your own
- Discussion of theory questions

Q&A of last week's exercise

Are there any open questions on Exercise 1? Homework solution visualization:



seasonally varying external conditions:

Reminder: The solutions are available on the course website https://www.eawag.ch/en/department/siam/teaching/modelling-aquatic-ecosystems/#c21285

Question 1

How can you derive the total (net) transformation rate of $C_{\text{HPO}_4^{-2}}$ and C_{ALG} from the process table (Table 11.1) and the process rates (Table 11.2)?

Hint: see equation (4.1) in the manuscript. What are the units?



Question 1 - Answer

$$r_{Alg} = k_{gro, Alg} \times \frac{C_P}{K + C_P} \times C_{Alg} - k_{death, Alg} \times C_{Alg}$$
$$[r_{Alg}] = \frac{1}{d} \times \frac{gDM}{m^3} = \frac{gDM}{d \times m^3}$$

$$r_{P} = -\alpha_{P,Alg} \times k_{gro,Alg} \times \frac{C_{P}}{K + C_{P}} \times C_{Alg}$$
$$[r_{P}] = \frac{gP}{gDM} \times \frac{1}{d} \times \frac{gDM}{m^{3}} = \frac{gP}{d \times m^{3}}$$

Question 2

Look at the state variables $C_{\text{HPO}_4^{2-}}$ and C_{ALG} . Which of them is more sensitive to the parameter $K_{\text{HPO}_4^{2-}}$, $_{\text{ALG}}$ and which of them is more sensitive to $C_{\text{in, HPO}_4^{2-}}$? Do you understand why?

Question 2 - Visualization



Look at the Manuscript in the chapter 11.1 (pp.170-174)

Intro to exercise 2 phytoplankton – zooplankton model



What constitute process rates ?

Process Rates (4.2)

Process rates depend on nutrients and organisms concentrations and can often be written in the form of a base rate with limiting and inhibiting factors.

Process formulation with multiplicative factors:



Process Rates (11.2)

Model with constant driving forces (Table 11.5):



linear death rate

Process Rates (11.2)

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Model with seasonally varying driving forces (Table 11.6):

$$T(t) = \frac{T_{\max} + T_{\min}}{2} + \frac{T_{\max} - T_{\min}}{2} \cos\left(2\pi \frac{t - t_{\max}}{t_{\text{per}}}\right)$$

$$I_0(t) = \frac{I_{0,\max} + I_{0,\min}}{2} + \frac{I_{0,\max} - I_{0,\min}}{2} \cos\left(2\pi \frac{t - t_{\max}}{t_{\text{per}}}\right)$$



Rate	Rate expression
$ ho_{ m gro,ALG}$	$k_{\text{gro,ALG},T_0} \left\{ \exp\left(\beta_{\text{ALG}}(T-T_0)\right) \right\} \left\{ \frac{1}{\lambda h} \log\left(\frac{K_I + I_0}{K_I + I_0 \exp(-\lambda h)}\right) \right\}$
	temperature dependence $C_{HPO_4^{2-}} + C_{ALG}$
	$^{11}\mathrm{HPO}_{4}^{2-},\mathrm{ALG}^{+}\mathrm{C}\mathrm{HPO}_{4}^{2-}$
$\rho_{\rm death,ALG}$	$k_{\text{death,ALG}} C_{\text{ALG}}$
$ ho_{ m gro,ZOO}$	$k_{\text{gro},\text{ZOO},T_0} \left\{ \exp\left(\beta_{\text{ZOO}}(T-T_0)\right) \right\} C_{\text{ALG}} C_{\text{ZOO}} $ light dependence
$\rho_{\rm death,ZOO}$	$k_{\rm death,ZOO} C_{\rm ZOO}$

Time to work on Exercise 2

Theory questions

- Are the algae concentrations controlled bottom-up (by phosphate limitation) or top-down (by grazing of zooplankton)?
- What is the reason for oscillating concentrations under constant driving forces? What happens when you introduce periodic driving forces?
- What are the main deficits of the model compared to a real lake?
- What is your expectation regarding the response of the model to the change in each parameter, does the result match your expectation and can you explain the observed changes?

Homeworks:

- Task 4 Sensitivity analysis
- Theory questions

Don't hesitate to send us an e-mail if you have any questions.

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Have a nice day !